

ON NEW CLASS OF AXIOMS IN TOPOLOGICAL SPACES

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ABSTRACT

In this paper, we study some separation axioms namely,  $SG-T_0$ -space,  $SG-T_1$ -space and  $SG-T_2$ -space and their properties. We also obtain some of their characterizations.

**Key Words:**  $SG-T_0$ -Space,  $SG-T_1$ -Space,  $SG-T_2$ -Space.

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1. INTRODUCTION

In the year 1987, [1] P.Bhattacharya and B.K.Lahiri introduced and studied SG-closed and SG-open sets respectively. In this paper we define and study the properties of a new topological axioms called  $SG-T_0$ -space,  $SG-T_1$ -space,  $SG-T_2$ -space.

II. PRELIMINARIES

Throughout this paper space  $(X, \tau)$  and  $(Y, \sigma)$  (or simply  $X$  and  $Y$ ) always denote topological space on which no separation axioms are assumed unless explicitly stated. For a subset  $A$  of a space  $X$ ,  $Cl(A)$ ,  $Int(A)$ ,  $A^c$ ,  $P-Cl(A)$  and  $P-int(A)$  denote the Closure of  $A$ , Interior of  $A$ , Compliment of  $A$ , pre-closure of  $A$  and pre-interior of  $(A)$  in  $X$  respectively.

**Definition 2.1:** A subset  $A$  of a topological space  $(X, \tau)$  is called

1. Semi Generalised Closed Set [1] if  $Scl(A) \subseteq U$  whenever  $A \subseteq U$  and  $U$  is Semi-open in  $X$
2. A pre generalized pre regular weakly closed set (briefly  $pgpr\omega$ -closed set) if  $pCl(A)$  [3] whenever  $A \subseteq U$  and  $U$  is  $rg\alpha$ -open in  $(X, \tau)$ .
3. A subset  $A$  of a topological space  $(X, \tau)$  is called pre generalized pre regular weakly open (briefly  $pgpr\omega$ -open) [4] set in  $X$  if  $A^c$  is  $pgpr\omega$ -closed in  $X$ .

**Definition 3:** A map  $f : (X, \tau) \rightarrow (Y, \sigma)$  is called

- (i) SG-continuous map [2] if  $f^{-1}(V)$  is SG closed in  $(X, \tau)$  for every closed  $V$  in  $(Y, \sigma)$ .
- (ii) SG-irresolute map [2] if  $f^{-1}(V)$  is SG closed in  $(X, \tau)$  for every SG-closed  $V$  in  $(Y, \sigma)$ .
- (iii) SG-closed map [2] if  $f^{-1}(V)$  is SG closed in  $(X, \tau)$  for every closed  $V$  in  $(Y, \sigma)$ .
- (iv) SG-open map [2] if  $f^{-1}(V)$  is SG closed in  $(X, \tau)$  for every closed  $V$  in  $(Y, \sigma)$ .

4. SEMI GENERALISED SPACE:

**Definition 4.4.1:** A topological space  $(X, \tau)$  is called  $SG-T_0$ -space if for any pair of distinct points  $x, y$  of  $(X, \tau)$  there exists an SG-open set  $G$  such that  $x \in G, y \notin G$  or  $x \notin G, y \in G$ .

**Example 4.4.2:** Let  $X = \{a, b\}$ ,  $\tau = \{\emptyset, \{b\}, X\}$ . Then  $(X, \tau)$  is  $SG-T_0$ -space, since for any pair of distinct points  $a, b$  of  $(X, \tau)$  there exists an  $SG-T_0$  open set  $\{b\}$  such that  $a \notin \{b\}, b \in \{b\}$ .

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**Remark 4.4.3:** Every SG-space is SG- $T_0$ -space.

**Theorem 4.4.4:** Every subspace of a SG- $T_0$ -space is SG- $T_0$ -space.

**Proof:** Let  $(X, \tau)$  be a SG- $T_0$ -space and  $(Y, \tau_y)$  be a subspace of  $(X, \tau)$ . Let  $Y_1$  and  $Y_2$  be two distinct points of  $(Y, \tau_y)$ . Since  $(Y, \tau_y)$  is subspace of  $(X, \tau)$ ,  $Y_1$  and  $Y_2$  are also distinct points of  $(X, \tau)$ . As  $(X, \tau)$  is SG- $T_0$ -space, there exists an SG-open set  $G$  such that  $Y_1 \in G$ ,  $Y_2 \notin G$ . Then  $Y \cap G$  is SG-open in  $(Y, \tau_y)$  containing  $Y_1$  not  $Y_2$ . Hence  $(Y, \tau_y)$  is SG- $T_0$ -space.

