

## ZERO-CONSTANT REVERSE MAGIC GRAPHOIDAL GRAPHS

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### ABSTRACT

In this paper we formulated a new definition called 0-constant Reverse Magic Graphoidal graphs. Let  $G$  admits  $\psi$  magic graphoidal total labelling of  $G$  if there exists one-to-one map  $f: V \cup E \rightarrow \{1, 2, 3, \dots, m + n\}$  such that for every path  $P$  in  $\psi$  then  $f^*(P) = \sum_{i=1}^{n-1} f(v_i v_{i+1}) - \{f(v_1) + f(v_n)\} = \mu_{rmgc} = 0$  (Zero) is a constant, where  $f^*$  is the induced labeling on  $\psi$  is called Zero-Constant Reverse Magic Graphoidal. And also proved that Binary tree and Coconut tree are Zero-Constant Reverse Magic Graphoidal Graphs.

**Keywords:** Zero-Constant Reverse Magic Graphoidal Graphs, Graphoidal Constant, Graphoidal Cover, Magic Graphoidal, reverse- magic graphoidal.

### 1. INTRODUCTION

Let  $G = (V, E)$  be a graph with  $n$  vertices and  $m$  edges. A graphoidal cover  $\psi$  of  $G$  is a collection of paths such that  $\psi$

- (i) Every edge is exactly one path of
- (ii) Every vertex is an internal vertex of almost one path in  $\psi$ .

In 1963, motivated by the notation of magic squares in number theory, **Magic labeling** were introduced by Sedlacek [10]. B.D. Acharya and E. Sampath Kumar defined Graphoidal cover as partition of edge set of  $G$  in to internally disjoint paths (not necessarily open). The maximum cardinality of such cover is known as graphoidal covering number of  $G$ .

A graph  $G = (V, E)$  is said to be magic if there exist a bijection  $f: V \cup E \rightarrow \{1, 2, 3, \dots, m + n\}$ . Such that for every path  $P = \{v_1, v_2, \dots, v_n\}$  in  $\psi$ . A graph  $G$  is called magic graphoidal if there exists a minimum graphoidal cover  $\psi$  of  $G$  such that  $G$  admits  $\psi$ - magic graphoidal total labelling of  $G$ .

Here we introduced a new type of (ie. Zero-Reverse) magic graphoidal total labeling is called Zero-reverse magic graphoidal (rmg) total labeling.

**Definition 1.1:** The **Trivial graph**  $K_1$  or  $P_1$  is the graph with one vertex and no edges

**Definition 1.2:** A **Binary tree** is an 2-ary tree in which every internal vertex has exactly 2 children and all leaves are at the same level.

**Definition 1.3:** The **Coconut tree** graph is obtained by identifying the vertex of  $K_{1,m}$  with a pendant vertex of the path  $P_n$

**Definition 1.4:** A reverse magic graphoidal labeling of a graph  $G$  is one-to-one map  $f$  from  $V(G) \cup E(G) \rightarrow \{1, 2, 3, \dots, m + n\}$ , where ' $n$ ' is the number of vertices of a graph and ' $m$ ' is the number of the edges of a graph, with the property that , there is an integer constant ' $\mu$ ' such that

$$f^*(p) = \sum_{i=1}^{n-1} f(v_i v_{i+1}) - \{f(v_1) + f(v_n)\} = \mu_{rmgc}, \text{ is a contant}$$

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**II. MAIN RESULTS**

**Definition 2.1:** Let  $G$  admits  $\psi$  magic graphoidal total labelling of  $G$  if there exists one-to-one map  $f: V \cup E \rightarrow \{1,2,3, \dots, m + n\}$  such that for every path  $P$  in  $\psi$  then  $f^*(P) = \sum_{i=1}^{n-1} f(v_i v_{i+1}) - \{f(v_1) + f(v_n)\} = \mu_{rmgc} = 0$  (Zero) is a constant, where  $f^*$  is the induced labeling on  $\psi$  is called **Zero-Constant Reverse Magic Graphoidal**. Then the reverse methodology of Zero-constant magic graphoidal labeling is called **Zero-constant reverse magic graphoidal labeling** (Zero-crmgl). Reverse process of Zero-constant magic graphoidal of a graph is called **Zero-constant reverse magic graphoidal graphs** (Zero-crmgg).

