

**ON  $*g\alpha$ -CLOSED SETS AND  $*g\alpha$ -CONTINUOUS MAPS**

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**ABSTRACT**

*The purpose of this paper is to introduce the concept of  $*g\alpha$ -closed set. Besides studying some properties, the interrelations of the set introduced with other related sets are studied with necessary counter examples. Introducing  $*g\alpha$ -continuous map, some interesting properties and characterizations are discussed.*

**Keywords:**  $\alpha$  semi-open set,  $\hat{g}\alpha$ -closed set,  $*g\alpha$ -closed set,  $*g\alpha$ -continuous map,  $*g\alpha$ -closure,  $T_{*g\alpha}$ -space.

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**1. INTRODUCTION**

$\alpha$ -open set was introduced and investigated by O. Njastad [12]. Cameron [4], Veerakumar. M. K. R. S. [17], Jafari. S, Noiri. T, Rajesh. N and Thivagar. M. L. [8] and Syed Ali Fathima and Mariasingam [14, 15, 16] introduced and investigated regular semi-open set,  $\hat{g}$ -closed set,  $*g$ -closed set,  $\#rg$ -closed set,  $\#rg$ -closure,  $\#rg$ -continuous map and  $T_{\#rg}$ -space. We introduce a new class of set called  $*g\alpha$ -closed set and study some of its properties. The concept of  $*g\alpha$ -continuous map is introduced and some basic properties are characterized.

**2. PRELIMINARIES**

Throughout this paper  $X, Y$  and  $Z$  denote the topological spaces  $(X, T), (Y, S)$  and  $(Z, R)$  respectively on which no separation axioms are assumed unless otherwise mentioned. For a subset  $A$  of a topological space  $X$ , the closure of  $A$ , interior of  $A$ , semi-closure of  $A$ , semipre-closure of  $A$ , the complement of  $A$  and  $\#rg$ -closure of  $A$  are denoted by  $cl(A), int(A), scl(A), spcl(A), X \setminus A$  and  $\#rg-cl(A)$  respectively. We recall the following definitions and results.

**Definition 2.1** A subset  $A$  of a space  $X$  is called

- (1) a semi-open set [10] if  $A \subseteq cl(int(A))$  and a semi-closed set if  $int(cl(A)) \subseteq A$ .
- (2) a regular open set [13] if  $A = int(cl(A))$  and a regular closed set if  $A = cl(int(A))$ .
- (3) a  $\pi$ -open set [18] if  $A$  is a finite union of regular open sets.
- (4) a  $\alpha$ -open set [12] if  $A \subseteq int(cl(int(A)))$  and a  $\alpha$ -closed set if  $cl(int(cl(A))) \subseteq A$ .
- (5) a regular semi-open set [4] if there is a regular open  $U$  such that  $U \subseteq A \subseteq cl(U)$ .
- (6) a semi-preopen set [1] if  $A \subseteq cl(int(cl(A)))$  and a semi-preclosed set if  $int(cl(int(A))) \subseteq A$ .

**Definition 2.2:** A subset  $A$  of a space  $X$  is called

- (1) a generalized closed set (briefly,  $g$ -closed) [9] if  $cl(A) \subseteq U$  whenever  $A \subseteq U$  and  $U$  is open in  $X$ .
- (2) a weakly generalized closed set (briefly,  $wg$ -closed) [11] if  $cl(int(A)) \subseteq U$  whenever  $A \subseteq U$  and  $U$  is open in  $X$ .
- (3) a  $\pi$ -generalized closed set (briefly,  $\pi g$ -closed) [7] if  $cl(A) \subseteq U$  whenever  $A \subseteq U$  and  $U$  is  $\pi$ -open in  $X$ .
- (4) a  $\hat{g}$ -closed set [17] if  $cl(A) \subseteq U$  whenever  $A \subseteq U$  and  $U$  is semi-open in  $X$ .
- (5) a  $*g$ -closed set [8] if  $cl(A) \subseteq U$  whenever  $A \subseteq U$  and  $U$  is  $\hat{g}$ -open in  $X$ .
- (6) a generalized semi-closed set (briefly,  $gs$ -closed) [2] if  $scl(A) \subseteq U$  whenever  $A \subseteq U$  and  $U$  is open in  $X$ .
- (7) a generalized semi pre-closed set (briefly,  $gsp$ -closed) [6] if  $spcl(A) \subseteq U$  whenever  $A \subseteq U$  and  $U$  is open in  $X$ .

