

**SUPRA SEMI NORMAL SPACES AND SOME SUPRA MAPS**

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**ABSTRACT**

*In this paper, We obtain the characterizations of supra semi normal space by using supra semi generalized-open sets (supra sg- open sets). Moreover, inorder to obtain preservation theorems of supra semi normal spaces, we introduce the concepts of supra pre sg- continuous maps and supra pre sg –closed maps and also investigate several properties of new notions*

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**1. INTRODUCTION**

In 1983, Mashhour *et al.* [6] introduced supra topological spaces and studied  $S$  –continuous maps and  $S^*$  - continuous maps. In 2008, Devi *et al.* [3] introduced and studied a class of sets called supra  $\alpha$ -open and a class of maps called  $s\alpha$ -continuous between topological spaces, respectively. Ravi *et al.* [10] introduced and studied a class of sets called supra  $g$ -closed and a class of maps called supra  $g$ -continuous and supra  $g$ -closed respectively. Kamaraj *et al.* [4] introduced the concepts of supra  $sg$  -closed sets and supra  $gs$ -closed sets and study their basic properties. Also, introduced the concepts of supra normal spaces and supra- $s$ -normal spaces. In this paper, we obtain the characterizations of supra semi normal space by using supra semi generalized-open sets (supra  $sg$ - open sets). Moreover, inorder to obtain preservation theorems of supra semi normal spaces, we introduce the concepts of supra pre  $sg$ - continuous maps and supra pre  $sg$  –closed maps and also investigate several properties of new notions

**2. PRELIMINARIES**

Throughout this paper  $(X, \tau)$ ,  $(Y, \sigma)$  and  $(Z, \nu)$  (or simply,  $X$ ,  $Y$  and  $Z$ ) denote topological spaces on which no separation axioms are assumed unless explicitly stated. For a subset  $A$  of  $(X, \tau)$ , the closure and the interior of  $A$  in  $X$  with respect to  $\tau$  are denoted by  $cl(A)$  and  $int(A)$  respectively. The complement of  $A$  is denoted by  $X \setminus A$ .

**Definition 2.1 [6, 11]:** Let  $X$  be a non-empty set. The subfamily  $\mu \subseteq P(X)$  where  $P(X)$  is the power set of  $X$  is said to be a supra topology on  $X$  if  $X \in \mu$  and  $\mu$  is closed under arbitrary unions.  $(X, \mu)$  is called a supra topological space.

The elements of  $\mu$  are said to be supra open in  $(X, \mu)$ .

The complement of supra open set is called supra closed set.

**Definition 2.2 [3]:** Let  $A$  be a subset of  $X$ . Then

- (i) The supra closure of a set  $A$  is, denoted by  $cl^\mu(A)$ , defined as  $cl^\mu(A) = \bigcap \{B : B \text{ is a supra closed and } A \subseteq B\}$ .
- (ii) the supra interior of a set  $A$  is, denoted by  $int^\mu(A)$ , defined as  $int^\mu(A) = \bigcup \{B : B \text{ is a supra open and } A \supseteq B\}$ .

**Definition 2.3 [6]:** Let  $(X, \tau)$  be a topological space and  $\mu$  be a supra topology on  $X$ . We call  $\mu$  is a supra topology associated with  $\tau$  if  $\tau \subseteq \mu$ .

**Definition 2.4:** Let  $(X, \mu)$  be a supra topological space. A subset  $A$  of  $X$  is called

- (i) supra semi-open [3] if  $A \subseteq \text{cl}^\mu(\text{int}^\mu(A))$ ;
- (ii) supra  $\alpha$ -open [3,12] if  $A \subseteq \text{int}^\mu(\text{cl}^\mu(\text{int}^\mu(A)))$ ;
- (iii) supra  $b$ -open [11] if  $A \subseteq \text{cl}^\mu(\text{int}^\mu(A)) \cup \text{int}^\mu(\text{cl}^\mu(A))$ ;
- (iv) supra  $\beta$ -open [9] if  $A \subseteq \text{cl}^\mu(\text{int}^\mu(\text{cl}^\mu(A)))$ ;
- (v) supra pre-open [12] if  $A \subseteq \text{int}^\mu(\text{cl}^\mu(A))$ .