**Theorem 2.1:** The binary tree is Zero-constant reverse magic graphoidal.

**Proof:**

Let  $G$  be the binary tree.

Let  $V(G) = u_i; 0 \leq i \leq n - 1$

And  $E(G) = \{(u_{i-1} u_{2i-1}), (u_{i-1} u_{2i})\}; 1 \leq i \leq \frac{n-1}{2}$

Here  $m + n = 2n - 1$

Define  $f: V \cup E \rightarrow \{1,2, \dots, m + n\}$  by

$$\begin{aligned} f(u_0) &= \text{no value} \\ f(u_{2i-1}) &= i; & 1 \leq i \leq \frac{n-1}{2} \\ f(u_{2i}) &= 2n - i & 1 \leq i \leq \frac{n-1}{2} \\ f(u_{i-1} u_{2i-1}) &= \frac{n-1}{2} + i; & 1 \leq i \leq \frac{n-1}{2} \\ f(u_{i-1} u_{2i}) &= \frac{3n+1}{2} - i; & 1 \leq i \leq \frac{n-1}{2} \end{aligned}$$

Let  $\psi = \{P = (u_{2i-1} u_{i-1} u_{2i})\}$

So,

$$\begin{aligned} f^*(P) &= f(u_{2i-1} u_{i-1}) + f(u_{i-1} u_{2i}) - \{f(u_{2i-1}) + f(u_{2i})\} \\ &= \frac{n-1}{2} + i + \frac{3n+1}{2} - i - \{i + 2n - i\} \\ &= \frac{n-1}{2} + \frac{3n+1}{2} - 2n \\ &= \frac{4n - 4n}{2} = 0 = \mu_{rmgc} \end{aligned} \tag{1}$$

From the above equation (1) we conclude that  $G$  admits  $\psi$  - reverse magic graphoidal total labeling. The reverse magic graphoidal constant  $\mu_{rmgc}$  of binary tree is '0'. Hence binary tree is Zero-reverse magic graphoidal.

**Theorem 16:** The Coconut tree  $K_{1,n} \odot P_n$  is Zero-constant reverse magic graphoidal.

**Proof:**

Let  $G$  be a coconut tree.

Let  $V(G) = u_i; 1 \leq i \leq 2n$

And  $E(G) = \begin{cases} u_i u_{i+1}; & i \leq n - 1 \\ u_n u_{n+i}; & 1 \leq i \leq n \end{cases}$

Here,  $m + n = 2m + 2n - 1$

Define  $f: V \cup E \rightarrow \{1,2, \dots, 2m + 2n - 1\}$  by

$$\begin{aligned} f(u_1) &= 2(m + n - 1) \\ f(u_2) &= 1 \\ f(u_1 u_2) &= 2m + 2n - 1 \end{aligned}$$

**Case (i):  $n = 0 \pmod{4}$**

$$\begin{aligned} f(u_{4i-2}) &= i; & 1 \leq i \leq \frac{n}{4} \\ f(u_{4i}) &= 2(m + n - 1) - i; & 1 \leq i \leq \frac{n}{4} \\ f(u_{4i-2} u_{4i-1}) &= \frac{8m + 7n - 8}{4} - i; & 1 \leq i \leq \frac{n}{4} \\ f(u_{4i-1} u_{4i}) &= \frac{n}{4} + i; & 1 \leq i \leq \frac{n}{4} \end{aligned}$$

