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HOMOMORPHISM AND ANTI HOMOMORPHISM FUNCTIONS IN BIPOLAR VALUED VAGUE SUBSEMIRINGS OF A SEMIRING

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ABSTRACT

In this paper, bipolar valued vague subsemiring of a semiring is studied by homomorphism and anti homomorphism and some properties are discussed. These properties are useful to further research.

Key Words: Fuzzy subset, vague subset, bipolar valued fuzzy subset, bipolar valued vague subset, bipolar valued vague subsemiring, bipolar valued vague normal subsemiring, intersection, image and preimage.

INTRODUCTION

In 1965, Zadeh [13] introduced the notion of a fuzzy subset of a set, fuzzy sets are a kind of useful mathematical structure to represent a collection of objects whose boundary is vague. Since then it has become a vigorous area of research in different domains, there have been a number of generalizations of this fundamental concept such as intuitionistic fuzzy sets, interval valued fuzzy sets, vague sets, soft sets etc. Grattan-Guiness [7] discussed about fuzzy membership mapped onto interval and many valued quantities. Vague set is an extension of fuzzy set and it is appeared as a unique case of context dependent fuzzy sets. The vague set was introduced by W.L.Gau and D.J.Buehrer [6]. Lee [8] introduced the notion of bipolar valued fuzzy sets. Bipolar valued fuzzy sets are an extension of fuzzy sets whose membership degree range is enlarged from the interval [0, 1] to [-1, 1]. In a bipolar valued fuzzy set, the membership degree 0 means that elements are irrelevant to the corresponding property, the membership degree (0, 1] indicates that elements somewhat satisfy the property and the membership degree [-1, 0) indicates that elements somewhat satisfy the implicit counter property. Bipolar valued fuzzy sets and intuitionistic fuzzy sets look similar each other. However, they are different each other [8, 9]. Fuzzy subgroup was introduced by Azriel Rosenfeld [3]. RanjitBiswas [11] introduced the vague groups. Cicily Flora. S and Arockiarani.I [5] have introduced a new class of generalized bipolar vague sets. Anitha.M.S., et.al. [1] defined as bipolar valued fuzzy subgroups of a group and Balasubramanian.A et.al [4] have defined the bipolar interval valued fuzzy subgroups of a group. K.Murugalingam and K.Arjunan[10] have discussed about interval valued fuzzy subsemiring of a semiring and then bipolar valued multi fuzzy subsemirings of a semiring have been introduced by Yasodara.B and KE.Sathappan [12]. Anitha.K., et.al. [2] defined as bipolar valued vague subsemirings of a semiring. Here, the concept of bipolar valued vague subsemiring of a semiring is introduced and estaiblished some results. Homomorphism and anti homomorphism are applied in bipolar valued vague subsemiring of a semiring.

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1. PRELIMINARIES

Definition 1.1: [13] Let X be any nonempty set. A mapping M: $X \rightarrow [0, 1]$ is called a fuzzy subset of X.

Definition 1.2: [6] A vague set A in the universe of discourse U is a pair $[t_A, I - f_A]$, where $t_A : U \rightarrow [0, 1]$ and $f_A : U \rightarrow [0, 1]$ are mappings, they are called truth membership function and false membership function respectively. Here $t_A(x)$ is a lower bound of the grade of membership of x derived from the evidence for x and $f_A(x)$ is a lower bound on the negation of x derived from the evidence against x and $t_A(x) + t_A(x) \leq 1$, for all $t \in U$.

Definition 1.3: [6] The interval [$t_A(x)$, $I - f_A(x)$] is called the vague value of x in A and it is denoted by $V_A(x)$, i.e., $V_A(x) = [t_A(x), I - f_A(x)]$.

Example 1.4: A = $\{ < a, [0.4, 0.6] >, < b, [0.6, 0.8] >, < c, [0.3, 0.9] > \}$ is a vague subset of X = $\{ a, b, c \}$.

