# THE INFLUENCE OF WALL PROPERTIES ON PERISTALTIC TRANSPORT OF DUSTY FLUID THROUGH POROUS MEDIUM

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# ABSTRACT

This paper investigates peristaltic transport of a dusty fluid (Saffman's model) through a Porous Medium in a twodimensional uniform channel and the elasticity of the channel's flexible walls was studied under long wavelength approximation. Perturbation solutions were obtained for the stream functions of both the fluid particles and solid particles, in terms of the wall slope parameter. The expressions for average velocity of the fluid particles and solid particles, and average fluid flow rate were derived. The effects of various elastic parameters and mass concentration of dust particles on the streamline pattern and average fluid flow rate were studied. The phenomenon of trapping was observed and the area of the trapped bolus increased along with the tension parameter and permeability of the porous medium, but decreased with damping, mass concentration of dust particles.

Key words: Peristaltic transport. Wall properties. Dust particles. Porous medium.

# **1. INTRODUCTION:**

A fluid transport induced by a progressive wave of area contraction or expansion along the length of a distensible tube containing fluid is called Peristaltic transport. Areas of applications of peristaltic flows cover widely the transport of fluids in physiological systems, in biomedical instruments, in industry, etc. This is known to be a major mechanism in biological systems, including urine transport from the kidneys to the bladder through the ureter. The industrial use of Peristaltic pumping in roller/ finger pumps is well known. Engineers to pump corrosive materials and fluids that must be kept away from pumping machinery have adopted this principle. In particular, the peristaltic transport of toxic liquid is used by the nuclear industry so as not to contaminate the environment. Peristaltic pumping is used in biomedical devices such as the heart-lung machine to pump blood. It is also speculated that peristalsis may be involved in the translocation of water in tall trees. The translocation of water involves its motion through the porous matrix of the trees.

Many of these studies explained the basic fluid mechanical aspects of peristalsis and two important phenomena trapping and reflux. Reflux refers to the net retrograde motion of some part of a fluid in a direction opposite that of wave propagation on the wall, trapping is the development, and transport of an internally circulating bolus of fluid was worked by Shapiro et al., [20]. Fung and Yih [1] observed that pumping against a positive pressure gradient than a critical value results in a backward flow in the central region of the stream. The literature on this topic is quite extensive. An elaborate review of the earlier literature regarding peristalsis is provided by Jaffrin and Shapiro [3]. As the behavior of most physiological fluids is known to be non-Newtonian, attempts have been made to analyze the peristaltic transport of non-Newtonian fluids. Several researchers Picologlou et al.[8], Srivatsava [24], Philip and Pecyush [7], Misery et al. [5], Srinivacharya et al. [21] that described the non-Newtonian behavior of fluids as power law, couple stress, simple micro, micro polar, and generalized Newtonian fluid models, respectively investigated peristaltic transport of blood in small vessels.

Saffman's [19] dusty fluid model serves as a good model for describing blood as a binary system. Kaimal [4] studied peristaltic transport of a solid- fluid mixture at a low Reynolds number under long wavelength approximation. Radhakrishnamacharya [9] studied the pulsatile flow of a fluid containing small solid particles through a two-dimensional constricted channel. Mitra and Prasad [6] studied peristaltic transport of a Newtonian viscous fluid in a two-dimensional uniform channel while considering the elasticity of the wall. They reported that flow reversal occurs at the center of the channel if the walls of the channel are elastic and that the position may shift to the boundaries if the viscous damping forces are considered.

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Srinivasalu and Radhakrishnacharya [22] studied peristaltic transport in a non-uniform channel with elastic effects. Srinivasacharya et al. [23] studied the effect of wall properties on peristaltic transport of a dusty fluid. Study of this interaction under different conditions may lead to a better understanding of the role of peristalsis in the transport of physiological fluids. Roni [18] studied Mathematical Modeling of unsteady dusty visco-elastic fluid flow through inclined channels. Rathod and Seema Jabeen [10] studied pulsatile flow of blood with volume fraction of microorganisms and gravity effect. Rathod and Seema Jabeen [11] studied Pulsatile two layer blood flow with volume fraction of microorganisms and gravity. Rathod and Srinivas [12] studied the flow of blood with microorganisms in capillaries of small exponential divergence through stenosed tube. Gireesha et al. [2] studied Flow of Unsteady Dusty Fluid under Varying Pulsatile Pressure Gradient in Anholonomic Co-ordinate System.