**Theorem 4.4.5:** Let  $f: (X, \tau) \rightarrow (Y, \mu)$  be an injection, SG-irresolute map. If  $(Y, \mu)$  is SG- $T_0$ -space, then  $(X, \tau)$  is SG- $T_0$ -space.

**Proof:** Suppose  $(Y, \mu)$  is SG- $T_0$ -space. Let  $a$  and  $b$  be two distinct points in  $(X, \tau)$ . As  $f$  is an injection  $f(a)$  and  $f(b)$  are distinct points in  $(Y, \mu)$ . Since  $(Y, \mu)$  is SG- $T_0$ -space, there exists an SG-open set  $G$  in  $(Y, \mu)$  such that  $f(a) \in G$  and  $f(b) \notin G$ . As  $f$  is SG-irresolute,  $f^{-1}(G)$  is SG-open set in  $(X, \tau)$  such that  $a \in f^{-1}(G)$  and  $b \notin f^{-1}(G)$ . Hence  $(X, \tau)$  is SG- $T_0$ -space.

**Theorem 4.4.6:** If  $(X, \tau)$  is SG- $T_0$ -space,  $T_{SG}$ -space and  $(Y, \tau_y)$  is SG-closed subspace of  $(X, \tau)$ , then  $(Y, \tau_y)$  is SG- $T_0$ -Space.

**Proof:** Let  $(X, \tau)$  be SG- $T_0$ -space,  $T_{SG}$ -space and  $(Y, \tau_y)$  is SG-closed subspace of  $(X, \tau)$ . Let  $a$  and  $b$  be two distinct points of  $Y$ . Since  $Y$  is subspace of  $(X, \tau)$ ,  $a$  and  $b$  are distinct points of  $(X, \tau)$ . As  $(X, \tau)$  is SG- $T_0$ -space, there exists an SG-open set  $G$  such that  $a \in G$  and  $b \notin G$ . Again since  $(X, \tau)$  is  $T_{SG}$ -space,  $G$  is open in  $(X, \tau)$ . Then  $Y \cap G$  is open. So  $Y \cap G$  is SG-open such that  $a \in Y \cap G$  and  $b \notin Y \cap G$ . Hence  $(Y, \tau_y)$  is SG- $T_0$ -space.

**Theorem 4.4.7:** Let  $f: (X, \tau) \rightarrow (Y, \mu)$  be bijective SG-open map from a SG- $T_0$  Space  $(X, \tau)$  onto a topological space  $(Y, \mu)$ . If  $(X, \tau)$  is  $T_{SG}$ -space, then  $(Y, \mu)$  is SG- $T_0$  Space.

**Proof:** Let  $a$  and  $b$  be two distinct points of  $(Y, \mu)$ . Since  $f$  is bijective, there exist two distinct points  $c$  and  $d$  of  $(X, \tau)$  such that  $f(c) = a$  and  $f(d) = b$ . As  $(X, \tau)$  is SG- $T_0$  Space, there exists a SG-open set  $G$  such that  $c \in G$  and  $d \notin G$ . Since  $(X, \tau)$  is  $T_{SG}$ -space,  $G$  is open in  $(X, \tau)$ . Then  $f(G)$  is SG-open in  $(Y, \mu)$ , since  $f$  is SG-open, such that  $a \in f(G)$  and  $b \notin f(G)$ . Hence  $(Y, \mu)$  is SG- $T_0$ -space.

**Definition 4.4.8:** A topological space  $(X, \tau)$  is said to be SG- $T_1$ -space if for any pair of distinct points  $a$  and  $b$  of  $(X, \tau)$  there exist SG-open sets  $G$  and  $H$  such that  $a \in G$ ,  $b \notin G$  and  $a \notin H$ ,  $b \in H$ .

**Example 4.4.9:** Let  $X = \{a, b\}$  and  $\tau = \{\emptyset, \{a\}, X\}$ . Then  $(X, \tau)$  is a topological space. Here  $a$  and  $b$  are two distinct points of  $(X, \tau)$ , then there exist SG-open sets  $\{a\}$ ,  $\{b\}$  such that  $a \in \{a\}$ ,  $b \notin \{a\}$  and  $a \notin \{b\}$ ,  $b \in \{b\}$ . Therefore  $(X, \tau)$  is SG- $T_0$  space.