Definition 1.5: [8] A bipolar valued fuzzy set (BVFS) A in X is defined as an object of the form $A = \{ < x, A^+(x), A^-(x) > / x \in X \}$, where $A^+ : X \to [0, 1]$ and $A^- : X \to [-1, 0]$. The positive membership degree $A^+(x)$ denotes the satisfaction degree of an element x to the property corresponding to a bipolar valued fuzzy set A and the negative membership degree $A^-(x)$ denotes the satisfaction degree of an element x to some implicit counter-property corresponding to a bipolar valued fuzzy set A.

Example 1.6: A = $\{$ < a, 0.4, -0.2 >, < b, 0.6, -0.5 >, < c, 0.3, -0.7 > $\}$ is a bipolar valued fuzzy subset of X = $\{$ a, b, c $\}$.

Definition 1.7: [5] A bipolar valued vague subset A in X is defined as an object of the form $A = \{\langle x, [t_A^+(x), 1-f_A^+(x)], [-1-f_A^-(x), t_A^-(x)] \rangle / x \in X \}$, where $t_A^+: X \to [0, 1], f_A^+: X \to [0, 1], t_A^-: X \to [-1, 0]$ and $f_A^-: X \to [-1, 0]$ are mapping such that $t_A(x) + f_A(x) \le 1$ and $-1 \le t_A^- + f_A^-$. The positive interval membership degree $[t_A^+(x), 1-f_A^+(x)]$ denotes the satisfaction region of an element x to the property corresponding to a bipolar valued vague subset A and the negative interval membership degree $[-1-f_A^-(x), t_A^-(x)]$ denotes the satisfaction region of an element x to some implicit counter-property corresponding to a bipolar valued vague subset A is denoted as $A = \{\langle x, V_A^+(x), V_A^-(x) \rangle / x \in X \}$, where $V_A^+(x), = [t_A^+(x), 1-f_A^+(x)]$ and $V_A^-(x) = [-1-f_A^-(x), t_A^-(x)]$.

Note that. [0] = [0, 0], [1] = [1, 1]and [-1] = [-1, -1].

Example 1.8: [A] = { < a, [0.4, 0.6], [-0.5, -0.2] >, < b, [0.2, 0.4], [-0.6, -0.3] > < c, [0.1, 0.6], [-0.6, -0.2] > } is a bipolar valued vague subset of X = {a, b, c}.

Definition 1.9: [5] Let $A = \langle V_A^+, V_A^- \rangle$ and $B = \langle V_B^+, V_B^- \rangle$ be two bipolar valued vague subsets of a set X. We define the following relations and operations:

- (i) [A] \subset [B] if and only if $V_A^+(u) \leq V_B^+(u)$ and $V_A^-(u) \geq V_B^-(u)$, $\forall u \in X$.
- (ii) [A] = [B] if and only if $V_A^+(u) = V_B^+(u)$ and $V_A^-(u) = V_B^-(u)$, $\forall u \in X$.
- (iii) [A] \cap [B] = {\langle u, rmin ($V_A^+(u)$, $V_B^+(u)$), rmax ($V_A^-(u)$, $V_B^-(u)$) \rangle / u \in X}.
- $\begin{aligned} &(\text{iv}) \; [\mathbf{A}] \cup [\mathbf{B}] = \{ \langle \; \mathbf{u}, \; \text{rmax} \; (V_A^+(\mathbf{u}), \; V_B^+(\mathbf{u}) \;), \; \text{rmin} \; (V_A^-(\mathbf{u}), \; V_B^-(\mathbf{u}) \;) \; \rangle \; \; / \; \mathbf{u} \in \mathbf{X} \}. \; \text{Here rmin} \; (V_A^+(\mathbf{u}), \; V_B^+(\mathbf{u}) \;) = [\; \text{min} \; \{ \; t_A^+(x), \; t_B^+(x) \; \}, \; \text{min} \; \{ \; 1 f_A^+(x), \; 1 f_B^+(x) \; \}], \; \text{rmax} \; (V_A^+(\mathbf{u}), \; V_B^+(\mathbf{u})) = [\; \text{max} \; \{ \; t_A^+(x), \; t_B^+(x) \; \}, \; \text{max} \; \{ \; 1 f_A^+(x), \; 1 f_B^-(x) \; \}, \; \text{rmin} \; \{ \; t_A^-(x), \; t_B^-(x) \; \}], \; \text{rmax} \; (V_A^-(\mathbf{u}), \; V_B^-(\mathbf{u})) = [\; \text{max} \; \{ \; -1 f_A^-(x), \; -1 f_B^-(x) \; \}, \; \text{max} \; \{ \; t_A^-(x), \; t_B^-(x) \; \}]. \end{aligned}$

