

**FLEXIBLE FUZZY SOFT M- STRUCTURES
UNDER THE EXTENSIONS OF MOLODTSOV'S SOFT SETS THEORY**

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ABSTRACT

In this paper, we introduce flexible fuzzy soft M-group structures by using Molodtsov's definition of soft sets and investigate their related properties with respect to α -inclusion of soft sets.

Keywords: *Soft set, flexible fuzzy soft set, flexible soft M-group, flexible fuzzy soft M-group structure, α -inclusion, pre-image and inverse image.*

SECTION-1: INTRODUCTION

Soft set theory was introduced by Molodtsov [26] for modeling vagueness and uncertainty and it has been received much attention in the field of set theory. Maji *et.al* [23, 24] explains the applications of soft sets in decision making problems. Ali *et.al* [2] defined some new operations in soft set theory and Sezgin and Atagun [31] introduced and studied operations of soft sets. Soft set theory has also potential applications especially in decision making as in [31]. This theory has started to progress in the mean of algebraic structures, since Aktas and Cagman [3] defined and studied soft groups. Since then, soft substructures of rings, fields and modules [4], union soft substructures of near-rings and near-ring modules [32], normalistic soft groups [25] are defined and studied in detailed. The theory of G-modules originated in the 20th century. Representation theory was developed on the basis of embedding a group G in to a linear group GL(V). In 1999, Molodtsov's [26] proposed an approach for Modeling, Vagueness and uncertainty, called soft set theory, since its inception, works on soft set theory have been progressing rapidly with a wide range applications especially in the mean of algebraic structures as in [2-12]. The structures of soft sets, operations of soft sets and some related concepts have been studied by [14-19]. The theory of soft set continues to experience tremendous growth and diversification in the mean of soft decision making as in the following studies [20-23] as well. Atagun and Sezgin defined soft N-subgroups and soft N-ideals of an N-group, they studied their properties with respect to soft set operators in more detail. In this paper, we introduce flexible fuzzy soft M-Group by using Molodtsov's definition of soft sets and investigate their related properties with respect to α -inclusion of soft sets.

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SECTION-2: PRELIMINARIES

Definition 2.1: Let $(\Gamma, +)$ be a group and $\mu: M \times \Gamma \rightarrow \Gamma(m, v) \rightarrow mv$, (Γ, μ) is called an M-group if $x, y \in M$ and $\forall v \in \Gamma$,

- (i) $x(y v) = (xy) v$ and
- (ii) $(x+y) v = x v + y v$. It is denoted by N^Γ .

Clearly M itself is an M-group by natural operation. A subgroup H of Γ with $MH \subseteq H$ is said to be an M-subgroup of Γ . Let Γ and ψ be two M- groups. Then $f: \Gamma \rightarrow \psi$ is called an M-homomorphism if $\forall v, H \in \Gamma, \forall m \in M$

- (i) $f(v + H) = f(v) + f(H)$ and
- (ii) $f(mv) = mf(v)$

For all undefined concepts and notations, we refer to [27]. From now on U refers to initial universe, E is a set of parameters, 2^U is the power set of U and $A, B, C \subseteq E$

Definition 2.2: Let U be any Universal set, E set of parameters and $A \subseteq E$. Then a pair (\mathcal{G}, A) is called soft set over U , where \mathcal{G} is a mapping from A to 2^U , the power set of U .

Example 2.3: Let $X = \{c_1, c_2, c_3\}$ be the set of three cars and $E = \{\text{costly}(e_1), \text{metallic colour}(e_2), \text{cheap}(e_3)\}$ be the set of parameters, where $A = \{e_1, e_2\} \subset E$. Then $(\mathcal{G}, A) = \{\mathcal{G}(e_1) = \{c_1, c_2, c_3\}, \mathcal{G}(e_2) = \{c_1, c_2\}\}$ is the crisp soft set over X .

Definition 2.4 [Moldosov]: Let U be an initial universe. Let $P(U)$ be the power set of U , E be the set of all parameters and $A \subseteq E$. A soft set (f_A, E) on the universe U is defined by the set of order pairs $(f_A, E) = \{(e, f_A(e)): e \in E, f_A \in P(U)\}$ where $f_A: E \rightarrow P(U)$ such that $f_A(e) = \emptyset$ if $e \notin A$. Here f_A is called an approximate function of the soft set.