The complements of the above mentioned open sets are called their respective closed sets.

**Definition 2.5 [4]:** Let  $A$  be a subset of  $(X, \mu)$ . Then

- (i) the supra semi-closure of  $A$  is, denoted by  $\text{scl}^\mu(A)$ , defined as  $\text{scl}^\mu(A) = \bigcap \{B : B \text{ is a supra semi-closed and } A \subseteq B\}$ .
- (ii) the supra semi-interior of  $A$  is, denoted by  $\text{sint}^\mu(A)$ , defined as  $\text{sint}^\mu(A) = \bigcup \{G : G \text{ is a supra semi-open and } A \supseteq G\}$ .

**Definition 2.6[4]:** Let  $(X, \mu)$  be a supra topological space. A subset  $A$  of  $X$  is called Suprasg-closed if  $\text{scl}^\mu(A) \subseteq U$  whenever  $A \subseteq U$  and  $U$  is supra semi-open in  $(X, \mu)$ .

**Definition 2.7[5]:** Let  $(X, \tau)$  and  $(Y, \sigma)$  be two topological spaces with  $\tau \subseteq \mu$  and  $\sigma \subseteq \lambda$ . A map  $f : (X, \mu) \rightarrow (Y, \lambda)$  is called

- (i) suprasg-continuous if the inverse image of each open set of  $Y$  is a supra sg-open set in  $X$ .
- (ii) Supra sg-irresolute if the inverse image of each supra sg-closed set of  $Y$  is a supra sg-closed set in  $X$ .
- (iii) Supra pre semi-closed (resp. supra pre semi-open) if the image of each semi-closed (resp. semi-open) set of  $X$  is supra semi-closed (resp. supra semi-open) in  $Y$ .

**Definition 2.8[4]:** A space  $X$  is called supra normal if for any pair of disjoint supra closed subsets  $A$  and  $B$  of  $X$ , there exist disjoint supra open sets  $U$  and  $V$  such that  $A \subseteq U$  and  $B \subseteq V$ .

**Definition 2.9[4]:** A space  $X$  is called supras-normal if for any pair of disjoint supraclosed subsets  $A$  and  $B$  of  $X$ , there exist disjoint suprasemi-open sets  $U$  and  $V$  such that  $A \subseteq U$  and  $B \subseteq V$ .

### 3. Supra semi-normal space

**Definition 3.1:** A space  $X$  is called supra semi normal if for each pair of disjoint supra semi-closed sets  $A$  and  $B$ , there exist disjoint supra-semi open sets  $U$  and  $V$  such that  $A \subseteq U$  and  $B \subseteq V$ .

**Definition 3.2:** A space  $X$  is called supra  $T_{1/2}$  if every supra  $g$ -closed set of  $X$  is supra closed in  $X$ .

**Definition 3.3:** A space  $X$  is called supra semi  $T_{1/2}$  if every supra  $sg$ -closed set of  $X$  is supra semi-closed in  $X$ .

**Theorem 3.4:** Let  $(X, \mu)$  be supra topological space. The following properties are equivalent.

- a)  $X$  is supra semi-normal.
- b) For each pair of disjoint supra semi-closed sets  $A$  and  $B$ , there exist disjoint supra  $sg$ -open sets  $U$  and  $V$  such that  $A \subseteq U$  and  $B \subseteq V$ .
- c) For each supra semi-closed set  $A$  and each supra semi-open set containing  $A$ , there exist a supra  $sg$ -open set  $G$  such that  $A \subseteq G \subseteq \text{scl}^\mu(G) \subseteq U$ .
- d) For each supra semi-closed set  $A$  and each supra  $sg$ -open set  $U$  containing  $A$ , there exist supra semi-open set  $G$ , such that  $A \subseteq G \subseteq \text{scl}^\mu(G) \subseteq \text{sint}^\mu(G)$ .
- e) For each supra  $sg$ -closed set  $A$  and each supra semi-open set  $U$  containing  $A$ , there exist supra semi open set  $G$ , such that  $A \subseteq \text{scl}^\mu(A) \subseteq G \subseteq \text{scl}^\mu(G) \subseteq U$ .
- f) For each supra semi-closed set  $A$  of  $X$  and supra semi open set  $U$  containing  $A$ , there exists  $G \in \text{S-SO}(X) \cap \text{S-SC}(X)$  such that  $A \subseteq G \subseteq U$ .