Definition 1.10: [2] Let R be a semiring. A bipolar valued vague subset A of R is said to be a bipolar valued vague subsemiring of R (BVVSSR) if the following conditions are satisfied,

- (i) $V_A^+(x+y) \ge \min\{V_A^+(x), V_A^+(y)\}$
- (ii) $V_A^+(xy) \ge \min\{V_A^+(x), V_A^+(y)\}$
- (iii) $V_A^-(x+y) \le \max\{V_A^-(x), V_A^-(y)\}$
- (iv) $V_A^-(xy) \le \operatorname{rmax} \{ V_A^-(x), V_A^-(y) \}$ for all x and y in R.

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Example 1.11: Let $R = Z_3 = \{0, 1, 2\}$ be a semiring with respect to the ordinary addition and multiplication. Then $A = \{<0, [0.5, 0.7], [-0.8, -0.5]>, <1, [0.4, 0.6], [-0.7, -0.4]>, <2, [0.4, 0.6], [-0.7, -0.4]>\}$ is a bipolar valued vague subsemiring of R.

Definition 1.12: Let R be a semiring. A bipolar valued vague subsemiring $A = \langle V_A^+, V_A^- \rangle$ of R is said to be a bipolar valued vague normal subsemiring of R if $V_A^+(x+y) = V_A^+(y+x)$, $V_A^+(xy) = V_A^+(yx)$, $V_A^-(x+y) = V_A^-(y+x)$ and $V_A^-(xy) = V_A^-(yx)$ for all x and y in R.

Definition 1.13: [3] Let R and R¹ be any two semirings. Then the function f: R \rightarrow R¹ is said to be an antihomomorphism if f(x+y) = f(y) + f(x) and f(xy) = f(y) + f(x) for all x and y in R.

Definition 1.14: Let X and X¹ be any two sets. Let $f: X \to X^1$ be any function and let $A = \langle V_A^+, V_A^- \rangle$ be a bipolar valued vague subset in X, $V = \langle V_V^+, V_V^- \rangle$ be a bipolar valued vague subset in $f(X) = X^1$, defined by $V_V^+(y) = r \inf_{x \in f^{-1}(y)} V_A^+(x)$ and $V_V^-(y) = r \inf_{x \in f^{-1}(y)} V_A^-(x)$, for all x in X and y in X¹. A is called a preimage of V under f and is defined as $V_A^+(x) = V_V^+(f(x))$, $V_A^-(x) = V_V^-(f(x))$ for all x in X and is denoted by $f^1(V)$.

2. SOME THEOREMS

Theorem 2.1: Let R and R^{†} be any two semirings. The homomorphic image of a bipolar valued vague subsemiring of R is a bipolar valued vague subsemiring of R^{†}.