**Theorem 4.4.10:** If  $(X, \tau)$  is SG- $T_1$ -space, then  $(X, \tau)$  is SG- $T_0$ -space.

**Proof:** Let  $(X, \tau)$  be a SG- $T_1$ -space. Let  $a$  and  $b$  be two distinct points of  $(X, \tau)$ . Since  $(X, \tau)$  is SG- $T_1$ -space, there exist SG-open sets  $G$  and  $H$  such that  $a \in G$ ,  $b \notin G$  and  $a \notin H$ ,  $b \in H$ . Hence we have  $a \in G$ ,  $b \notin G$ . Therefore  $(X, \tau)$  is SG- $T_0$ -space. The converse of the above theorem need not be true as seen from the following example.

**Example 4.4.11:** Let  $X = \{a, b\}$  and  $\tau = \{\emptyset, \{b\}, X\}$ . Then  $(X, \tau)$  is SG- $T_0$ -space but not SG- $T_1$ -space. For any two distinct points  $a, b$  of  $X$  and an SG-open set  $\{b\}$  such that  $a \notin \{b\}$ ,  $b \in \{b\}$  but then there is no SG-open set  $G$  with  $a \in G$ ,  $b \notin G$  for  $a \neq b$ .

**Theorem 4.4.12:** If  $f: (X, \tau) \rightarrow (Y, \tau_y)$  is a bijective SG-open map from a SG- $T_1$ -space and  $T_{SG}$ -space  $(X, \tau)$  on to a topological space  $(Y, \tau_y)$ , then  $(Y, \tau_y)$  is SG- $T_1$ -space.

**Proof:** Let  $(X, \tau)$  be a SG- $T_1$ -space and  $T_{SG}$ -space. Let  $a$  and  $b$  be two distinct points of  $(Y, \tau_y)$ . Since  $f$  is bijective there exist distinct points  $c$  and  $d$  of  $(X, \tau)$  such that  $f(c) = a$  and  $f(d) = b$ . Since  $(X, \tau)$  is SG- $T_1$ -space there exist SG-open sets  $G$  and  $H$  such that  $c \in G$ ,  $d \notin G$  and  $c \notin H$ ,  $d \in H$ . Since  $(X, \tau)$  is  $T_{SG}$ -space,  $G$  and  $H$  are open sets in  $(X, \tau)$  also  $f$  is SG-open  $f(G)$  and  $f(H)$  are SG-open sets such that  $a = f(c) \in f(G)$ ,  $b = f(d) \notin f(G)$  and  $a = f(c) \notin f(H)$ ,  $b = f(d) \in f(H)$ . Hence  $(Y, \tau_y)$  is SG- $T_1$ -space.

**Theorem 4.4.13:** If  $(X, \tau)$  is  $SG-T_1$  space and  $T_{SG}$ -space,  $Y$  is a subspace of  $(X, \tau)$ , then  $Y$  is  $SG-T_1$  space.

**Proof:** Let  $(X, \tau)$  be a  $SG-T_1$  space and  $T_{SG}$ -space. Let  $Y$  be a subspace of  $(X, \tau)$ . Let  $a$  and  $b$  be two distinct points of  $Y$ . Since  $Y \subseteq X$ ,  $a$  and  $b$  are also distinct points of  $X$ . Since  $(X, \tau)$  is  $SG-T_1$ -space, there exist  $SG$ -open sets  $G$  and  $H$  such that  $a \in G$ ,  $b \notin G$  and  $a \notin H$ ,  $b \in H$ . Again since  $(X, \tau)$  is  $T_{SG}$ -space,  $G$  and  $H$  are open sets in  $(X, \tau)$ , then  $Y \cap G$  and  $Y \cap H$  are open sets so  $SG$ -open sets of  $Y$  such that  $a \in Y \cap G$ ,  $b \notin Y \cap G$  and  $a \notin Y \cap H$ ,  $b \in Y \cap H$ . Hence  $Y$  is  $SG-T_1$  space.

**Theorem 4.4.14:** If  $(X, \tau) \rightarrow (Y, \tau_y)$  is injective  $SG$ -irresolute map from a topological space  $(X, \tau)$  into  $SG-T_1$ -space  $(Y, \tau_y)$ , then  $(X, \tau)$  is  $SG-T_1$  - space.

**Proof:** Let  $a$  and  $b$  be two distinct points of  $(X, \tau)$ . Since  $f$  is injective,  $f(a)$  and  $f(b)$  are distinct points of  $(Y, \tau_y)$ . Since  $(Y, \tau_y)$  is  $SG-T_1$  space there exist  $SG$ -open sets  $G$  and  $H$  such that  $f(a) \in G$ ,  $f(b) \notin G$  and  $f(a) \notin H$ ,  $f(b) \in H$ . Since  $f$  is  $SG$ -irresolute,  $f^{-1}(G)$  and  $f^{-1}(H)$  are  $SG$ -open sets in  $(X, \tau)$  such that  $a \in f^{-1}(G)$ ,  $b \notin f^{-1}(G)$  and  $a \notin f^{-1}(H)$ ,  $b \in f^{-1}(H)$ . Hence  $(X, \tau)$  is  $SG-T_1$ space.