**Definition 2.3 [15]:** For a subset A of a space X,  $\#rg\text{-cl}(A) = \bigcap \{F: A \subseteq F, F \text{ is } \#rg \text{ closed in } X\}$  is called the  $\#rg$ -closure of A.

**Definition 2.4:** A map  $f: (X, T) \rightarrow (Y, S)$  is called

- (1) continuous [3] if  $f^{-1}(V)$  is closed set in X for every closed subset V of Y.
- (2)  $\pi$ -continuous [7] if  $f^{-1}(V)$  is  $\pi$ -closed set in X for every closed subset V of Y.
- (3)  $\pi g$ -continuous [7] if  $f^{-1}(V)$  is  $\pi g$ -closed set in X for every closed subset V of Y.
- (4) wg-continuous [11] if  $f^{-1}(V)$  is wg-closed set in X for every closed subset V of Y.
- (5) gs-continuous [5] if  $f^{-1}(V)$  is gs-closed set in X for every closed subset V of Y.
- (6) gsp-continuous [6] if  $f^{-1}(V)$  is gsp-closed set in X for every closed subset V of Y.
- (7)  $\#rg$ -continuous [16] if  $f^{-1}(V)$  is  $\#rg$ -closed set in X for every closed subset V of Y.

**Definition 2.5:** A space X is called

- (1)  $T_{1/2}$ -space [9] if every g-closed set is closed.
- (2)  $T_{\#rg}$ -space [14] if every  $\#rg$ -closed set in it is closed.

**Definition 2.6 [15]:** Let  $(X, T)$  be a topological space and  $T_{\#rg} = \{V \subseteq X : \#rg\text{-cl}(X \setminus V) = X \setminus V\}$ .

### 3 \*g $\alpha$ -CLOSED SETS AND THEIR BASIC PROPERTIES

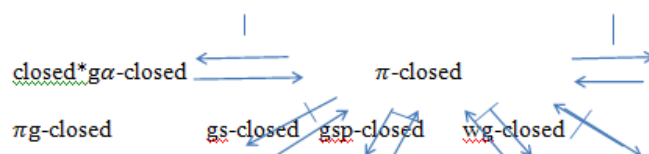
In this section we introduce and study \*g $\alpha$ -closed sets.

**Definition 3.1:** A subset A of a space X is called a  $\alpha$  semi-open set if there is a  $\alpha$ -open U such that  $U \subseteq A \subseteq \text{cl}(U)$ .

**Definition 3.2:** A subset A of a space X is called a  $\hat{g}\alpha$ -closed set if  $\text{cl}(A) \subseteq U$  whenever  $A \subseteq U$  and U is  $\alpha$  semi-open in X.

**Definition 3.3:** A subset A of a space X is called a \*g $\alpha$ -closed set if  $\text{cl}(A) \subseteq U$  whenever  $A \subseteq U$  and U is  $\hat{g}\alpha$ -open in X.

The interrelations among the set introduced and other related sets are exhibited below:



**Diagram-1**

The converse of the above interrelations need not be true as seen from the following examples.

**Example 3.1:** Let  $X = \{a, b, c, d\}$  and  $T = \{\emptyset, X, \{a\}, \{b\}, \{a, b\}, \{a, b, c\}\}$ . Then

- (i) The set  $A = \{a, d\}$  is \*g $\alpha$ -closed but not closed in X.
- (ii) The set  $A = \{a, d\}$  is \*g $\alpha$ -closed but not  $\pi$ -closed in X.
- (iii) The set  $A = \{a, c\}$  is  $\pi g$ -closed but not \*g $\alpha$ -closed in X.
- (iv) The set  $A = \{c\}$  is wg-closed but not \*g $\alpha$ -closed in X.
- (v) The set  $A = \{a\}$  is gs-closed but not \*g $\alpha$ -closed in X.
- (vi) The set  $A = \{b\}$  is gsp-closed but not \*g $\alpha$ -closed in X.

