

## A STUDY ON THE BEHAVIOUR OF A TAGGED VEHICLE USING IRREDUCIBLE SMP MODEL

M. RENI SAGAYARAJ\*<sup>1</sup>, C. BAZIL WILFRED<sup>2</sup>, S. UDAYABASKARAN<sup>3</sup>,  
S. ANAND GNANA SELVAM<sup>4</sup>

<sup>1,4</sup>Department of Mathematics,  
Sacred Heart College (Autonomous), Tirupattur, India.

<sup>2</sup>Department of Mathematics,  
Karunya University, Coimbatore, India.

<sup>3</sup>Department of Mathematics,  
Vel Tech University, Avadi, Chennai, India.

(Received On: 21-04-15; Revised & Accepted On: 30-05-15)

---

### ABSTRACT

*The tagged vehicle is in idle state with probability  $u_b$  if there is no packet. After a packet is generated, the vehicle goes from state idle to state CS 1 with probability  $1 - u_b$ , here the vehicle senses channel activity for DIFS time period. If the channel is detected not busy during this period (DIFS) (with probability  $1 - q_b$ ), the vehicle goes from idle state to TX state, which means that a packet is transmitting. Otherwise, the vehicle will defer until channel is idle for DIFS duration represented by state DCS. Such deference behavior for the tagged vehicle includes two parts: waiting for the current packet in the channel finishing transmission and waiting for subsequent transmissions if any from other neighbors within its receiving range.*

---

### INTRODUCTION

The self-loop for state DCS represents the phenomena in Fig (5.3) that the tagged vehicle (vehicle B) waits for the current packet (from vehicle A) in the channel finishing transmission, and then senses the channel for DIFS time, which seizes the transmission from another vehicle (vehicle C) and leads to further deference for backoff procedure of vehicle B. The probability that the tagged vehicle detects another neighbors transmission during DIFS time is denoted as  $r_b$ . If no other neighbors transmission is detected, the tagged vehicle will start backoff procedure and randomly choose a backoff counter in the range  $[0, W - 1]$ , where  $W = CW + 1$  is the backoff window size.

### I. THE MODEL DESCRIPTION WITH MODIFIED SMP MODEL FOR BEACON MESSAGE DISSEMINATION

The backoff counter will be decreased by one if the channel is detected to be idle for a time slot of duration  $\sigma$  (with probability  $1 - p_b$ ), which is captured by the transition from state  $W - i$  to state  $W - i - 1$ .

If the channel is busy during a backoff time slot of duration  $\sigma$  (i.e., another vehicle starts to transmit a packet during this time slot), the backoff counter of the tagged vehicle will be suspended, which represented by the transition from state  $W - i$  to  $DW - i - 1$  with probability  $p_b$ . Similar to state DCS, state  $DW - i - 1$  also contains self-loop because other neighbors transmission can lead to further deference of the tagged vehicle. When the backoff counter reaches zero, the packet will directly be transmitted (an SMP transition occurs from state 0 to state TX with probability one). In TX state, a packet is transmitting. To capture the out-dated packet replacement behavior, which can happen during any state except state idle, we simplify the model by considering the total replacement probability and placing it after state TX. If the current packet has not been replaced by the next packet (with probability  $1 - P_f$ ), the SMP goes to state idle.

---

*Corresponding Author: M. Reni Sagayaraj\*<sup>1</sup>*

Otherwise, this current packet is out-dated and replaced by the next incoming packet. Such simplification is reasonable since the packet transmission delay is usually much smaller than the packet generation interval and hence the replacement occurs extremely rare. Next, the tagged vehicle starts the service for the next packet immediately and senses the channel for DIFS time (state  $CS_2$ ). A new backoff procedure is started subsequently for the new packet instead of inheriting the backoff state of the old message. This is mainly because the out-dated message may finish the backoff procedure and is replaced during its transmission. The SMP model proposed here captures more detailed DCF behavior for periodic beacon message transmission by adding more states and self-loop structure. In addition, out-dated message replacement behavior is incorporated into the model by the newly introduced model parameter  $P_f$ . The sojourn time in state  $j$  is defined as  $T_j$ . The mean and variance of  $T_j$  in the SMP model are:

$$E[T_j] = \tau_j = \begin{cases} A_1 & j = TX \\ A_2 & j = idle \\ A_3 & j = CS_1, CS_2 \\ A_4 & j = D_{cs} \\ A_5 & j = D_0, D_1, D_2, \dots, D_{W-2} \\ 0 & j = 0 \\ \sigma & j = 1, 2, 3, \dots, W-1 \end{cases}$$

$$Var[T_j] = 0_j^2 = \begin{cases} 0 & j \in U \text{ (set of states expect idle)} \\ B_1 & j = idle \end{cases}$$