**Proof:**

(a)  $\Rightarrow$  (b): It is obvious, since every supra semi-open set is supra  $sg$ -open set.

$(b) \Rightarrow (c)$ : Let  $A \in S\text{-SC}(X)$  and  $U \in S\text{-SO}(X)$  containing  $A$ . Then  $A \cap (X \setminus U) = \emptyset$  and  $X \setminus U \in SC(X)$ . There exist supra sg-open sets  $G$  and  $V$  such that  $A \subseteq G$ ,  $X \setminus U \subseteq V$ ,  $G \cap V = \emptyset$ . Therefore, we have  $A \subseteq G \subseteq X \setminus U \subseteq V$  and hence  $\text{scl}^{\mu}(G) \subseteq \text{scl}^{\mu}(X \setminus U) \subseteq U$  since  $X \setminus U$  is supra sg-closed and  $U \in S\text{-SO}(X)$ . Consequently, we obtain  $A \subseteq G \subseteq \text{scl}^{\mu}(G) \subseteq U$ .

$(c) \Rightarrow (d)$ : Let  $A \in S\text{-SC}(X)$  and  $U$  be a supra sg-open set containing  $A$ . We have  $A \subseteq \text{sint}^{\mu}(U)$  and  $\text{sint}^{\mu}(U) \in S\text{-SO}(X)$ . There exist a supra sg-open set  $V$  such that  $A \subseteq V \subseteq \text{sint}^{\mu}(V) \subseteq \text{sint}^{\mu}(U)$ . Put  $G = \text{sint}^{\mu}(V)$ , then we obtain  $G \in S\text{-SO}(X)$  and  $A \subseteq G \subseteq \text{sint}^{\mu}(G) \subseteq \text{sint}^{\mu}(U)$ .

$(d) \Rightarrow (e)$ : Let  $A$  be supra sg-closed set and  $U \in S\text{-SO}(X)$  containing  $A$ . Then, we have  $\text{scl}^{\mu}(A) \subseteq U$  and  $\text{scl}^{\mu}(A) \in S\text{-SC}(X)$ . Since every supra semi open set is supra sg-open, there exist  $G \in S\text{-SO}(X)$  such that  $A \subseteq \text{scl}^{\mu}(A) \subseteq G \subseteq \text{scl}^{\mu}(G) \subseteq U$ .

$(e) \Rightarrow (f)$ : Let  $A \in S\text{-SC}(X)$  and  $U \in S\text{-SO}(X)$  containing  $A$ . There exist  $V \in S\text{-SO}(X)$  such that  $A \subseteq V \subseteq \text{scl}^{\mu}(V) \subseteq U$ . Put  $G = \text{scl}^{\mu}(V)$ , then  $G$  is supra semi-open and supra semi-closed and  $A \subseteq G \subseteq U$ .

$(f) \Rightarrow (a)$ : Let  $A$  and  $B$  be any pair of disjoint supra semi-closed sets. Then we have  $A \subseteq X \setminus B \in S\text{-SO}(X)$  and there exist  $U \in S\text{-SO}(X) \cap S\text{-SC}(X)$  such that  $A \subseteq U \subseteq X \setminus B$ . Now, put  $V = X \setminus U$  then we obtain  $A \subseteq U$ ,  $B \subseteq V \in S\text{-SO}(X)$  and  $U \cap V = \emptyset$ . This shows that  $X$  is supra semi-normal.