**Proposition 3.1:** The union of two \*g $\alpha$ -closed subsets of X is also a \*g $\alpha$ -closed subset of X.

**Proof:** Assume that A and B are \*g $\alpha$ -closed sets in X. Let  $A \cup B \subseteq U$  and U be  $\hat{g}\alpha$ -open in X. Then  $A \subseteq U$  and  $B \subseteq U$  and U is  $\hat{g}\alpha$ -open in X. Since A and B are \*g $\alpha$ -closed sets in X,  $\text{cl}(A) \subseteq U$  and  $\text{cl}(B) \subseteq U$ . Hence,  $\text{cl}(A \cup B) = \text{cl}(A) \cup \text{cl}(B) \subseteq U$ . Therefore,  $A \cup B$  is a \*g $\alpha$ -closed set in X.

**Proposition 3.2:** The intersection of two \*g $\alpha$ -closed subsets of X is also a \*g $\alpha$ -closed subset of X.

**Proposition 3.3:** Let A be a \*g $\alpha$ -closed set in X. Then  $\text{cl}(A) \setminus A$  does not contain any non-empty  $\hat{g}\alpha$ -closed set in X.

**Proof:** Let U be a non-empty  $\hat{g}\alpha$ -closed subset of  $\text{cl}(A) \setminus A$ . Now  $A \subseteq X \setminus U$  and  $X \setminus U$  is  $\hat{g}\alpha$ -open in X. Since A is \*g $\alpha$ -closed,  $\text{cl}(A) \subseteq X \setminus U$ . Then  $U \subseteq X \setminus \text{cl}(A)$ . This is a contradiction since by assumption,  $U \subseteq \text{cl}(A)$ .

**Proposition 3.4:** Let A be a \*g $\alpha$ -closed set in X. Then A is closed iff  $\text{cl}(A) \setminus A$  is  $\hat{g}\alpha$ -closed.

**Proposition 3.5:** For every point  $x$  of a space  $X$ ,  $X \setminus \{x\}$  is  $*g\alpha$ -closed (or)  $\hat{g}\alpha$ -open.

**Proposition 3.6:** Let  $A$  be a  $*g\alpha$ -closed subset of  $(X, T)$  such that  $A \subseteq B \subseteq \text{cl}(A)$ . Then  $B$  is also a  $*g\alpha$ -closed subset of  $(X, T)$ .

**Proof:** Let  $B \subseteq U$  and  $U$  be  $\hat{g}\alpha$ -open in  $(X, T)$ . Since  $A \subseteq B$ ,  $A \subseteq U$  and  $U$  is a  $\hat{g}\alpha$ -open set in  $(X, T)$ . Since  $A$  is  $*g\alpha$ -closed,  $\text{cl}(A) \subseteq U$ . Then  $\text{cl}(B) \subseteq \text{cl}(\text{cl}(A)) = \text{cl}(A) \subseteq U$ . Therefore,  $\text{cl}(B) \subseteq U$ . Hence,  $B$  is  $*g\alpha$ -closed.

The converse of the above Proposition need not be true as seen from the following Example.

**Example 3.2:** Let  $X = \{a, b, c, d\}$  and  $T = \{\emptyset, X, \{a\}, \{b\}, \{a, b\}, \{a, b, c\}\}$ . Let  $A = \{c, d\}$  and  $B = \{a, c, d\}$ . Then  $A$  and  $B$  are  $*g\alpha$ -closed sets in  $(X, T)$ . But  $A = \{c, d\} \subseteq B = \{a, c, d\} \not\subseteq \text{cl}(A) = \{c, d\}$ .

**Proposition 3.7:** If a subset  $A$  of a topological space  $X$  is both  $\hat{g}\alpha$ -open and  $*g\alpha$ -closed. Then  $A$  is a closed set.

**Proposition 3.8:** Let  $A$  be  $\hat{g}\alpha$ -open and  $*g\alpha$ -closed in  $X$ . Suppose that  $F$  is closed in  $X$ . Then  $A \cap F$  is a  $*g\alpha$ -closed set in  $X$ .

**Proof:** Let  $A$  be a  $\hat{g}\alpha$ -open and  $*g\alpha$ -closed set in  $X$  and let  $F$  be a closed set in  $X$ . By Proposition 3.7,  $A$  is closed and so  $A \cap F$  is closed. Since every closed set is  $*g\alpha$ -closed,  $A \cap F$  is a  $*g\alpha$ -closed set in  $X$ . Hence,  $A \cap F$  is a  $*g\alpha$ -closed set in  $X$ .