Rathod and Srinivas [13] studied pulsatile flow of blood through a stenosed tube in two-layer model with effect of volume fraction of microorganisms. Rathod and Asha [14] studied effect of couple stress fluid and an endoscope in peristaltic motion. Rathod and Srinivas [15] studied pulsatile flow of blood through a stenosed tube with effect of volume fraction of micro-organisms. Rathod and Shakera Tanveer [16] studied pulsatile flow of Couple Stress Fluid through a Porous medium with Periodic Body Acceleration and Magnetic Field. Rathod and Mahadev [17] studied Effect magnetic field on urethral peristalsis in cylindrical tube. Srinivas and Gayathri [25] studied peristaltic transport of a Newtonian fluid in a vertical asymmetric channel with heat transfer and porous medium.

In recent years, the flows of dusty fluid through porous media have attracted the attention of a number of research scholars because of their possible applications in many branches of science and technology. Flows through the porous medium occur in filtration of fluids and seepage of water in riverbeds. Another example is the seepage under a dam, which is very important. In fact, a porous material containing the dusty fluid is a non-homogeneous medium but it may be possible to treat it as a homogeneous one.

The present research is aimed to study the effects of wall properties on peristaltic transport of a dusty fluid (Saffman's model) through a Porous Medium in a two-dimensional channel. The expressions for average velocity of the fluid particles and solid particles, and average fluid flow rate were derived. The effects of various elastic parameters and mass concentration of dust particles on the streamline pattern and average fluid flow rate were studied.

# 2. FORMULATION OF THE PROBLEM:

Consider the laminar flow of an incompressible fluid that contains small solid particles, whose number density (N) (assumed to be a constant  $N_0$ ) is large enough to define average properties of the dust particles at a point through a symmetrical two-dimensional channel. Peristaltic waves of long wavelength are assumed to travel along the walls of the channel.

The geometry of the wall surface is described by

$$\eta = d + a \sin\left(\frac{2\pi}{\lambda}(x - ct)\right)$$
(2.1)

Where d is the width of the channel, a is the amplitude of the wave,  $\lambda$  is the wavelength and t is time.

The equations of motion for viscous incompressible fluid with uniform distribution of solid particles are given by Saffman [19]. The flow of the fluid is governed by the continuity and momentum equation,

$$\nabla . V = 0 \tag{2.2}$$

$$\frac{\partial V}{\partial t} + (V \cdot \nabla)V = -\frac{1}{\rho}\nabla p + \upsilon\nabla^2 V + \frac{KN_0}{\rho}(V_s - V) - \frac{\upsilon}{k}V$$
(2.3)

Where V = [u, v] is the velocity of the fluid particles, p is the fluid pressure, k is the permeability of porous medium,  $\rho$  is the density of the fluid, v is the kinematic coefficient of the viscosity of fluid, and K is the resistance coefficient for the dust particles- a constant. The first two terms on the right side of Eq. (2.3) are, respectively, the pressure gradient and viscosity terms. The last term represents the force due to the relative motion between the fluid and solid particles. It is assumed that the Reynolds number of the relative velocity is small. In such a case, the force between the solid and fluid is proportional to the relative velocity.

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Figure-1: Geometry of two-dimensional peristaltic motion of channel wall.

The motion of the dust particles is governed by Newton's second law is

$$\nabla . V_{s} = 0 \tag{2.4}$$

$$\frac{\partial V_s}{\partial t} + (V_s \cdot \nabla) V_s = \frac{K}{m} (V - V_s)$$
(2.5)

Where  $V_s = [u_s, v_s]$  is the velocity of solid particles and  $\mathcal{M}$  is the mass of the solid particles.