**Definition 4.4.15:** A topological space  $(X, \tau)$ . is said to be  $SG-T_2$ - space (or  $T_{SG}$ -Hausdorff space) if for every pair of distinct points  $x, y$  of  $X$  there exist  $T_{SG}$ -open sets  $M$  and  $N$  such that  $x \in N$ ,  $y \in M$  and  $N \cap M = \emptyset$ .

**Example 4.4.16:** Let  $X = \{a, b\}$ ,  $\tau = \{\emptyset, \{a\}, \{b\}, X\}$ . Then  $(X, \tau)$  is topological space. Then  $(X, \tau)$  is  $SG-T_2$ -space.  $T_{SG}$ -open sets are  $\emptyset, \{a\}, \{b\}$ , and  $X$ . Let  $a$  and  $b$  be a pair of distinct points of  $X$ , then there exist  $T_{SG}$  - open sets  $\{a\}$  and  $\{b\}$  such that  $a \in \{a\}$ ,  $b \in \{b\}$  and  $\{a\} \cap \{b\} = \emptyset$ . Hence  $(X, \tau)$  is  $SG-T_2$ -space.

**Theorem 4.4.17:** Every  $SG-T_2$ - space is  $SG-T_1$ space.

**Proof:** Let  $(X, \tau)$  be a  $SG-T_2$ - space. Let  $x$  and  $y$  be two distinct points in  $X$ . Since  $(X, \tau)$  is  $SG-T_2$ - space, there exist disjoint  $T_{SG}$ -open sets  $U$  and  $V$  such that  $x \in U$ , and  $y \in V$ . This implies,  $x \in U$ ,  $y \notin U$  and  $x \in V$ ,  $y \notin V$ . Hence  $(X, \tau)$  is  $SG-T_1$ - space.

**Theorem 4.4.18:** If  $(X, \tau)$  is  $SG-T_2$ -space,  $T_{SG}$ - space and  $(Y, \tau_y)$  is subspace of  $(X, \tau)$ , then  $(Y, \tau_y)$  is also  $SG-T_2$ -space.

**Proof:** Let  $(X, \tau)$ , be a  $SG-T_2$  - space and let  $Y$  be a subset of  $X$ . Let  $x$  and  $y$  be any two distinct points in  $Y$ . Since  $Y \subseteq X$ ,  $x$  and  $y$  are also distinct points of  $X$ . Since  $(X, \tau)$  is  $SG-T_2$  - space, there exist disjoint  $T_{SG}$ -open sets  $G$  and  $H$  which are also disjoint open sets, since  $(X, \tau)$  is  $T_{SG}$  - space. So  $G \cap Y$  and  $H \cap Y$  are open sets and so  $T_{SG}$ - open sets in  $(Y, \tau_y)$ . Also  $x \in G$ ,  $x \in Y$  implies  $x \in G \cap Y$  and  $y \in H$  and  $y \in Y$  this implies  $y \in H \cap Y$ , since  $G \cap H = \emptyset$ , we have  $(Y \cap G) \cap (Y \cap H) = \emptyset$ . Thus  $G \cap Y$  and  $H \cap Y$  are disjoint  $T_{SG}$ -open sets in  $Y$  such that  $x \in G \cap Y$ ,  $y \in H \cap Y$  and  $(Y \cap G) \cap (Y \cap H) = \emptyset$ . Hence  $(Y, \tau_y)$  is  $SG-T_2$  - space.

**Theorem 4.4.19:** Let  $(X, \tau)$ , be a topological space. Then  $(X, \tau)$ , is  $SG-T_2$ - space if and only if the intersection of all  $T_{SG}$ -closed neighbourhood of each point of  $X$  is singleton.

**Proof:** Suppose  $(X, \tau)$ , is  $SG-T_2$ .space. Let  $x$  and  $y$  be any two distinct points of  $X$ . Since  $X$  is  $SG-T_2$ -space, there exist open sets  $G$  and  $H$  such that  $x \in G$ ,  $y \in H$  and  $G \cap H = \emptyset$ . Since  $G \cap H = \emptyset$ . implies  $x \in G \subseteq X - H$ . So  $X - H$  is  $T_{SG}$ -closed neighbourhood of  $x$ , which does not contain  $y$ . Thus  $y$  does not belong to the intersection of all  $T_{SG}$ -closed neighbourhood of  $x$ . Since  $y$  is arbitrary, the intersection of all  $T_{SG}$ -closed neighbourhoods of  $x$  is the singleton  $\{x\}$ .