**Remark 3.1:** If a subset  $A$  of a topological space  $X$  is

- (i) open and  $g$ -closed, then  $A$  is  $*g\alpha$ -closed.
- (ii)  $\pi$ -open and  $\pi g$ -closed, then  $A$  is  $*g\alpha$ -closed.
- (iii) semi-open and  $\hat{g}$ -closed, then  $A$  is  $*g\alpha$ -closed.
- (iv)  $\alpha$ semi-open and  $\hat{g}\alpha$ -closed, then  $A$  is  $*g\alpha$ -closed.
- (v) open and  $wg$ -closed, then  $A$  is  $*g\alpha$ -closed.

**Definition 3.4:** A space  $X$  is called a  $T_{*g\alpha}$ -space if every  $*g\alpha$ -closed set in it is closed.

**Proposition 3.9:** Every  $T_{1/2}$ -space is  $T_{*g\alpha}$ -space.

#### **$4 *g\alpha$ -CONTINUOUS MAPS**

In this section we introduce and study  $*g\alpha$ -continuous maps.

**Definition 4.1:** For a subset  $A$  of a space  $X$ ,  $*g\alpha\text{-cl}(A) = \bigcap \{F : A \subseteq F, F \text{ is } *g\alpha\text{-closed in } X\}$  is called the  $*g\alpha$ -closure of  $A$ .

**Definition 4.2:** Let  $(X, T)$  be a topological space and  $T_{*g\alpha} = \{V \subseteq X : *g\alpha\text{-cl}(X \setminus V) = X \setminus V\}$ .

**Definition 4.3:** A map  $f : (X, T) \rightarrow (Y, S)$  is called  $*g\alpha$ -continuous if  $f^{-1}(V)$  is  $*g\alpha$ -closed set in  $X$  for every closed subset  $V$  of  $Y$ .

**Remark 4.1:** Let  $A$  and  $B$  be subsets of  $(X, T)$ . Then

- 1)  $*g\alpha\text{-cl}(\emptyset) = \emptyset$  and  $*g\alpha\text{-cl}(X) = X$ .
- 2) If  $A \subseteq B$ , then  $*g\alpha\text{-cl}(A) \subseteq *g\alpha\text{-cl}(B)$ .
- 3)  $A \subseteq *g\alpha\text{-cl}(A)$ .
- 4) If  $A$  is  $*g\alpha$ -closed, then  $*g\alpha\text{-cl}(A) = A$ .

**Proposition 4.1:** Suppose  $T_{*g\alpha}$  is a topology. If  $A$  is  $*g\alpha$ -closed in  $(X, T)$ , then  $A$  is closed in  $(X, T_{*g\alpha})$ .

**Proposition 4.2:** A set  $A \subseteq X$  is  $*g\alpha$ -open iff  $F \subseteq \text{int}(A)$  whenever  $F \subseteq A$  and  $F$  is  $\hat{g}\alpha$ -closed.

**Proof:** Let  $A$  be a  $*g\alpha$ -open set in  $X$ . Let  $F \subseteq A$  and  $F$  be  $\hat{g}\alpha$ -closed. Now  $X \setminus A \subseteq X \setminus F$  and  $X \setminus F$  is  $\hat{g}\alpha$ -open. Since  $X \setminus A$  is  $*g\alpha$ -closed,  $\text{cl}(X \setminus A) \subseteq X \setminus F$ . Therefore,  $X \setminus \text{int}(A) \subseteq X \setminus F$ . Hence,  $F \subseteq \text{int}(A)$ .

Suppose  $F \subseteq \text{int}(A)$  whenever  $F \subseteq A$  and  $F$  is  $\hat{g}\alpha$ -closed. Let  $X \setminus F \subseteq U$  where  $U$  is  $\hat{g}\alpha$ -open. Then  $X \setminus U \subseteq F \subseteq A$ , where  $X \setminus U$  is  $\hat{g}\alpha$ -closed. By hypothesis,  $X \setminus U \subseteq \text{int}(A)$ . This implies  $X \setminus \text{int}(A) \subseteq U$  and so  $\text{cl}(X \setminus A) \subseteq U$ , which implies  $X \setminus A$  is  $*g\alpha$ -closed. Therefore,  $A$  is  $*g\alpha$ -open.

**Proposition 4.3:** Let  $X$  be a space in which every singleton set is  $\hat{g}\alpha$ -closed. Then  $f: (X, T) \rightarrow (Y, S)$  is  $*g\alpha$ -continuous iff  $x \in \text{int}(f^{-1}(V))$  for every open subset  $V$  of  $Y$  which contains  $f(x)$ .