The governing equation of motion of the flexible wall may be expressed as

$$L(\eta) = p - p_0 \tag{2.6}$$

Where L is an operator that is used to represent the motion of the stretched membrane with damping forces such that

$$L = -T \frac{\partial^2}{\partial x^2} + m' \frac{\partial^2}{\partial t^2} + C \frac{\partial}{\partial t}$$
(2.7)

Here, T is the tension in the membrane, m' is mass per unit area, C is the coefficient of viscous damping forces, and  $p_0$  is the pressure on the outside of the wall due to tension in the muscles. This tension may be due to the constitutive relations of the muscles when the displacements are known. Certain terms may be added to Eq. (2.7) to account for spring foundations, but they do not change the mathematical nature of the problem; therefore, to keep the analysis simple they are not considered herein (Mitra and Prasad, 1973).

It is assumed that  $p_0 = 0$  and the walls of the channel are inextensible, so that only their lateral motion takes place and the horizontal displacement of the wall is zero. Thus, the no-slip boundary condition for the velocities is

$$u = 0, u_s = 0 \text{ At } y = \pm \eta \tag{2.8}$$

Continuity of stresses requires that at the interfaces of the walls and fluid, p must be the same as that which acts on the fluid at  $y = \pm \eta$ . The use of the x-momentum equation yields

$$\frac{\partial}{\partial x}(L(\eta)) = \frac{\partial p}{\partial x} = \rho v \left[ \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right] - \rho \left[ \frac{\partial u}{\partial x} + u \frac{\partial u}{\partial y} + v \frac{\partial u}{\partial y} \right] + \frac{KN_0}{\rho} (u_s - u) - \frac{v}{k} u$$
  
at  $y = \pm \eta$  (2.9)

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Introducing the steam functions  $\Psi$  and  $\phi$  such that

$$u = \frac{\partial \psi}{\partial y}, v = -\frac{\partial \psi}{\partial x}, u_s = \frac{\partial \phi}{\partial y}, v_s = -\frac{\partial \phi}{\partial x}$$
(2.10)

and following non-dimensional variables

$$x' = x / \lambda, y' = y / d, \eta' = \eta / d, t' = (vt) / (\lambda d), \psi' = \psi / v, \phi' = \phi / (Kd^2 / m)$$
(2.11)

into equations (2.2)- (2.5), we obtain the following equations (after dropping primes and eliminating the pressure term)

$$\delta\left[\frac{\partial}{\partial t}\left(\nabla_{1}^{2}\psi\right) + \frac{\partial\psi}{\partial y}\frac{\partial}{\partial x}\left(\nabla_{1}^{2}\psi\right) - \frac{\partial\psi}{\partial x}\frac{\partial}{\partial y}\left(\nabla_{1}^{2}\psi\right)\right] = \nabla_{1}^{4}\psi + P\left[\frac{1}{R}\nabla_{1}^{2}\phi - \nabla_{1}^{2}\psi\right] - \frac{1}{k_{0}}\left(\nabla_{1}^{2}\psi\right)$$
(2.12)

$$\delta \left[ R \frac{\partial}{\partial t} \left( \nabla_1^2 \phi \right) + \frac{\partial \phi}{\partial y} \frac{\partial}{\partial x} \left( \nabla_1^2 \phi \right) - \frac{\partial \phi}{\partial x} \frac{\partial}{\partial y} \left( \nabla_1^2 \phi \right) \right] = R \nabla_1^2 \psi - \nabla_1^2 \phi$$
(2.13)

Where  $\nabla_1^2 = \left(\delta^2 \frac{\partial^2}{\partial x^2} + \frac{\partial}{\partial y^2}\right), \varepsilon = a / d, \delta = d / \lambda$  are geometric parameters and

$$R = \frac{vm}{Kd^2}$$
 and  $P = \frac{KN_0 d^2}{\rho v}$  are non-dimensional parameters.

And  $k_0 = \frac{k}{d^2}$  is the coefficient of permeability of porous medium.