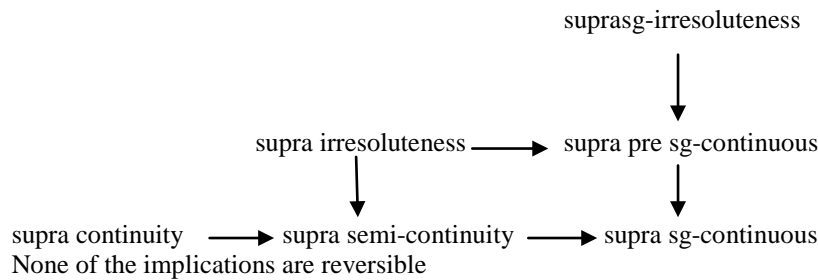
#### 4. Supra pre sg-continuous maps

In this section, we introduce a new class of functions called supra pre sg-continuous maps.

**Definition 4.1:** Let  $(X, \tau)$  and  $(Y, \sigma)$  be two supra topological space and  $\tau \subseteq \mu$ . A map  $f: (X, \mu) \rightarrow (Y, \sigma)$  is said to be supra pre sg-continuous if the inverse image of each semi-closed set in  $Y$  is supra sg-closed set in  $X$ .

**Definition 4.2:** Let  $(X, \tau)$  and  $(Y, \sigma)$  be two supra topological space and  $\tau \subseteq \mu, \sigma \subseteq \lambda$ . A map  $f: (X, \mu) \rightarrow (Y, \lambda)$  is called supra pre sg\* - continuous if the inverse image each supra semi-closed set in  $Y$  is supra sg-closed in  $X$ .

**Remark 4.3:** From the above definition we have the following implications



**Theorem 4.4:** Let  $(X, \tau)$  and  $(Y, \sigma)$  be two supra topological space with  $\tau \subseteq \mu, \sigma \subseteq \lambda$ . A map  $f: (X, \mu) \rightarrow (Y, \lambda)$  is called supra pre sg- continuous and supra pre semi-closed then  $f$  is supra sg-irresolute.

**Proof:** Let  $K$  be any supra sg-closed set of  $Y$  and  $U$  be supra semi open set containing  $f^{-1}(K)$ . Since  $f$  is supra pre semi-closed, there exist supra semi open set  $V$  in  $Y$  such that  $K \subseteq V$  and  $f^{-1}(V) \subseteq U$ . Since  $K$  is supra sg-closed in  $Y$ ,  $\text{scl}^{\mu}(V) \subseteq V$  and hence  $f^{-1}(\text{scl}^{\mu}(V)) \subseteq f^{-1}(V) \subseteq U$ . Since  $f$  is supra pre sg-continuous.  $f^{-1}(\text{scl}^{\mu}(V))$  is supra sg-closed in  $X$  and hence  $\text{scl}^{\mu}(f^{-1}(K)) \subseteq \text{scl}^{\mu}(f^{-1}(\text{scl}^{\mu}(V))) \subseteq U$ . This shows that  $f^{-1}(K)$  supra sg-closed in  $X$ . Hence  $f$  is supra sg-irresolute.

**Corollary 4.5:** Every supra irresolute, supra pre-semi closed function is supra sg-irresolute.

**Corollary 4.6:** Let  $(X, \tau)$  and  $(Y, \sigma)$  be topological space with  $\tau \subseteq \mu, \sigma \subseteq \lambda$ . If a space  $X$  is supra semi  $T_{1/2}$  and  $f: (X, \mu) \rightarrow (Y, \lambda)$  is onto supra irresolute and supra pre semi-closed then the space  $(Y, \sigma)$  is supra semi  $T_{1/2}$ .

**Proof:** Let  $A$  be supra sg-closed set in  $Y$ . we have that  $f^{-1}(A)$  is supra sg-closed in  $X$  [In 5 Theorem 3.6]. since  $X$  is supra semi  $T_{1/2}$ ,  $f^{-1}(A)$  is supra semi-closed and hence  $A$  is supra semi closed. Hence  $Y$  is supra  $T_{1/2}$  space.

**Theorem 4.7:** Let  $(X, \tau)$  and  $(Y, \sigma)$  be two topological space with  $\tau \subseteq \mu, \sigma \subseteq \lambda$ . Let  $X$  be supra semi  $T_{1/2}$  space. A map  $f: X \rightarrow Y$  is supra pre  $sg^*$ -continuous if and only if  $f$  is supra semi-irresolute.