**Proof:** Suppose  $f: (X, T) \rightarrow (Y, S)$  is  $*g\alpha$ -continuous. Fix  $x \in X$  and an open set  $V$  in  $Y$  such that  $f(x) \in V$ . Then  $f^{-1}(V)$  is  $*g\alpha$ -open. Since  $x \in f^{-1}(V)$  and  $\{x\}$  is  $\hat{g}\alpha$ -closed,  $x \in \text{int}(f^{-1}(V))$  by Proposition 4.2.

Suppose  $x \in \text{int}(f^{-1}(V))$  for every open subset  $V$  of  $Y$  which contains  $f(x)$ . Let  $V$  be an open set in  $Y$ . Suppose  $F \subseteq f^{-1}(V)$  and  $F$  is  $\hat{g}\alpha$ -closed. Let  $x \in F$ . Then  $f(x) \in V$  so that  $x \in \text{int}(f^{-1}(V))$ . This implies  $F \subseteq \text{int}(f^{-1}(V))$ . By Proposition 4.2,  $f^{-1}(V)$  is  $*g\alpha$ -open. Hence,  $f$  is  $*g\alpha$ -continuous.

**Proposition 4.4:** Let  $f: (X, T) \rightarrow (Y, S)$  be a map. Let  $(X, T)$  and  $(Y, S)$  be any two spaces such that  $T_{*g\alpha}$  is a topology on  $X$ . Then the following statements are equivalent:

- (i) For every subset  $A$  of  $X$ ,  $f(*g\alpha\text{-cl}(A)) \subseteq \text{cl}(f(A))$ .
- (ii)  $f: (X, T_{*g\alpha}) \rightarrow (Y, S)$  is continuous.

**Proof:**

**(i)  $\Rightarrow$  (ii):** Suppose (i) holds. Let  $A$  be a closed set in  $Y$ . By (i),  $f(*g\alpha\text{-cl}(f^{-1}(A))) \subseteq \text{cl}(f(f^{-1}(A))) \subseteq \text{cl}(A) = A$  and so  $*g\alpha\text{-cl}(f^{-1}(A)) \subseteq f^{-1}(A)$ . Also  $f^{-1}(A) \subseteq *g\alpha\text{-cl}(f^{-1}(A))$ . Hence,  $*g\alpha\text{-cl}(f^{-1}(A)) = f^{-1}(A)$ . This implies  $(f^{-1}(A))^c \in T_{*g\alpha}$ . Thus,  $f^{-1}(A)$  is closed in  $(X, T_{*g\alpha})$ . Hence,  $f$  is continuous.

**(ii)  $\Rightarrow$  (i):** Suppose (ii) holds. Let  $A$  be a subset of  $X$ . Then  $\text{cl}(f(A))$  is closed in  $Y$ . Since  $f: (X, T_{*g\alpha}) \rightarrow (Y, S)$  is continuous,  $f^{-1}(\text{cl}(f(A)))$  is closed in  $(X, T_{*g\alpha})$ . By Definition 4.2,  $*g\alpha\text{-cl}(f^{-1}(\text{cl}(f(A)))) = f^{-1}(\text{cl}(f(A)))$ . Now  $A \subseteq f^{-1}(f(A)) \subseteq f^{-1}(\text{cl}(f(A)))$ , which implies  $*g\alpha\text{-cl}(A) \subseteq *g\alpha\text{-cl}(f^{-1}(\text{cl}(f(A)))) = f^{-1}(\text{cl}(f(A)))$ . Therefore,  $f(*g\alpha\text{-cl}(A)) \subseteq \text{cl}(f(A))$ .

**Proposition 4.5:** The composition of two  $*g\alpha$ -continuous maps need not be a  $*g\alpha$ -continuous map in general as seen from the following Example.