$$\begin{aligned}
 f(u_{4i}u_{4i+1}) &= \frac{4m + 3n - 4}{2} - i; & 1 \leq i \leq \frac{n}{4} - 1 \\
 f(u_{4i+1}u_{4i+2}) &= \frac{n + 2}{2} + i; & 1 \leq i \leq \frac{n}{2} \\
 f(u_n u_{n+2i-1}) &= \frac{8m + 3n - 4}{4} - i; & 1 \leq i \leq \frac{n}{2} \\
 f(u_n u_{n+2i}) &= \frac{5n}{4} + i; & 1 \leq i \leq \frac{n}{2} \\
 f(u_{n+2i-1}) &= \frac{8m + 5n - 4}{4} - i; & 1 \leq i \leq \frac{n}{2} \\
 f(u_{n+2i}) &= \frac{3n}{4} + i; & 1 \leq i \leq \frac{n}{2}
 \end{aligned}$$

Let  $\psi = \{P_1 = (u_1 u_2)$

$$P_2 = (u_{4i-2} u_{4i-1}) \cup (u_{4i-1} u_{4i}); \quad 1 \leq i \leq \frac{n}{4}$$

$$P_3 = (u_{4i} u_{4i+1}) \cup (u_{4i+1} u_{4i+2}); \quad 1 \leq i \leq \frac{n}{4}$$

$$P_4 = (u_n u_{n+2i-1}) \cup (u_n u_{n+2i}); \quad 1 \leq i \leq \frac{n}{2}$$

So,

$$\begin{aligned}
 f^*(P_1) &= f(u_1 u_2) - \{f(u_1) + f(u_2)\} \\
 &= 2m + 2n - 1 - \{2(m + n - 1) + 1\} \\
 &= 0 = \mu_{rmgc} \text{ _____ (1)}
 \end{aligned}$$

$$\begin{aligned}
 f^*(P_2) &= f(u_{4i-2} u_{4i-1}) + f(u_{4i-1} u_{4i}) - \{f(u_{4i-2}) + f(u_{4i})\} \\
 &= \frac{8m + 7n - 8}{4} - i + \frac{n}{4} + i - \{i + 2(m + n - 1) - i\} \\
 &= 0 = \mu_{rmgc} \text{ _____ (2)}
 \end{aligned}$$

$$\begin{aligned}
 f^*(P_3) &= f(u_{4i} u_{4i+1}) + f(u_{4i+1} u_{4i+2}) - \{f(u_{4i}) + f(u_{4i+2})\} \\
 &= \frac{4m + 3n - 4}{2} - i + \frac{n + 2}{2} + i - \{2(m + n - 1) - i + i + 1\} \\
 &= 0 = \mu_{rmgc} \text{ _____ (3)}
 \end{aligned}$$

$$\begin{aligned}
 f^*(P_4) &= f(u_n u_{n+2i-1}) - f(u_n u_{n+2i}) - \{f(u_{n+2i-1}) + f(u_{n+2i})\} \\
 &= \frac{8m + 3n - 4}{4} - i + \frac{5n}{4} + i - \left\{ \frac{8m + 5n - 4}{4} - i + \frac{3n}{4} + i \right\} \\
 &= 0 = \mu_{rmgc} \text{ _____ (4)}
 \end{aligned}$$

From the above equation (1), (2), (3)& (4) we conclude that  $G$  admits  $\psi$  - reverse magic graphoidal total labeling. The reverse magic graphoidal constant  $\mu_{rmgc}$  of coconut tree is '0'. Hence coconut tree is Zero-reverse magic graphoidal.