Example 2.5: Let $U = \{u_1, u_2, u_3, u_4\}$ be a set of four shirts and $E = \{\text{white}(e_1), \text{red}(e_2), \text{blue}(e_3)\}$ be a set of parameters. If $A = \{e_1, e_2\} \subseteq E$. Let $f_A(e_1) = \{u_1, u_2, u_3, u_4\}$ and $f_A(e_2) = \{u_1, u_2, u_3\}$. Then we write the soft set $(f_A, E) = \{(e_1, \{u_1, u_2, u_3, u_4\}), (e_2, \{u_1, u_2, u_3\})\}$ over U which describe the "colour of the shirts" which Mr. X is going to buy. We may represent the soft set in the following form:

U	e_1	e_2	e_3
u_1	1	1	0
u_2	1	1	0
u_3	1	1	0
u_4	1	0	0

Definition 2.6: Let U be the universal set, E set of parameters and $A \subset E$. Let $\mathcal{G}(X)$ denote the set of all fuzzy subsets of U . Then a pair (\mathcal{G}, A) is called fuzzy soft set over U , where \mathcal{G} is a mapping from A to $\mathcal{G}(U)$.

Example 2.7: Let $U = \{c_1, c_2, c_3\}$ be the set of three cars and $E = \{\text{costly}(e_1), \text{metallic colour}(e_2), \text{cheap}(e_3)\}$ be the set of parameters, where $A = \{e_1, e_2\} \subset E$. Then $(\mathcal{G}, A) = \{\mathcal{G}(e_1) = \{c_1/0.6, c_2/0.4, c_3/0.3\}, \mathcal{G}(e_2) = \{c_1/0.5, c_2/0.7, c_3/0.8\}\}$ is the fuzzy soft set over U denoted by F_A .

Definition 2.8: Let \mathcal{G}_A be a fuzzy soft set over U and α be a subset of U . Then upper α -inclusion of \mathcal{G}_A denoted by $\mathcal{G}_A^\alpha = \{x \in A / \mathcal{G}(x) \geq \alpha\}$.

Similarly $\mathcal{G}_A^\alpha = \{x \in A / \mathcal{G}(x) \leq \alpha\}$ is called lower α -inclusion of \mathcal{G}_A .

Definition 2.9: Let \mathcal{G}_A and G_B be fuzzy soft sets over the common universe U and $\psi: A \rightarrow B$ be a function. Then fuzzy soft image of \mathcal{G}_A under ψ over U denoted by $\psi(\mathcal{G}_A)$ is a set-valued function, where $\psi(\mathcal{G}_A): B \rightarrow 2^U$ defined by $\psi(\mathcal{G}_A)(b) = \{\cup\{\mathcal{G}(a) / a \in A \text{ and } \psi(a) = b\}, \text{ if } \psi^{-1}(b) \neq \emptyset\}$ for all $b \in B$, the soft pre-image of G_B under ψ over U denoted by $\psi^{-1}(G_B)$ is a set-valued function, where $\psi^{-1}(G_B): A \rightarrow 2^U$ defined by $\psi^{-1}(G_B)(b) = G(\psi(a))$ for all $a \in A$. Then fuzzy soft anti-image of \mathcal{G}_A under ψ over U denoted by $\psi(\mathcal{G}_A)$ is a set-valued function, where $\psi(\mathcal{G}_A): B \rightarrow 2^U$ defined by $\psi^{-1}(\mathcal{G}_A)(b) = \{\cap\{\mathcal{G}(a) / a \in A \text{ and } \psi(a) = b\}, \text{ if } \psi^{-1}(b) \neq \emptyset\}$ for all $b \in B$.