**Proof:** Suppose that  $f$  is supra pre  $sg^*$ -continuous. Let  $K$  be any supra semi closed set of  $Y$ . Then  $f^{-1}(K)$  is supra sg-closed in  $X$ . Since  $X$  is supra semi  $T_{1/2}$ ,  $f^{-1}(K)$  is supra semi-closed. Hence  $f$  is supra semi-irresolute. The converse is obvious.

**Corollary 4.8:** Let  $(X, \tau)$  and  $(Y, \sigma)$  be two topological space with  $\tau \subseteq \mu, \sigma \subseteq \lambda$ . A map  $f: (X, \mu) \rightarrow (Y, \lambda)$  is supra sg-irresolute and  $X$  is supra semi  $T_{1/2}$  then  $f$  is supra semi irresolute.

**Proof:** Let  $V$  be supra semi-closed in  $Y$ . Every supra semi-closed set is supra sg-closed. Since  $f$  is supra sg-irresolute then  $f^{-1}(V)$  is supra sg-closed in  $X$ . Since  $X$  is supra semi  $T_{1/2}$ ,  $f^{-1}(V)$  is supra semi-closed in  $X$ . Hence  $f$  is supra semi-irresolute.

**Definition 4.9:** Let  $(X, \tau)$  and  $(Y, \sigma)$  be two topological space with  $\tau \subseteq \mu, \sigma \subseteq \lambda$ . A map  $f: (X, \mu) \rightarrow (Y, \lambda)$  is called supra pre semi<sup>\*</sup>-closed if the image of each supra semi-closed in  $X$  is supra semi-closed in  $Y$ .

**Theorem 4.10:** Let  $(X, \tau)$  and  $(Y, \sigma)$  be two topological space with  $\tau \subseteq \mu, \sigma \subseteq \lambda$ . If a map  $f: (X, \mu) \rightarrow (Y, \lambda)$  is supra pre  $sg^*$ -continuous, supra pre semi<sup>\*</sup>-closed injection and  $Y$  is supra semi normal space, then  $X$  is supra semi normal.

**Proof:** Let  $A$  and  $B$  be any two disjoint supra semi-closed sets of  $X$ . Since  $f$  is supra pre semi<sup>\*</sup>-closed injection,  $f(A)$  and  $f(B)$  are disjoint supra semi-closed sets of  $Y$ . By supra semi normality of  $Y$ , there exist supra semi-open sets  $U$  and  $V$  in  $Y$  such that  $f(A) \subseteq U$  and  $f(B) \subseteq V$ . Since  $f$  is supra pre  $sg^*$ -continuous,  $f^{-1}(U)$  and  $f^{-1}(V)$  are disjoint supra sg-closed sets containing  $A$  and  $B$  respectively. By theorem 3.4,  $X$  is supra semi normal.

**Corollary 4.11:** The inverse image of supra semi normal space under an supra irresolute and supra pre semi<sup>\*</sup>-closed injection is supra semi-normal.

## 5. Supra pre sg-closed maps

In this section, we introduce the new class of maps called supra pre sg-closed and supra pre  $sg^*$ -closed maps.

**Definition 5.1:** Let  $(X, \tau)$  and  $(Y, \sigma)$  be two topological space with  $\tau \subseteq \mu, \sigma \subseteq \lambda$ . If a map  $f: (X, \mu) \rightarrow (Y, \lambda)$  is called supra pre sg-closed if the image of each semi closed set in  $X$  is supra sg-closed in  $Y$ .

**Definition 5.2:** Let  $(X, \tau)$  and  $(Y, \sigma)$  be two topological space with  $\tau \subseteq \mu, \sigma \subseteq \lambda$ . A map  $f: (X, \mu) \rightarrow (Y, \lambda)$  is called supra  $sg^*$ -closed if image of each supra semi-closed in  $X$  is supra sg-closed in  $Y$ .