**Case (ii):  $n \equiv 1 \pmod{4}$**

$$\begin{aligned}
 f(u_{4i-2}) &= i; & 1 \leq i \leq \frac{n+3}{4} \\
 f(u_{4i}) &= 2(m + n - 1) - i; & 1 \leq i \leq \frac{n-1}{4} \\
 f(u_{4i-2} u_{4i-1}) &= \frac{4m + 3n - 5}{2} - i; & 1 \leq i \leq \frac{n-1}{4} \\
 f(u_{4i-1} u_{4i}) &= \frac{n+1}{2} + i; & 1 \leq i \leq \frac{n-1}{4} \\
 f(u_{4i} u_{4i+1}) &= \frac{8m + 7n - 7}{2} - i; & 1 \leq i \leq \frac{n-1}{4} \\
 f(u_{4i+1} u_{4i+2}) &= \frac{n+3}{4} + i; & 1 \leq i \leq \frac{n-1}{4} \\
 f(u_{n+2i}) &= \frac{8m + 5n - 9}{4} - i; & 1 \leq i \leq \frac{n-1}{2} \\
 f(u_{n+2i+1}) &= \frac{3n+1}{4} + i; & 1 \leq i \leq \frac{n-1}{2} \\
 f(u_n u_{n+2i}) &= \frac{8m + 3n - 7}{4} - i; & 1 \leq i \leq \frac{n-1}{2} \\
 f(u_n u_{n+2i+1}) &= \frac{5n-1}{4} + i; & 1 \leq i \leq \frac{n-1}{2}
 \end{aligned}$$

$$\begin{aligned} \text{Let } \psi &= \{P_1 = (u_1u_2) \\ &P_2 = (u_{4i-2}u_{4i-1}) \cup (u_{4i-1}u_{4i}) \\ &P_3 = (u_{4i}u_{4i+1}) \cup (u_{4i+1}u_{4i+2}) \\ &P_4 = (u_{n+2i}u_n) \cup (u_nu_{n+2i+1})\} \end{aligned}$$

So,

$$\begin{aligned} f^*(P_1) &= f(u_1u_2) - \{f(u_1) + f(u_2)\} \\ &= 2m + 2n - 1 - \{2m + 2n - 2 + 1\} \\ &= 0 = \mu_{rmgc} \end{aligned} \tag{1}$$

$$\begin{aligned} f^*(P_2) &= f(u_{4i-2}u_{4i-1}) + f(u_{4i-1}u_{4i}) - \{f(u_{4i-2}) + f(u_{4i})\} \\ &= \frac{4m + 3n - 5}{2} - i + \frac{n + 1}{2} + i - \{i + 2(m + n - 1) - i\} \\ &= 0 = \mu_{rmgc} \end{aligned} \tag{2}$$

$$\begin{aligned} f^*(P_3) &= f(u_{4i}u_{4i+1}) + f(u_{4i+1}u_{4i+2}) - \{f(u_{4i}) + f(u_{4i+2})\} \\ &= \frac{8m + 7n - 7}{4} - i + \frac{n + 3}{4} + i - \{2(m + n - 1) - i + i + 1\} \\ &= 0 = \mu_{rmgc} \end{aligned} \tag{3}$$

$$\begin{aligned} f^*(P_4) &= f(u_{n+2i}u_n) - f(u_nu_{n+2i+1}) - \{f(u_{n+2i}) + f(u_{n+2i+1})\} \\ &= \frac{8m + 3n - 7}{4} - i + \frac{5n - 1}{4} + i - \left\{ \frac{8m + 5n - 9}{4} - i + \frac{3n + 1}{4} + i \right\} \\ &= 0 = \mu_{rmgc} \end{aligned} \tag{4}$$

From the above equation (1), (2), (3)& (4) we conclude that  $G$  admits  $\psi$  - reverse magic graphoidal total labeling. The reverse magic graphoidal constant  $\mu_{rmgc}$  of coconut tree is '0'. Hence coconut tree is Zero-reverse magic graphoidal.