Definition 2.10[Subbiah et.al]: Let X be a set. Then a mapping $\mu: X \rightarrow M^*([0, 1])$ is called flexible subset of X , where $M^*([0, 1])$ denotes the set of all non empty subset of $[0, 1]$

Definition 2.11 [Subbiah et.al]: Let X be a non empty set .Let μ and λ be two flexible fuzzy subsets of X. Then the intersection of μ and λ denoted by $\mu \cap \lambda$ and defined by $\mu \cap \lambda = \{\min\{a, b\} / a \in \mu(x), b \in \lambda(x)\}$ for all $x \in X$. The union of μ and λ and denoted by $\mu \cup \lambda$ and defined by $\mu \cup \lambda = \{\max\{a, b\} / a \in \mu(x), b \in \lambda(x)\}$ for all $x \in X$.

Definition 2.12 [Naim Cagman]: Let U be an initial universe, E be the set of all parameters and $A \subseteq E$. A pair (F, A) is called a flexible fuzzy soft set over U where $F: A \rightarrow \tilde{P}(U)$ is a mapping from A into $\tilde{P}(U)$, where $\tilde{P}(U)$ denotes the collection of all subsets of U.

Example 2.13: Consider the example 2.5, here we cannot express with only two real numbers 0 and 1, we can characterized it by a membership function instead of crisp numbers 0 and 1, which associate with each element a real number in the interval [0,1].Then

$$(f_A, E) = \{f_A(e_1) = \{(u_1, 0.7), (u_2, 0.5), (u_3, 0.4), (u_4, 0.2)\}, \\ f_A(e_2) = \{(u_1, 0.5), (u_2, 0.1), (u_3, 0.5)\}\}$$

is the fuzzy soft set representing the “colour of the shirts” which Mr. X is going to buy.

Definition 2.14: Let H be an M-subgroup of Γ and \mathcal{G} be a flexible fuzzy soft over Γ . If for all $x, y \in H$ and $m \in M$,

- (i) $\max\{\mathcal{G}(x-y), \varphi\} \leq \min\{\mathcal{G}(x) \cup \mathcal{G}(y), \theta\}$ and
- (ii) $\max\{\mathcal{G}(mx), \varphi\} \leq \min\{\mathcal{G}(x), \theta\}$, then the flexible fuzzy soft set \mathcal{G} is called a threshold flexible fuzzy soft M-subgroup of Γ and denoted by $\mathcal{G} <_M \Gamma$

Example 2.15: Consider $M = \{0, 1, 2, 3\}$ be a group with operation +

+	0	1	2	3
0	0	1	2	3
1	1	2	3	0
2	2	3	0	1
3	3	0	1	2

If we define a flexible fuzzy soft set G over Γ by

$$G(x) = \{y \in \Gamma / 3x = y\} \text{ for all } x \in H.$$

Then $G(0) = \{0\}$ and $G(2) = \{2\}$ since $G(2-2) = G(0) \neq G(2)$, G is not a threshold flexible fuzzy soft M-subgroup of Γ .

Definition 2.16: The relative complement of the flexible fuzzy soft set \mathcal{G}_A over U is denoted by \mathcal{G}_A^r where $\mathcal{G}_A^r: A \rightarrow 2^U$ is a mapping given as $\mathcal{G}_A^r(x) = U / \mathcal{G}_A(x)$, for all $x \in A$.

SECTION-3: Characterization's of threshold flexible fuzzy soft M-group structures

In this section, we characterize the flexible fuzzy soft set through M-group structures.

Proposition 3.1: Let \mathcal{G}_A be a flexible fuzzy soft set over Γ and α be a subset of Γ . If \mathcal{G}_A is a flexible fuzzy soft M-subset of Γ , then upper α - inclusion of \mathcal{G}_A is an M-subgroup of Γ .

Proof: Since \mathcal{G}_A is flexible fuzzy soft M-subgroup of Γ . Assume $x, y \in \mathcal{G}_A^\alpha$ and $m \in M$, then $\mathcal{G}(x) \geq \alpha$ and $\mathcal{G}(y) \geq \alpha$. We need to show that $x-y \in \mathcal{G}_A^\alpha$ and $m \in \mathcal{G}_A^\alpha$. Since \mathcal{G}_A is flexible fuzzy soft M-subgroup of Γ , it follows that $\max\{\mathcal{G}(x-y), \varphi\} \leq \min\{(\mathcal{G}(x), \mathcal{G}(y)), \theta\} = \min\{(\alpha, \alpha), \theta\} \geq \alpha$ and $\max\{\mathcal{G}(mx), \varphi\} \leq \min\{\alpha, \theta\} = \alpha$ which completes the proof.