Conversely, let  $(x)$  be the intersection of all  $T_{SG}$ -closed neighbourhoods of an arbitrary point  $x \in X$ . Let  $y$  be any point of  $X$  different from  $x$ . Since  $y$  does not belong to the intersection, there exists a  $T_{SG}$ -closed neighbourhood  $N$  of  $x$  such that  $y \notin N$ . Since  $N$  is  $T_{SG}$ -neighbourhood of  $x$ , there exists an  $T_{SG}$ -open set  $G$  such  $x \in G \subseteq X - N$ . Thus  $G$  and  $X - N$  are  $T_{SG}$ -open sets such that  $x \in G$ ,  $y \in X - N$  and  $G \cap (X - N) = \emptyset$ . Hence  $(X, \tau)$  is  $SG-T_2$ -space.

**Theorem 4.4.20:** Let  $f: (X, \tau) \rightarrow (Y, \tau_y)$  be a bijective  $SG$ -open map. If  $(X, \tau)$  is  $SG-T_2$ - space and  $T_{SG}$  space, then  $(Y, \tau_y)$  is also  $SG-T_2$ - space.

**Proof:** Let  $(X, \tau)$ , is  $SG-T_2$ - space and  $T_{SG}$ - space. Let  $y_1$  and  $y_2$  be two distinct points of  $Y$ . Since  $f$  is bijective map, there exist distinct points  $x_1$  and  $x_2$  of  $X$  such that  $f(x_1) = y_1$  and  $f(x_2) = y_2$ . Since  $(X, \tau)$  is  $SG-T_2$ - space, there exist  $SG$ -open sets  $G$  and  $H$  such that  $x_1 \in G$ ,  $x_2 \in H$  and  $G \cap H = \emptyset$ . Since  $(X, \tau)$  is  $T_{SG}$ - space,  $G$  and  $H$  are open sets, then  $f(G)$  and  $f(H)$  are  $SG$ - open sets of  $(Y, \tau_y)$ , since  $f$  is pprw-open, such that  $y_1 = f(x_1) \in f(G)$ ,  $y_2 = f(x_2) \in f(H)$  and  $f(G) \cap f(H) = \emptyset$ . Therefore we have  $f(G) \cap f(H) = f(G \cap H) = \emptyset$ . Hence  $(Y, \tau_y)$  is  $SG-T_2$ -space.

**Theorem 4.4.21:** Let  $(X, \tau)$  be a topological space and let  $(Y, \tau_y)$  be a SG- $T_2$ -space. Let  $f: (X, \tau) \rightarrow (Y, \tau_y)$  be an injective SG-irresolute map. Then  $(X, \tau)$  is SG- $T_2$ -space.

**Proof:** Let  $X_1$  and  $X_2$  be any two distinct points of  $X$ . Since  $f$  is injective,  $x_1 \neq x_2$  implies  $f(x_1) \neq f(x_2)$ . Let  $y_1 = f(x_1)$ ,  $y_2 = f(x_2)$  so that  $x_1 = f^{-1}(y_1)$ ,  $x_2 = f^{-1}(y_2)$ . Then  $y_1, y_2 \in Y$  such that  $y_1 \neq y_2$ . Since  $(Y, \tau_y)$  is SG- $T_2$ -space there exist  $T_{SG}$ -open sets  $G$  and  $H$  such that  $y_1 \in G$ ,  $y_2 \in H$  and  $G \cap H = \emptyset$ . As  $f$  is  $T_{SG}$ -irresolute  $f^{-1}(G)$  and  $f^{-1}(H)$  are  $T_{SG}$ -open sets of  $(X, \tau)$ . Now  $f^{-1}(G) \cap f^{-1}(H) = f^{-1}(G \cap H) = f^{-1}(\emptyset) = \emptyset$  and  $y_1 \in G$  implies  $f^{-1}(y_1) \in f^{-1}(G)$  implies  $X_1 \in f^{-1}(G)$ ,  $y_2 \in H$  implies  $f^{-1}(y_2) \in f^{-1}(H)$  implies  $x_2 \in f^{-1}(H)$ . Thus for every pair of distinct points  $x_1, x_2$  of  $X$  there exist disjoint  $T_{SG}$ -open sets  $f^{-1}(G)$  and  $f^{-1}(H)$  such that  $X_1 \in f^{-1}(G)$ ,  $x_2 \in f^{-1}(H)$ . Hence  $(X, \tau)$  is SG- $T_2$ -space.

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