Where

$$\begin{cases} A_1 = \frac{PL}{R_d} \\ A_2 = \tau - E[s] \\ A_3 = DIFS \\ A_4 = \frac{(A_1 + DIFS)}{2} \\ A_5 = A_1 + DIFS \end{cases}$$

And

$$B_1 = \text{var}[s]$$

$T_H$  presents the time to transmit the packet header including physical layer header and MAC layer header.  $E[S]$  and  $Var[S]$  are the mean and variance of the overall message service time, which will be derived later. The sojourn time in state *idle* is the packet inter arrival time excluding the packet service time. In addition, to simplify the model, the sojourn times for channel sensing states ( $CS_1$ ,  $CS_2$ , and  $i = 0, 1, \dots, W-1$ ) are modeled as deterministic using the upper bound channel sensing time (i.e., the sensing for each state only performs once). Such simplification may have impact on dense network in which channel contentions are severe. Moreover, the sojourn time in state  $D_{CS}$  is different from that in  $D_i$  ( $i = 0, 1, \dots, W-2$ ) is because the packet transmission from another vehicle may already started before the new packet is generated from the tagged vehicle. Therefore, on average, the tagged vehicle only defers for a half of the packet transmission time plus an additional idle DIFS duration in state  $D_{CS}$ . In contrast, for state  $D_i$  ( $i = 0, 1, \dots, W-2$ ), the start point of packet transmission from another vehicle is detected within the backoff time slot (state  $i+1$ ), and hence the tagged vehicle needs to defer for the whole packet transmission time plus an additional idle DIFS duration. The embedded DTMC is solved for its steady-state probabilities for each state:

## II. BALANCE EQUATION FOR THE STATES

**For the State  $DCS$**

$$(1-rb)vDCS + vDVS \quad rb = vDVS \quad rb + vCS_1qb$$

Therefore

$$v_{DCS} = \frac{vCS_1}{(1-rp)^v} q \quad (1)$$

**For the state  $CS_1$**

$$vCS_1qb + vCS_1(1-qb) = v_{idle} \cdot (1-ub)$$

Therefore

$$vCS_1 = v_{idle} \cdot (1-ub) \quad (2)$$

**For the idle state**

$$v_{idle}(1-ub) + v_{idleub} = vTX(1-pf)v_{idleub}$$

$$v - v_{idleTX} \frac{(1-pbf)}{(1-u)} \quad (3)$$

**For the state  $TX$**

$$vTX = vCS_1(1-qb) + v_0$$

$$vTX = vCS_1(1-qb) + v_0$$

**For the state  $CS_2$**

$$vCS_2.1 = vTXpf \quad (5)$$

$$v_{0.1} = v_{DCS} \left( \frac{1-r_b}{w} \right) + v_{CS_2} \frac{1}{w} + v_1(1-p_b) + v_{D_0}(1-r_b)$$

$$v_0 = v_{DCS} \left( \frac{1-r_b}{w} \right) + v_{CS_2} \frac{1}{w} + v_1(1-p_b) + v_{D_0}(1-r_b)$$

$$v_1 = v_{DCS} \left( \frac{1-r_b}{w} \right) + v_{CS_2} \frac{1}{w} + v_2(1-p_b) + v_{D_1}(1-r_b)$$

.....  
 .....

$$v_j = v_{DCS} \left( \frac{1-r_b}{w} \right) + v_{CS_2} \frac{1}{w} + v_{j+1}(1-p_b) + v_{D_j}(1-r_b) \quad (6)$$

.....  
 .....

$$v_{w-2} = v_{DCS} \left( \frac{1-r_b}{w} \right) + v_{CS_2} \frac{1}{w} + v_{w-1}(1-p_b) + v_{D_{w-2}}(1-r_b)$$

$$v_{w-1} = v_{DCS} \left( \frac{1-r_b}{w} \right) + v_{CS_2} \frac{1}{w} \quad (7)$$

Substituting the equation (7) in (6) we get

$$\begin{aligned} v_j &= v_{w-1} + v_{j+1}(1 - p_b) + v_{D_j}(1 - p_b), j = 0, 1, 2, \dots, w-2 \\ v_j - v_{j+1} &= v_{w-1} + p_b v_{j+1} + (1 - r_b) v_{D_j}, j = 0, 1, 2, \dots, w-2 \end{aligned} \quad (8)$$

Substituting  $j=0, 1, 2, \dots, (w-2)$  in equation (8) and summing up we get

$$\begin{aligned} v_0 - v_1 &= v_{w-1} - p_b v_1 + (1 - r_b) v_{D_0} \\ v_1 - v_2 &= v_{w-1} - p_b v_1 + (1 - r_b) v_{D_1} \end{aligned}$$

.....