Proposition 3.2: Let \mathcal{G}_A be a flexible fuzzy soft set over Γ . Then \mathcal{G}_A is a threshold flexible fuzzy soft M-subgroup of Γ if \mathcal{G}_A^r is threshold flexible anti fuzzy soft M-subgroup of Γ .

Proof: Let \mathcal{G}_A be a threshold flexible fuzzy soft M-subgroup of Γ . Then for all $x, y \in A$ and $m \in M$.

$$\begin{aligned} \max\{\mathcal{G}_A^r(x-y), \varphi\} &= \Gamma / \max\{\mathcal{G}_A(x-y), \varphi\} \\ &\geq \Gamma / \min\{\mathcal{G}_A(x), \mathcal{G}_A(y), \theta\} \\ &= \min\{\Gamma / \mathcal{G}_A(x), \Gamma / \mathcal{G}_A(y), \theta\} \\ &= \min\{\mathcal{G}_A^r(x), \mathcal{G}_A^r(y), \theta\} \end{aligned}$$

$$\begin{aligned} \max\{\mathcal{G}_A^r(mx), \varphi\} &= \Gamma / \max\{\mathcal{G}_A(mx), \varphi\} \\ &\geq \Gamma / \min\{\mathcal{G}_A(x), \theta\} \end{aligned}$$

$$\max\{\mathcal{G}_A^r(mx), \varphi\} = \min\{\mathcal{G}_A^r(x), \theta\}.$$

Hence \mathcal{G}_A^r is threshold flexible anti fuzzy soft M-subgroup of Γ .

Proposition 3.3: Let $\mathcal{G}_A: X \rightarrow X^1$ be a soft homomorphism of M-subgroups. If \mathcal{G}_A is threshold flexible fuzzy soft M-subgroup of X, then \mathcal{G}_A is threshold flexible fuzzy soft M-subgroup of X^1 .

Proof: Suppose \mathcal{G}_A is threshold flexible fuzzy soft M-subgroup of X^1 , then

- (i) Let $x^1, y^1 \in X^1$, then exists $x, y \in X$ such that
 $f(x) = x^1$ and $f(y) = y^1$, we have
 $\max\{\mathcal{G}_A(x^1 - y^1), \varphi\} = \min\{\mathcal{G}_A(f(x) - f(y)), \theta\}$
 $\leq \min\{\mathcal{G}_A(f(x)), \mathcal{G}_A(f(y)), \theta\}$
 $\max\{\mathcal{G}_A(x^1 - y^1), \varphi\} = \min\{\mathcal{G}_A^1(x), \mathcal{G}_A^1(y), \theta\}$
- (ii) $\max\{\mathcal{G}_A(mx^1), \varphi\} = \min\{\mathcal{G}_A(mf(x)), \theta\} \leq \min\{\mathcal{G}_A^f(x), \theta\}$
 $\max\{\mathcal{G}_A(mx^1), \varphi\} = \min\{\mathcal{G}_A^f(x), \theta\}$.
 $\therefore \mathcal{G}_A$ is threshold flexible fuzzy soft M-subgroup X^1 .

Proposition 3.4: Let \mathcal{G}_A be threshold flexible soft M-sub group of X and \mathcal{G}_A^α be a flexible fuzzy soft set in X given by $\mathcal{G}_A^\alpha(x) = \mathcal{G}_A(x) + 1 - \mathcal{G}_A(1)$ for all $x \in X$. Then \mathcal{G}_A^α is threshold flexible fuzzy soft M-subgroup of X and $\mathcal{G}_A \subseteq \mathcal{G}_A^\alpha$.