**Case (iii) :  $n = 2 \pmod{4}$**

$$\begin{aligned} f(u_{4i}) &= 2(m + n - 1) - i; & 1 \leq i \leq \frac{n - 2}{4} \\ f(u_{4i-2}) &= i; & 1 \leq i \leq \frac{n + 2}{4} \\ f(u_{4i-2}u_{4i-1}) &= \frac{4m + 3n - 4}{2} - i; & 1 \leq i \leq \frac{n - 2}{4} \\ f(u_{4i-1}u_{4i}) &= \frac{n}{2} + i; & 1 \leq i \leq \frac{n - 2}{4} \\ f(u_{4i}u_{4i+1}) &= \frac{8m + 7n - 6}{4} - i; & 1 \leq i \leq \frac{n - 2}{4} \\ f(u_{4i+1}u_{4i+2}) &= \frac{n + 2}{4} + i; & 1 \leq i \leq \frac{n - 2}{4} \\ f(u_{n+2i-1}) &= \frac{8m + 5n - 6}{4} - i; & 1 \leq i \leq \frac{n}{2} \\ f(u_{n+2i}) &= \frac{3n - 2}{4} + i; & 1 \leq i \leq \frac{n}{2} \\ f(u_nu_{n+2i-1}) &= \frac{8m + 3n - 6}{4} - i; & 1 \leq i \leq \frac{n}{2} \\ f(u_nu_{n+2i}) &= \frac{5n - 2}{4} + i; & 1 \leq i \leq \frac{n}{2} \end{aligned}$$

$$\begin{aligned} \text{Let } \psi &= \{P_1 = (u_1u_2) \\ &P_2 = (u_{4i-2}u_{4i-1}) \cup (u_{4i-1}u_{4i}) \\ &P_3 = (u_{4i}u_{4i+1}) \cup (u_{4i+1}u_{4i+2}) \\ &P_4 = (u_{n+2i-1}u_n) \cup (u_nu_{n+2i})\} \end{aligned}$$

So,

$$\begin{aligned} f^*(P_1) &= f(u_1u_2) - \{f(u_1) + f(u_2)\} \\ &= 2m + 2n - 1 - \{2(m + n - 1) + 1\} \\ &= 0 = \mu_{rmgc} \end{aligned} \tag{1}$$

$$\begin{aligned} f^*(P_2) &= f(u_{4i-2}u_{4i-1}) + f(u_{4i-1}u_{4i}) - \{f(u_{4i-2}) + f(u_{4i})\} \\ &= \frac{4m + 3n - 4}{2} - i + \frac{n}{2} + i - \{i + 2(m + n - 1) - i\} \\ &= 0 = \mu_{mgc} \end{aligned} \tag{2}$$

$$\begin{aligned}
 f^*(P_3) &= f(u_{4i}u_{4i+1}) + f(u_{4i+1}u_{4i+2}) - \{f(u_{4i}) + f(u_{4i+2})\} \\
 &= \frac{8m + 7n - 6}{4} - i + \frac{n + 2}{4} + i - \{2(m + n - 1) - i + i + 1\} \\
 &= 0 = \mu_{rmgc} \text{ (3)}
 \end{aligned}$$

$$\begin{aligned}
 f^*(P_4) &= f(u_{n+2i-1}u_n) - f(u_nu_{n+2i}) - \{f(u_{n+2i-1}) + f(u_{n+2i})\} \\
 &= \frac{8m + 3n - 6}{4} - i + \frac{5n - 2}{4} + i - \left\{ \frac{8m + 5n - 6}{4} - i + \frac{3n - 2}{4} + i \right\} \\
 &= 0 = \mu_{rmgc} \text{ (4)}
 \end{aligned}$$

From the above equation (1), (2), (3)& (4) we conclude that  $G$  admits  $\psi$  - reverse magic graphoidal total labeling. The reverse magic graphoidal constant  $\mu_{rmgc}$  of coconut tree is '0'. Hence coconut tree is Zero-reverse magic graphoidal.