Proof: Let $f: R \to R^{l}$ be a homomorphism. Let $V = f(A) = \langle V_{V}^{+}, V_{V}^{-} \rangle$, where $A = \langle V_{A}^{+}, V_{A}^{-} \rangle$ is a bipolar valued vague subsemiring of R. We have to prove that V is a bipolar valued vague subsemiring of R^{l} . Now for f(x), f(y) in R^{l} , $V_{V}^{+}(f(x)+f(y)) = V_{V}^{+}(f(x+y)) \geq V_{A}^{+}(x+y) \geq \min\{V_{A}^{+}(x), V_{A}^{+}(y)\} = \min\{V_{V}^{+}(f(x)), V_{V}^{+}(f(y))\}$ which implies that $V_{V}^{+}(f(x)+f(y)) \geq \min\{V_{V}^{+}(f(x)), V_{V}^{+}(f(y))\}$. And $V_{V}^{+}(f(x)+f(y)) \geq V_{A}^{+}(x) \geq \min\{V_{A}^{+}(x), V_{A}^{+}(y)\} = \min\{V_{V}^{+}(f(x)), V_{V}^{+}(f(x)), V_{V}^{+}(f(y))\}$ which implies that $V_{V}^{+}(f(x)+f(y)) \geq V_{A}^{-}(f(x))$, $V_{V}^{+}(f(x)+f(y)) \geq V_{A}^{-}(f(x)+f(y)) \geq V_{A}^{-}(f(x)+f(y)) \geq V_{A}^{-}(f(x))$, $V_{V}^{-}(f(x)+f(y)) \geq V_{A}^{-}(f(x))$, $V_{V}^{-}(f(x))$, $V_{V}^{-}(f(x$

2.2 Theorem: Let R and R^{\dagger} be any two semirings. The homomorphic preimage of a bipolar valued vague subsemiring of R^{\dagger} is a bipolar valued vague subsemiring of R.

Proof: Let $f: R \to R^{\top}$ be a homomorphism. Let $V = f(A) = \langle V_V^+, V_V^- \rangle$ where V is a bipolar valued vague subsemiring of R^{\top} . We have to prove that $A = \langle V_A^+, V_A^- \rangle$ is a bipolar valued vague subsemiring of R. Let X and Y in R. Now $V_A^+(X+Y) = V_V^+(f(X+Y)) = V_V^+(f(X+Y)) \geq r\min\{V_V^+(f(X)), V_V^+(f(Y))\} = r\min\{V_A^+(X), V_A^+(Y)\}$ which implies that $V_A^+(X+Y) \geq r\min\{V_A^+(X), V_A^+(Y)\}$. And $V_A^+(X+Y) \geq r\min\{V_A^+(X), V_A^+(Y)\}$ which implies that $V_A^+(X+Y) \geq r\min\{V_A^+(X), V_A^+(Y)\}$ which implies that $V_A^+(X+Y) \geq r\min\{V_A^+(X), V_A^+(Y)\}$. Also $V_A^-(X+Y) = V_V^-(f(X+Y)) = V_V^-(f(X+Y)) \leq r\max\{V_A^-(X), V_A^-(Y)\}$ which implies that $V_A^-(X+Y) \leq r\max\{V_A^-(X), V_A^-(Y)\}$ which implies that $V_A^-(X+Y) \leq r\max\{V_A^-(X), V_A^-(Y)\}$. And $V_A^-(X+Y) \leq r\max\{V_A^-(X), V_A^-(Y)\}$ which implies that $V_A^-(X+Y) \leq r\max\{V_A^-(X), V_A^-(Y)\}$ which implies that $V_A^-(X+Y) \leq r\max\{V_A^-(X), V_A^-(Y)\}$. Hence X is a bipolar valued vague subsemiring of X.

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2.3 Theorem: Let R and R^{l} be any two semirings. The antihomomorphic image of a bipolar valued vague subsemiring of R is a bipolar valued vague subsemiring of R^{l} .