The boundary conditions in non-dimensional form now become

$$\frac{\partial \psi}{\partial y} = \frac{\partial \phi}{\partial y} = 0 \qquad \text{at} \quad y = \pm \eta = \pm \left(1 + \varepsilon \sin 2\pi (x - t)\right) \tag{2.14}$$

$$\nabla_{1}^{2} \frac{\partial \psi}{\partial y} - \delta \left[ \frac{\partial}{\partial t} \frac{\partial \psi}{\partial y} + \frac{\partial \psi}{\partial y} \frac{\partial}{\partial x} \frac{\partial \psi}{\partial y} - \frac{\partial \psi}{\partial x} \frac{\partial}{\partial y} \frac{\partial \psi}{\partial y} \right] + P \left( \frac{1}{R} \frac{\partial \phi}{\partial y} - \frac{\partial \psi}{\partial y} \right) - \frac{1}{k_{0}} \frac{\partial \psi}{\partial y} = \left( E_{1} \frac{\partial^{3}}{\partial x^{3}} + E_{2} \frac{\partial^{3}}{\partial x \partial t^{2}} + E_{3} \frac{\partial^{2}}{\partial x \partial t} \right) \eta$$
  
at  $y = \pm \eta = \pm \left( 1 + \varepsilon \sin 2\pi (x - t) \right)$  (2.15)

Where  $E_1 = \frac{Td^4}{v\rho}$ , membrane tension parameter,  $E_2 = \frac{m'd^2}{\lambda^3\rho}$ , mass characterizing parameter and  $E_3 = \frac{cd^3}{\lambda^2 v\rho}$ , the damping parameter.

#### **3. METHOD OF SOLUTION:**

Assuming  $\delta$  is very small, the stream functions  $\psi$  and  $\phi$  may be expanded in power series of  $\delta$  as

$$\psi = \psi_0 + \delta \psi_1 + \delta^2 \psi_2 + \dots$$

$$\phi = \phi_0 + \delta \phi_1 + \delta^2 \phi_2 + \dots$$
(3.1)

Substituting Eq. (3.1) in Equations (2.12) - (2.15) and collecting the coefficients of various powers of  $\delta$  on both sides, we obtain the following sets of coupled linear differential equations for  $\psi_0, \phi_0$  and  $\psi_1, \phi_1$ :

Zeroth order in  $\delta$  :

$$\frac{\partial^4 \psi_0}{\partial y^4} + P\left(\frac{1}{R}\frac{\partial^2 \phi_0}{\partial y^2} - \frac{\partial^2 \psi_0}{\partial y^2}\right) - \frac{1}{k_0}\frac{\partial^2 \psi_0}{\partial y^2} = 0$$
(3.2)

$$R\frac{\partial^2 \phi_0}{\partial y^2} - \frac{\partial^2 \psi_0}{\partial y^2} = 0$$
(3.3)

And the corresponding boundary conditions at  $y = \pm \eta$  are

$$\frac{\partial \phi_0}{\partial y} = \frac{\partial \psi_0}{\partial y} = 0 \tag{3.4}$$

$$\frac{\partial^3 \psi_0}{\partial y^3} + P\left(\frac{1}{R}\frac{\partial \phi_0}{\partial y} - \frac{\partial \psi_0}{\partial y}\right) - \frac{1}{k_0}\frac{\partial \psi_0}{\partial y} = \left(E_1\frac{\partial^3}{\partial x^3} + E_2\frac{\partial^3}{\partial x\partial t^2} + E_3\frac{\partial^2}{\partial x\partial t}\right)\eta$$
(3.5)

First order in  $\delta$  :

$$\frac{\partial^4 \psi_1}{\partial y^4} + P\left(\frac{1}{R}\frac{\partial^2 \phi_1}{\partial y^2} - \frac{\partial^2 \psi_1}{\partial y^2}\right) - \frac{1}{k_0}\frac{\partial^2 \psi_1}{\partial y^2} = \frac{\partial^3 \psi_0}{\partial t \partial y^2} + \frac{\partial \psi_0}{\partial y}\frac{\partial^3 \psi_0}{\partial x \partial y^2} - \frac{\partial \psi_0}{\partial x}\frac{\partial^3 \psi_0}{\partial y^3}$$
(3.6)