Proof: Since \mathcal{G}_A is threshold flexible fuzzy soft M-subgroup of X and $\mathcal{G}_A^\alpha(x) = \mathcal{G}_A(x) + 1 - \mathcal{G}_A(1)$ for $x \in X$. For any $x, y \in X$, we have $\mathcal{G}_A(1) = \mathcal{G}_A(1) + 1 - \mathcal{G}_A(1) = 1 > \mathcal{G}_A^\alpha(x)$ and for all $x, y \in X$, we have

$$\begin{aligned} \max\{\mathcal{G}_A^\alpha(x - y), \varphi\} &= \max\{\mathcal{G}_A(x - y) + 1 - \mathcal{G}_A(1), \varphi\} \\ &\leq \min\{(\mathcal{G}_A(x), \mathcal{G}_A(y)) + 1 - \mathcal{G}_A(1), \theta\} \\ &= \min\{\mathcal{G}_A(x) + 1 - \mathcal{G}_A(1), \mathcal{G}_A(y) + 1 - \mathcal{G}_A(1), \theta\} \\ &= \min\{\mathcal{G}_A^\alpha(x), \mathcal{G}_A^\alpha(y), \theta\} \end{aligned}$$

$$\begin{aligned} \max\{\mathcal{G}_A^\alpha(mx), \varphi\} &= \max\{\mathcal{G}_A(mx) + 1 - \mathcal{G}_A(1), \varphi\} \\ &= \min\{\mathcal{G}_A(x) + 1 - \mathcal{G}_A(1), \theta\} \\ &= \min\{\mathcal{G}_A^\alpha(x), \theta\} \end{aligned}$$

Hence \mathcal{G}_A^α is threshold flexible fuzzy soft M-subgroup of X and $\mathcal{G}_A \subseteq \mathcal{G}_A^\alpha$.

Proposition 3.5: Let \mathcal{G}_A and \mathcal{G}_B two flexible fuzzy soft sets over Γ , where A and B are M- groups of Γ and $\varphi: A \rightarrow B$ is an M-homomorphism. If \mathcal{G}_A is threshold flexible fuzzy soft M- subgroup of Γ , then so is $\varphi(\mathcal{G}_A)$.

Proof: Let $\alpha_1, \alpha_2 \in B$ such φ is surjective, there exists $a_1, a_2 \in A$ such that $\varphi(a_1) = \alpha_1$ and $\varphi(a_2) = \alpha_2$. Thus

$$\begin{aligned} \max\{\varphi(\mathcal{G}_A)(\alpha_1 - \alpha_2), \varphi\} &= \max\{\mathcal{G}(a)/A \in A, \varphi(A) = \alpha_1 - \alpha_2, \varphi\} \\ &= \max\{\mathcal{G}(a)/A \in A, A = \varphi^{-1}(\alpha_1 - \alpha_2), \varphi\} \\ &= \max\{\mathcal{G}(a)/A \in A, A = \varphi^{-1}(\varphi(a_1 - a_2)) = A_1 - A_2, \varphi\} \\ &= \max\{\mathcal{G}(a_1 - a_2)/\alpha_1, \alpha_2 \in B, \varphi(a_i) = \alpha_i, i = 1, 2, \varphi\} \\ &= \min\{\max\{\mathcal{G}(a_1)/\alpha_1 \in B, \varphi(a_1) = \alpha_1, \theta\}, \max\{\mathcal{G}(a_2)/\alpha_2 \in B, \varphi(a_2) = \alpha_2, \theta\}\} \\ &= \min\{\varphi(\mathcal{G}_A)(\alpha_1), \varphi(\mathcal{G}_A)(\alpha_2), \theta\} \end{aligned}$$

Now let $m \in M$ and $\alpha \in B$. Since φ surjective, then exists $\bar{A} \in A$ such that $\varphi(\bar{A}) = \alpha$. We have

$$\begin{aligned} \max\{\varphi(\mathcal{G}_A)(m\alpha), \varphi\} &= \max\{\mathcal{G}(A)/A \in A, \varphi(A) = m\alpha, \varphi\} \\ &= \max\{\mathcal{G}(A)/A \in A, A = \varphi^{-1}(m\alpha), \varphi\} \\ &= \max\{\mathcal{G}(A)/A \in A, A = \varphi^{-1}(m\varphi(\bar{A})), \varphi\} \\ &= \max\{\mathcal{G}(A)/A \in A, A = \varphi^{-1}(\varphi(m\bar{A})) = m\bar{A}, \varphi\} \\ &= \max\{\mathcal{G}(m\bar{A})/\bar{A} \in A, \varphi(\bar{A}) = \alpha, \varphi\} \\ &= \min\{\mathcal{G}(\bar{A})/\bar{A} \in A, \varphi(\bar{A}) = \alpha, \theta\} \\ &= \min\{\varphi(\mathcal{G}_A)(\alpha), \theta\}. \text{ Hence} \end{aligned}$$

Hence $\varphi(\mathcal{G}_A)$ is threshold flexible fuzzy soft M-subgroup of Γ .