Proof: Let $f: R \to R^1$ be an antihomomorphism. Let $V = f(A) = \langle V_V^+, V_V^- \rangle$ where $A = \langle V_A^+, V_A^- \rangle$ is a bipolar valued vague subsemiring of R. We have to prove that V is a bipolar valued vague subsemiring of R^1 . Now for f(x), f(y) in R^1 , $V_V^+(f(x)+f(y)) = V_V^+(f(y+x)) \geq V_A^+(y+x) \geq \min\{V_A^+(x), V_A^+(y)\} = \min\{V_V^+(f(x)), V_V^+(f(y))\}$ which implies that $V_V^+(f(x)+f(y)) \geq \min\{V_V^+(f(x)), V_V^+(f(y))\}$. And $V_V^+(f(x)f(y)) = V_V^+(f(y)) \geq V_A^+(yx) \geq \min\{V_A^+(x), V_A^+(y)\}$ and $V_V^+(f(x)) \geq V_V^+(f(x))$ which implies that $V_V^+(f(x)) \geq V_V^-(f(x))$. Also $V_V^-(f(x)+f(y)) \geq V_V^-(f(y+x)) \leq V_V^-(f(y+x)) \leq V_V^-(f(y))$. And $V_V^-(f(x)) \geq V_V^-(f(x)) \geq V_V^-(f(x))$ which implies that $V_V^-(f(x)) \geq V_V^-(f(x))$ which implies that $V_V^-(f(x)) \geq V_V^-(f(x))$. Hence V is a bipolar valued vague subsemiring of $V_V^-(f(y))$ which implies that $V_V^-(f(x)) \leq V_V^-(f(x))$.

2.4 Theorem: Let R and R¹ be any two semirings. The antihomomorphic preimage of a bipolar valued vague subsemiring of R¹ is a bipolar valued vague subsemiring of R.

Proof: Let $f: R \to R^{\top}$ be an antihomomorphism. Let $V = f(A) = \langle V_V^+, V_V^- \rangle$ where V is a bipolar valued vague subsemiring of R^{\top} . We have to prove that $A = \langle V_A^+, V_A^- \rangle$ is a bipolar valued vague subsemiring of R. Let X and Y in X in X is a bipolar valued vague subsemiring of X. Let X and Y in X is a bipolar valued vague subsemiring of X. Let X and X in X in

2.5 Theorem: Let R and R^{†} be any two semirings. The homomorphic image of a bipolar valued vague normal subsemiring of R is a bipolar valued vague normal subsemiring of R^{†}.

Proof: Let $f: R \to R^{\scriptscriptstyle \parallel}$ be a homomorphism. Let $V = f(A) = \langle V_V^+, V_V^- \rangle$ where $A = \langle V_A^+, V_A^- \rangle$ is a bipolar valued vague normal subsemiring of R. We have to prove that V is a bipolar valued vague normal subsemiring of $R^{\scriptscriptstyle \parallel}$. By Theorem 2.1, V is a bipolar valued vague subsemiring of $R^{\scriptscriptstyle \parallel}$. Now for f(x), f(y) in $R^{\scriptscriptstyle \parallel}$, V_V^+ (f(x)+f(y)) = V_V^+ (f(x+y)) $\geq V_A^+$ (x+y) = V_A^+ (y+x) $\leq V_V^+$ (f(y+x)) = V_V^+ (f(y)+f(x)) which implies that V_V^+ (f(x)+f(y)) = V_V^+ (f(y)+f(x)). And V_V^+ (f(x)+f(y)) = V_V^- (f(x)+f(y)) = V_V

2.6 Theorem: Let R and R^{\dagger} be any two semirings. The homomorphic preimage of a bipolar valued vague normal subsemiring of R^{\dagger} is a bipolar valued vague normal subsemiring of R.

Proof: Let $f: R \to R^+$ be a homomorphism. Let $V = f(A) = \langle V_V^+, V_V^- \rangle$ where V is a bipolar valued vague normal subsemiring of R^+ . We have to prove that $A = \langle V_A^+, V_A^- \rangle$ is a bipolar valued vague normal subsemiring of R. By Theorem 2.2, $A = \langle V_A^+, V_A^- \rangle$ is a bipolar valued vague subsemiring of R. Let X and Y in Y in Y is a bipolar valued vague subsemiring of Y. Let Y and Y in Y is a bipolar valued vague subsemiring of Y, which implies that Y is a bipolar valued vague Y.