**Case (iv) :  $n = 3 \pmod 4$**

$$\begin{aligned}
 f(u_{4i-2}) &= i; & 1 \leq i \leq \frac{n+1}{4} \\
 f(u_{4i}) &= 2(m+n-1) - i; & 1 \leq i \leq \frac{n+1}{4} \\
 f(u_{4i-2}u_{4i-1}) &= \frac{8m+7n-9}{4} - i; & 1 \leq i \leq \frac{n+1}{4} \\
 f(u_{4i-1}u_{4i}) &= \frac{n+1}{4} + i; & 1 \leq i \leq \frac{n+1}{4} \\
 f(u_{4i}u_{4i+1}) &= \frac{4m+3n-5}{2} - i; & 1 \leq i \leq \frac{n-3}{2} \\
 f(u_{4i+1}u_{4i+2}) &= \frac{n+3}{2} + i; & 1 \leq i \leq \frac{n-3}{2} \\
 f(u_{n+2i}) &= \frac{8m+5n-7}{4} + i; & 1 \leq i \leq \frac{n-1}{2} \\
 f(u_{n+2i+1}) &= \frac{3n+3}{4} + i; & 1 \leq i \leq \frac{n-1}{2} \\
 f(u_nu_{n+2i}) &= \frac{8m+3n-5}{4} - i; & 1 \leq i \leq \frac{n-1}{2} \\
 f(u_nu_{n+2i+1}) &= \frac{5n+1}{4} + i; & 1 \leq i \leq \frac{n-1}{2}
 \end{aligned}$$

Let  $\psi = \{P_1 = (u_1u_2)$   
 $P_2 = (u_{4i-2}u_{4i-1}) \cup (u_{4i-1}u_{4i})$   
 $P_3 = (u_{4i}u_{4i+1}) \cup (u_{4i+1}u_{4i+2})$   
 $P_4 = (u_{n+2i}u_n) \cup (u_nu_{n+2i+1}) \}$

So,

$$\begin{aligned}
 f^*(P_1) &= f(u_1u_2) - \{f(u_1) + f(u_2)\} \\
 &= 2m + 2n - 1 - \{2(m + n - 1) + 1\} \\
 &= 0 = \mu_{rmgc} \text{ (1)}
 \end{aligned}$$

$$\begin{aligned}
 f^*(P_2) &= f(u_{4i-2}u_{4i-1}) + f(u_{4i-1}u_{4i}) - \{f(u_{4i-2}) + f(u_{4i})\} \\
 &= \frac{8m + 7n - 9}{4} - i + \frac{n + 1}{4} + i - \{i + 2(m + n - 1) - i\} \\
 &= 0 = \mu_{rmgc} \text{ (2)}
 \end{aligned}$$

$$\begin{aligned}
 f^*(P_3) &= f(u_{4i}u_{4i+1}) + f(u_{4i+1}u_{4i+2}) - \{f(u_{4i}) + f(u_{4i+2})\} \\
 &= \frac{4m + 3n - 5}{2} - i + \frac{n + 3}{2} + i - \{2(m + n - 1) - i + i + 1\} \\
 &= 0 = \mu_{rmgc} \text{ (3)}
 \end{aligned}$$

$$\begin{aligned}
 f^*(P_4) &= f(u_{n+2i}u_n) + f(u_nu_{n+2i+1}) - \{f(u_{n+2i}) + f(u_{n+2i+1})\} \\
 &= \frac{8m + 3n - 5}{4} - i + \frac{5n + 1}{4} + i - \left\{ \frac{8m + 5n - 7}{4} - i + \frac{3n + 3}{4} + i \right\} \\
 &= \frac{8m + 3n - 5 + 5n + 1 - 8m - 5n + 7 - 3n - 3}{4} \\
 &= 0 = \mu_{rmgc} \text{ (4)}
 \end{aligned}$$

From the above equation (1), (2), (3) & (4) we conclude that  $G$  admits  $\psi$  - reverse magic graphoidal total labeling. The reverse magic graphoidal constant  $\mu_{rmgc}$  of coconut tree is '0'. Hence coconut tree is Zero-reverse magic graphoidal.

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