.....

$$v_0 - v_{w-1} = v_{w-1} - p_b v_{w-1} + (1 - r_b) v_{D_{w-1}}$$

Adding the above equations we get

$$v_0 - v_{w-1} = (w-1)v_{w-1} - p_b(v_1 + \dots + v_{w-1}) + (1 - r_b)(v_{D_0} + \dots + v_{D_{w-2}}) \quad (9)$$

## CONCLUSION

In this paper the mathematical analysis for each state of the semi markov process is completely evaluated and the behaviour of the beacon message contenting for the channel resource is modeled. Also the steady state probability for the vehicle in transaction state is derived. The service time distribution using SMP model is evaluated.

## REFERENCE

1. Bae, Y. H., Kim, K. J., Moon, Mi-Nam. and Choi, B. D. (2008), Analysis of IEEE 802.11 non-saturated DCF by matrix analytic methods, Ann. Oper Res., Vol. 162, pp. 3-18.
2. Bastani, S., Landfeldt, B. and Libman, L. (2011), On the Reliability of Safety Message Broadcast in Urban Vehicular Ad hoc Networks, Proc. ACM int. conf. on Modeling, Analysis and Simulation of Wireless and Mobile Systems, , pp. 307-316.
3. Behrouz A. Forouzan. (2007), Data Communications and Networking., IV Edition, 2007.
4. Bianchi, G. (2000), Performance analysis of the IEEE 802.11 distributed coordination function, IEEE Journal on Selected areas in Communications, Vol. 18(3), pp. 535- 547.
5. Breuer, L., Baum, D. (2005), An Introduction to Queueing Theory and Matrix- Analytic Methods.
6. Choi, J., Alazemi, H.M.K., Vijayakumar, R., Margolis, A., Roy, S., Choi, B. D. (2007), Analysis of 802.11 DCF with Heterogeneous Non-Saturated Nodes, Computer Communications, Vol. 30 (18), pp. 3652- 3661.
7. Dharma, P. A., Qing-An, Z. (2011) Introduction to Wireless & Mobile Systems. Cengage Learning.
8. Duffy, K., Malone, D. and Leith, D. (2005), Modelling the 802.11 Distributed Coordination Function in Non-saturated Conditions, IEEE Commun. Lett, Vol. 9 (8), pp. 715-717.
9. ElBatt, T.A., Goel, S. K., Holland, G., Krishnan, H., Parikh, J. S. (2006), Cooperative collision warning using dedicated short range wireless communications, Proceeding of ACM VANET workshop,.
10. IEEE Standard for Information technology Telecommunications and information exchange between systems Local and metropolitan area networks Specific requirements (June 2007).
11. Kim, T. O., Kim, K. J. and Choi, B. D. (2008), Performance Analysis of IEEE 802.11 DCF and IEEE 802.11e EDCA in non-saturated conditions, IEICE Trans. Commun., Vol. RE91-B(4), pp. 1122-1131.
12. Ma, X., Chen, X. and Refai, H. H. (2009), Performance and Reliability of DSRC Vehicular Safety Communication: A Formal Analysis, EURASIP Journal on Wireless Comm. and Networking, Vol. 2009(969164), pp. 1-13.
13. Torrent-Moreno, M. (2007), Inter-Vehicle Communications: Achieving Safety in a Distributed Wireless Environment: Challenges, Systems and Protocols, PhD- dissertation, Karlsruhe,.
14. Wah-Chun, C. (2002), Performance Analysis of Telecommunications and Local Area Networks.
15. Winands, E., Denteneer, J., Rensing. and Riteman, R. (2005), A finite source feedback queueing network as a model for the IEEE 802.11 distributed coordination function, European Transactions on Telecommunications, Vol. 16, pp. 77-89.

16. Yin, X., Ma, X. and Tirvedi, K.S. (2011), Performance Evaluation for DSRC Vehicular Safety Communication: A Semi-Markov Process Approach, Int. Conf. on Comm. Theory, Rel., and Quality of Service,, pp. 9-14.
17. Yin, X., Ma, X. and Tirvedi, K.S. (2013), An Interacting Stochastic Models Approach for the Performance Evaluation of DSRC Vehicular Safety Communication, Computers, IEEE Transactions, pp. 873-885.
18. Yin, X., Ma, X. and Tirvedi, K.S. (2014), MAC and application level performance evaluation of beacon message dissemination in DSRC safety communication, Performance Evaluation, Vol. 71, pp. 1 - 24.

**Source of support: Nil, Conflict of interest: None Declared**

***[Copy right © 2015. This is an Open Access article distributed under the terms of the International Journal of Mathematical Archive (IJMA), which permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly cited.]***