Proposition 3.6: Let $\mathcal{G}_A: X \rightarrow Y$ be a soft homomorphism of M-subgroups. If \mathcal{G}_A is threshold flexible fuzzy soft M-subgroup of Y, then \mathcal{G}_A^f is threshold flexible fuzzy soft M-subgroup of X.

Proof: Suppose \mathcal{G}_A is threshold flexible fuzzy soft M-subgroup of Y, then

- i) For all $x, y \in X$, we have
 $\max\{\mathcal{G}_A(x - y), \varphi\} = \max\{\mathcal{G}_A(f(x) - f(y)), \varphi\}$
 $= \max\{\mathcal{G}_A(f(x) - f(y)), \varphi\}$
 $= \min\{\mathcal{G}_A(f(x)), \mathcal{G}_A(f(y)), \theta\}$
 $= \min\{\mathcal{G}_A^f(x), \mathcal{G}_A^f(y), \theta\}$

$$\begin{aligned} \text{ii) } \max \{ \mathcal{G}_A^f(mx), \varphi \} &= \max \{ \mathcal{G}_A(f(mx)), \varphi \} \leq \min \{ \mathcal{G}_A(f(x)), \theta \} \\ &= \min \{ \mathcal{G}_A^f(x), \theta \}. \end{aligned}$$

Therefore \mathcal{G}_A^f is threshold flexible fuzzy soft M- subgroup of X.

Proposition 3.7: Let \mathcal{G}_A and \mathcal{G}_B be flexible fuzzy soft sets over Γ , where A and B are M-subgroups of Γ . Let \mathcal{O} be on M-homomorphism from A to B. If \mathcal{G}_B is a threshold flexible fuzzy soft M-subgroup of Γ , then so is $\mathcal{O}^{-1}(\mathcal{G}_B)$.

Proof: Let $a_1, a_2 \in A$. Then

$$\begin{aligned} \max \{ (\mathcal{O}^{-1}(\mathcal{G}_B))(a_1-a_2), \varphi \} &= \max \{ \mathcal{G}(\mathcal{O}(a_1-a_2)), \varphi \} \\ &\geq \min \{ \mathcal{G}(\mathcal{O}(a_1)), \mathcal{G}(\mathcal{O}(a_2)), \theta \} \\ &= \min \{ (\mathcal{O}^{-1}(\mathcal{G}_B))(a_1), (\mathcal{O}^{-1}(\mathcal{G}_B))(a_2), \theta \} \end{aligned}$$

Now let $m \in M$ and $A \in A$, then

$$\begin{aligned} \max \{ (\mathcal{O}^{-1}(\mathcal{G}_B))(m_A), \varphi \} &= \max \{ \mathcal{G}(\mathcal{O}(m_A)), \varphi \} \\ &= \min \{ \mathcal{G}(m\mathcal{O}(A)), \theta \} \\ &= \min \{ \mathcal{G}(\mathcal{O}(A)), \theta \} \\ &= \min \{ (\mathcal{O}^{-1}(\mathcal{G}_B))(A), \theta \}. \end{aligned}$$

Hence $\mathcal{O}^{-1}(\mathcal{G}_B)$ is a flexible fuzzy soft M-subgroup of Γ .

CONCLUSION

This paper summarized the basic concepts of flexible soft sets. By using these concepts we studied the algebraic properties of flexible fuzzy soft M-groups. This work focused on flexible fuzzy soft pre-image, flexible fuzzy soft image, flexible fuzzy soft anti image. To extend this work one could study the properties of flexible fuzzy soft M-groups in other algebraic structures such as rough set and vague set.

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