$$R\frac{\partial^2 \psi_1}{\partial y^2} - \frac{\partial^2 \phi_1}{\partial y^2} = R\frac{\partial^3 \phi_0}{\partial t \partial y^2} + \frac{\partial \phi_0}{\partial y}\frac{\partial^3 \phi_0}{\partial x \partial y^2} - \frac{\partial \phi_0}{\partial x}\frac{\partial^3 \phi_0}{\partial y^3}$$
(3.7)

and the corresponding boundary conditions at  $y = \pm \eta$  are

$$\frac{\partial \phi_1}{\partial y} = \frac{\partial \psi_1}{\partial y} = 0 \tag{3.8}$$

$$\frac{\partial^3 \psi_1}{\partial y^3} + P\left(\frac{1}{R}\frac{\partial \phi_1}{\partial y} - \frac{\partial \psi_1}{\partial y}\right) - \frac{1}{k_0}\frac{\partial \psi_1}{\partial y} = \frac{\partial^2 \psi_0}{\partial t \partial y} + \frac{\partial \psi_0}{\partial y}\frac{\partial^2 \psi_0}{\partial x \partial y} - \frac{\partial \psi_0}{\partial x}\frac{\partial^2 \psi_0}{\partial y^2}$$
(3.9)

$$\Psi_{0} = \frac{A_{1}(y^{3} - 3\eta^{2}y)}{1 - \frac{1}{2k_{0}}(y^{2} - 2\eta y)}$$
(3.10)

$$\phi_0 = \frac{A_1 R \left( y^3 - 3\eta^2 y \right)}{1 - \frac{1}{2k_0} \left( y^2 - 2\eta y \right)}$$
(3.11)

Where  $A_1 = -\frac{\varepsilon}{6} \Big[ (2\pi)^3 (E_1 + E_2) \cos 2\pi (x - t) - E_3 (2\pi)^2 \sin 2\pi (x - t) \Big]$ 

Similarly, the solutions of Eq. (3.6) and (3.7) subject to the boundary conditions (3.8) and (3.9) are

$$\psi_{1} = \left[\frac{B_{1}y^{7}}{840} + \frac{B_{2}y^{5}}{120} + \frac{B_{3}y^{3}}{6} + B_{4}y\right] / 1 - \frac{1}{2k_{0}} \left(y^{2} - 2\eta y\right)$$
(3.12)

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$$\phi_{1} = \frac{R\left(\frac{B_{1}y^{7}}{840} + \frac{B_{2}y^{5}}{120} + \frac{B_{3}y^{3}}{6} + B_{4}y\right)}{\left(1 - \frac{1}{2k_{0}}\left(y^{2} - 2\eta y\right)\right)^{2}} - \frac{6R^{2}\left(\frac{D_{1}y^{5}}{20} + \frac{D_{2}y^{3}}{6} + D_{3}y\right)}{\left(1 - \frac{1}{2k_{0}}\left(y^{2} - 2\eta y\right)\right)}$$
(3.13)

Where

$$B_{1} = 12(1+S)A_{1}(\partial A_{1}/\partial x)$$

$$B_{2} = 6(1+S)\left[6A_{1}^{2}\eta(\partial \eta/\partial x) + (\partial A_{1}/\partial t)\right]$$

$$B_{3} = 12A_{1}(\partial A_{1}/\partial x)\eta^{4} + 36A_{1}^{2}\eta^{3}(\partial \eta/\partial x) - 6A_{1}\eta(\partial \eta/\partial t) - \frac{B_{1}}{4}\eta^{4} - \frac{B_{2}}{2}\eta^{2}$$

$$B_{4} = -\left(\frac{B_{1}}{120}\eta^{6} + \frac{B_{2}}{24}\eta^{4} + \frac{B_{3}}{2}\eta^{2}\right)$$

$$D_{1} = B_{1}/\left[6(1+S)\right]$$

$$D_{2} = B_{2}/\left[6(1+S)\right]$$

$$D_{1} = 6R^{2}\left(\frac{D_{1}}{4}\eta^{4} + \frac{D_{2}}{2}\eta^{2}\right)$$

$$S = \frac{N_0 m}{\rho}$$
, mass concentration of dust particles.