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And $V_A^+(xy) = V_V^+(f(xy)) = V_V^+(f(x)f(y)) = V_V^+(f(y)f(x)) = V_V^+(f(y)f(x)) = V_A^+(yx)$ which implies that $V_A^+(xy) = V_A^+(yx)$. Also $V_A^-(x+y) = V_V^-(f(x+y)) = V_V^-(f(x)+f(y)) = V_V^-(f(y)+f(x)) = V_V^-(f(y+x)) = V_A^-(y+x)$ which implies that $V_A^-(x+y) = V_A^-(y+x)$. And $V_A^-(xy) = V_V^-(f(xy)) = V_V^-(f(x)f(y)) = V_V^-(f(y)f(x)) = V_V^-(f(y)f(x))$

2.7 Theorem: Let R and R^{†} be any two semirings. The antihomomorphic image of a bipolar valued vague normal subsemiring of R is a bipolar valued vague normal subsemiring of R^{†}.

Proof: Let $f: R \to R^{\dagger}$ be an antihomomorphism. Let $V = f(A) = \langle V_V^+, V_V^- \rangle$ where $A = \langle V_A^+, V_A^- \rangle$ is a bipolar valued vague normal subsemiring of R. We have to prove that V is a bipolar valued vague normal subsemiring of R^{\dagger} . By Theorem 2.3, V is a bipolar valued vague subsemiring of R^{\dagger} . Now for f(x), f(y) in R^{\dagger} , V_V^+ (f(x)+f(y)) = V_V^+ (f(y+x)) $\geq V_A^+$ (y+x) = V_A^+ (x+y) $\leq V_V^+$ (f(x+y)) = V_V^+ (f(y)+f(x)) which implies that V_V^+ (f(x)+f(y)) = V_V^+ (f(y)+f(x)). And V_V^+ (f(x)+f(y)) = V_V^- (f(x)+f(y)) = V_V^-

2.8 Theorem: Let R and R^{\dagger} be any two semirings. The antihomomorphic preimage of a bipolar valued vague normal subsemiring of R^{\dagger} is a bipolar valued vague normal subsemiring of R.

Proof: Let $f: R \to R^{\perp}$ be an antihomomorphism. Let $V = f(A) = \langle V_V^+, V_V^- \rangle$ where V is a bipolar valued vague normal subsemiring of R^{\perp} . We have to prove that $A = \langle V_A^+, V_A^- \rangle$ is a bipolar valued vague normal subsemiring of R. By Theorem 2.4, $A = \langle V_A^+, V_A^- \rangle$ is a bipolar valued vague subsemiring of R. Let x and y in R.

Now $V_A^+({\bf x}+{\bf y})=V_V^+({\bf f}({\bf x}+{\bf y}))=V_V^+({\bf f}({\bf y})+{\bf f}({\bf x}))=V_V^+({\bf f}({\bf x})+{\bf f}({\bf y}))=V_V^+({\bf f}({\bf y}+{\bf x}))=V_A^+({\bf y}+{\bf x})$ which implies that $V_A^+({\bf x}+{\bf y})=V_A^+({\bf y}+{\bf x})$. And $V_A^+({\bf x}{\bf y})=V_V^+({\bf f}({\bf x}{\bf y}))=V_V^+({\bf f}({\bf y})+{\bf f}({\bf y}))=V_V^+({\bf f}({\bf y}+{\bf y}))=V_V^+({\bf f}({\bf y}+{\bf y}))=V_V^+({\bf f}({\bf y}+{\bf y}))=V_V^+({\bf f}({\bf y}+{\bf y}))=V_V^-({\bf f}({\bf y}+{\bf y})$

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