**Example 4.1:** Let  $X = Y = Z = \{a, b, c, d\}$ ,  $T = \{\emptyset, X, \{c\}, \{a, b\}, \{a, b, c\}\}$ ,  $S = \{\emptyset, Y, \{a\}, \{b\}, \{a, b\}\}$  and  $R = \{\emptyset, Z, \{a\}, \{b\}, \{a, b\}, \{a, b, c\}\}$ . Let  $f: (X, T) \rightarrow (Y, S)$  be the identity map. Then clearly,  $f$  is  $*g\alpha$ -continuous. Let  $g: (Y, S) \rightarrow (Z, R)$  be defined by  $g(a) = a$ ,  $g(b) = b$ ,  $g(c) = d$  and  $g(d) = c$ . Then clearly,  $g$  is  $*g\alpha$ -continuous. But their composition  $g \circ f: (X, T) \rightarrow (Z, R)$  is not  $*g\alpha$ -continuous, since for the closed set  $\{d\}$  in  $(Z, R)$ ,  $(g \circ f)^{-1}(\{d\}) = f^{-1}(g^{-1}\{d\}) = f^{-1}\{c\} = \{c\}$ , which is not  $*g\alpha$ -closed in  $(X, T)$ .

**Proposition 4.6:** Let  $(X, T)$ ,  $(Y, S)$  and  $(Z, R)$  be topological spaces such that  $S_{*g\alpha} = S$ . Let  $f: (X, T) \rightarrow (Y, S)$  and  $g: (Y, S) \rightarrow (Z, R)$  be  $*g\alpha$ -continuous. Then their composition  $g \circ f: (X, T) \rightarrow (Z, R)$  is also a  $*g\alpha$ -continuous.

The interrelations among the map introduced and other related maps are exhibited below:

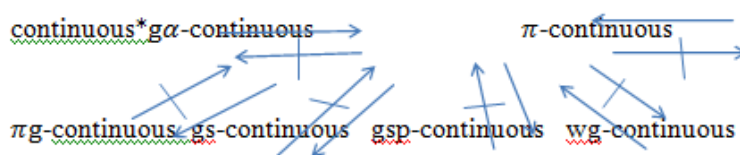


Diagram-2

**Proposition 4.7:** Let  $f: (X, T) \rightarrow (Y, S)$  be a map. Then the following are equivalent:

- (i)  $f$  is  $*g\alpha$ -continuous.
- (ii) The inverse image of each open set in  $(Y, S)$  is  $*g\alpha$ -open in  $(X, T)$ .
- (iii) The inverse image of each closed set in  $(Y, S)$  is  $*g\alpha$ -closed in  $(X, T)$ .

**Proof:**

**(i)  $\Rightarrow$  (ii):** Suppose (i) holds. Let  $V$  be open in  $Y$ . Then  $Y \setminus V$  is closed in  $Y$ . Since  $f$  is  $*g\alpha$ -continuous,  $f^{-1}(Y \setminus V)$  is  $*g\alpha$ -closed in  $X$ . But  $f^{-1}(Y \setminus V) = X \setminus f^{-1}(V)$  which is  $*g\alpha$ -closed in  $X$ . Therefore,  $f^{-1}(V)$  is  $*g\alpha$ -open in  $X$ . Hence, the inverse image of each open set in  $(Y, S)$  is  $*g\alpha$ -open in  $(X, T)$ .

**(ii)  $\Rightarrow$  (iii):** Suppose (ii) holds. Let  $V$  be a closed set in  $Y$ . Then  $Y \setminus V$  is open in  $Y$ . Since the inverse image of each open set in  $(Y, S)$  is  $*g\alpha$ -open in  $(X, T)$ ,  $f^{-1}(Y \setminus V)$  is  $*g\alpha$ -open. But  $f^{-1}(Y \setminus V) = X \setminus f^{-1}(V)$  which is  $*g\alpha$ -open. Therefore,  $f^{-1}(V)$  is  $*g\alpha$ -closed in  $X$ . Hence, the inverse image of each closed set in  $(Y, S)$  is  $*g\alpha$ -closed in  $(X, T)$ .

**(iii)  $\Rightarrow$  (i):** Suppose (iii) holds. Let  $V$  be a closed set in  $Y$ . Since, the inverse image of each closed set in  $(Y, S)$  is  $*g\alpha$ -closed in  $(X, T)$ ,  $f^{-1}(V)$  is  $*g\alpha$ -closed in  $X$ . Hence,  $f$  is  $*g\alpha$ -continuous.

**Proposition 4.8:** If a map  $f: (X, T) \rightarrow (Y, S)$  is  $*g\alpha$ -continuous, then  $f(*g\alpha\text{-cl}(A)) \subseteq \text{cl}(f(A))$  for every subset  $A$  of  $X$ .

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