Average axial velocities of the fluid particle ( $\overline{u}$ ) and the solid particle ( $\overline{u}_s$ ) (up to first order) over one period of motion are given by

$$\overline{u} = \int_{0}^{1} u dt \tag{3.14}$$

$$\overline{u}_s = \int_0^1 u_s dt \tag{3.15}$$

Where

$$u = \frac{3A_{1}(y^{2} - \eta^{2})X + M^{2}(y - \eta)A_{1}(y^{3} - 3\eta^{2}y)}{X^{2}} + \frac{\delta\left\{X^{2}\left[\frac{B_{1}y^{6}}{120} + \frac{B_{2}y^{4}}{24} + \frac{B_{3}y^{2}}{2} + B_{4}\right] + 2M^{2}(y - \eta)X\left[\frac{B_{1}y^{7}}{840} + \frac{B_{2}y^{5}}{120} + \frac{B_{3}y^{3}}{6} + B_{4}y\right]\right\}}{X^{4}}$$

$$(3.16)$$

$$u_{s} = \frac{3RA_{1}(y^{2} - \eta^{2})X + M^{2}(y - \eta)A_{1}R(y^{3} - 3\eta^{2}y)}{X^{2}} + \frac{\delta\left\{RX^{2}\left[\frac{B_{1}y^{6}}{120} + \frac{B_{2}y^{4}}{24} + \frac{B_{3}y^{2}}{2} + B_{4}\right] + 2M^{2}R(y - \eta)X\left[\frac{B_{1}y^{7}}{840} + \frac{B_{2}y^{5}}{120} + \frac{B_{3}y^{3}}{6} + B_{4}y\right]\right\}}{X^{4}} + \frac{6R^{2}\delta\left\{X\left(\frac{D_{1}y^{4}}{4} + \frac{D_{2}y^{2}}{2} + D_{3}\right) + M^{2}\left(\frac{D_{1}y^{5}}{20} + \frac{D_{2}y^{3}}{6} + D_{3}y\right)\right\}}{X^{2}}$$

$$(3.17)$$

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Where 
$$X = \left(1 - \frac{1}{2k_0} \left(y^2 - 2\eta y\right)\right)$$

The fluid flow rate (Q) defined by

$$Q = \int_{0}^{\eta} u dy \tag{3.18}$$

can be obtained using Eq. (3.16) as

$$Q = \frac{-2A_{1}\eta^{3}}{\left(1 + \frac{1}{2k_{0}}\eta^{2}\right)} + \frac{\delta\left[\frac{B_{1}\eta^{7}}{840} + \frac{B_{2}\eta^{5}}{120} + \frac{B_{3}\eta^{3}}{6} + B_{4}\eta\right]}{\left(1 + \frac{1}{2k_{0}}\eta^{2}\right)^{2}}$$
(3.19)

The time average flow rate over a period defined by

$$\overline{Q} = \int_{0}^{1} Q dt \tag{3.20}$$

can be obtained using Eq. (3.19).

# 4. RESULT AND DISCUSSION:

To explicitly see the effects of various parameters on these flow variables, these quantities were numerically evaluated and the results are graphically presented through the figures 2-8. The rigid nature of the wall is represented by the parameter  $E_1$ , which depends on the wall tension and  $E_2$  represents the stiffness property of the wall. The parameter  $E_3$  represents the dissipative feature of the wall. The choice  $E_3 = 0$  implies that the wall moves up and down, with no damping force on it and, therefore, indicates the case of elastic walls.

The effect of the rigid nature of the walls on the streamline patterns for the elastic walls ( $E_3 = 0$ ) is shown in the Figure 2a and 2b. It can be seen from the figure that the streamline got closer as the tension parameter ( $E_1$ ) increased and the phenomenon of trapping was observed. It is significant to note that the trapping phenomenon became predominant and the area of the trapped bolus increased as the tension parameter increased. The effect of the dissipative feature of the walls on the streamline is given in Figure 2c and 2d. Figure 2c and 2d shows that, as the dissipative feature of the wall increased, change in the character of the streamlines for fixed values of  $E_1$  was not significant. Though trapping was observed and was predominant, it can be seen that as damping increased the area of the trapped bolus in some regions decreased.

Figure 3 shows the effect of the mass characterizing parameter  $E_2$  on the streamline pattern for elastic and dissipative feature of the walls. As the mass concentration parameter  $E_2$  increases, the streamlines get closer and the area of the trapped bolus increases, both for elastic (Figure 3a and 3b) and dissipative feature of the walls (Figure 3c and 3d). The effect of the mass characterizing parameter (S) on the streamline pattern is shown in Figure 4; change in the character of the streamlines with the variation in the mass concentration of dust particles (S) was not significant. Though trapping was observed and was predominant for all values of S, it can be seen that as the mass concentration of dust particles increased, the area of the trapped bolus in some regions decreased. The influence of  $k_0$  on the trapping is analyzed in Figure 5; it reveals that the volume of the trapped bolus increases with increasing permeability and more trapped bolus appears with increasing  $k_0$ .

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Figure- 2: Effect of  $E_1$  and  $E_3$  on the streamline pattern of fluid particles for  $E_2$ =0.2,  $\delta$ =0.2,  $\varepsilon$ =0.4  $k_0$ =1, R=1 and S=0.5



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**Figure- 3:** Effect of  $E_2$  and  $E_3$  on the streamline pattern of fluid particles for  $E_1 = 1.0$ ,  $\delta = 0.2$ ,  $\varepsilon = 0.4$   $k_0 = 1$ , R=1 and S=0.5



Figure- 4: Effect of S on the streamline pattern of fluid particles for  $E_1 = 1.0$ ,  $E_2 = 0.75$ ,  $E_3 = 0.6$ ,  $\delta = 0.2$ ,  $\varepsilon = 0.4$ 

 $k_0 = 1$  and R=1.

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Figure- 5: Effect of  $k_0$  on the streamline pattern of fluid particles for  $E_1 = 1.0$ ,  $E_2 = 0.75$ ,  $E_3 = 0.6$ ,  $\delta = 0.2$ ,  $\varepsilon = 0.4$ , S=0.5 and R=1.

The effect of  $E_1$ ,  $E_2$ ,  $E_3$ , S and  $k_0$  on the average fluid flow rate is shown through the figures 6-10. The phenomenon of reflux, i.e. flow reversal, is observed for all values of the parameter. For higher values of  $E_1$ , the amplitude ratio at which the fluid flow rate is decreased. A similar trend was observed for the mass characterizing parameter  $E_2$ . It can be seen from Figure 8 that for lower damping values ( $E_3$ =0.2), reflux occurred. Figure 9 shows that for higher mass concentration of dust particles (S=0.8), reflux occurred for amplitude ratio up to 0.2 (approx). Figure 10 shows that for values of the permeability ( $k_0$ ) reflux occurred for all values of amplitude ratios.



Figure- 6: Effect of  $E_1$  on the flow rate of fluid particles for  $E_2$ =0.5,  $E_3$ =0.75,  $\delta$ =0.1,  $k_0$ =1, R=1 and S=0.5



Figure- 7: Effect of  $E_2$  on the flow rate of fluid particles for  $E_1$ =0.5,  $E_3$ =0.75,  $\delta$ =0.1,  $k_0$ =1, R=1 and S=0.5



Figure- 8: Effect of o  $E_3$  n the flow rate of fluid particles for  $E_1$ =0.5,  $E_2$ =0.75,  $\delta$ =0.1,  $k_0$ =1, R=1 and S=0.5



Figure- 9: Effect of S on the flow rate of fluid particles for  $E_1$ =0.5,  $E_2$ =0.75,  $E_3$ =0.75,  $\delta$ =0.1, R=1 and  $k_0$ =1.



Figure- 10 Effect of  $k_0$  on the flow rate of fluid particles for  $E_1 = 0.5$ ,  $E_2 = 0.75$ ,  $E_3 = 0.75$ ,  $\delta = 0.1$ , R=1 and S = 0.5.

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