**Theorem 5.3:** Let  $(X, \tau)$  and  $(Y, \sigma)$  be two topological space with  $\tau \subseteq \mu, \sigma \subseteq \lambda$ . A map  $f: (X, \mu) \rightarrow (Y, \lambda)$  is an supra semi irresolute and supra pre  $sg^*$ -closed map and  $A$  is a supra sg-closed of  $X$ , then  $f(A)$  is a supra sg-closed in  $Y$ .

**Proof:** Let  $A$  be a supra sg-closed set of  $X$ . Let  $f(A) \subseteq U$  where  $U$  is supra semi-open set of  $Y$ . Then  $A \subseteq f^{-1}(U)$  and  $f^{-1}(U)$  is supra semi-open in  $X$  because  $f$  is supra semi irresolute. Since  $f$  is supra pre  $sg^*$ -closed  $scl^h(A)$  is supra semi closed in  $X$  and  $f(scl^h(A))$  is supra sg-closed in  $Y$  and  $f(scl^h(A)) \subseteq U$ . Therefore we have  $scl^h f(A) \subseteq scl^h(f(scl^h(A))) = f(scl^h(A)) \subseteq U$ . Hence  $f(A)$  is supra sg-closed in  $Y$ .

**Proposition 5.4:** Let  $(X, \tau)$  and  $(Y, \sigma)$  be two topological space with  $\tau \subseteq \mu, \sigma \subseteq \lambda$ . A surjective map  $f: (X, \mu) \rightarrow (Y, \lambda)$  is supra pre  $sg^*$ -closed if and only if for each subset  $B$  of  $Y$  and each supra open set  $U$  of  $X$  contain  $f^{-1}(B)$ , there exist a supra sg-open set  $V$  of  $Y$  such that  $B \subseteq V$  and  $f^{-1}(V) \subseteq U$ .

**Proof:**

**Necessity:** Suppose that  $f$  is supra pre  $sg^*$ -closed. Let  $B$  be any subset of  $Y$  and  $U$  is supra semi open set containing  $f^{-1}(B)$ .  $V=Y \setminus f(X \setminus U)$  then  $V$  is supra  $sg$ -open in  $Y$ ,  $B \subseteq V$  and  $f^{-1}(V) \subseteq U$ .

**Sufficient:** Let  $F$  be any supra semi-closed set of  $X$ . Put  $B = Y \setminus f(F)$  then we have  $f^{-1}(B) \subseteq X \setminus F$  supra semi open in  $X$ . There exist a supra  $sg$ -open set  $V$  of  $Y$  such that  $B \subseteq V$  and  $f^{-1}(V) \subseteq X \setminus F$ . Therefore we obtain  $f(F) = Y - V$  and hence  $f(F)$  is supra  $sg$ -closed in  $Y$ . Hence  $f$  is supra pre  $sg^*$ -closed.

**Theorem 5.5:** Let  $(X, \tau)$  and  $(Y, \sigma)$  be two topological space with  $\tau \subseteq \mu$ ,  $\sigma \subseteq \lambda$ . A surjective map  $f: (X, \mu) \rightarrow (Y, \lambda)$  is supra pre  $sg^*$ -closed and supra semi-irresolute surjection and  $X$  is supra semi-normal space, then  $Y$  is supra semi normal.

**Proof:** Let  $A$  and  $B$  be any pair of disjoint supra semi-closed sets of  $Y$ . Since  $f$  is supra semi-irresolute,  $f^{-1}(A)$  and  $f^{-1}(B)$  are disjoint semi closed sets of  $X$ . By semi normality of  $X$ , there exist supra semi open set  $U$  and  $V$  of  $X$  such that  $f^{-1}(A) \subseteq U$  and  $f^{-1}(B) \subseteq V$  and  $U \cap V = \emptyset$ . By proposition 5.4 there exist supra  $sg$ -open set  $G$  and  $H$  such that  $A \subseteq G$  and  $B \subseteq H$ ,  $f^{-1}(G) \subseteq U$  and  $f^{-1}(H) \subseteq V$ , since  $f$  is surjective and  $U \cap V = \emptyset$ . We have  $G \cap H = \emptyset$ . By theorem 3.4 we have  $Y$  is supra semi-normal.

**Corollary 5.6:** Supra semi normality is preserved under supra pre semi<sup>\*</sup>-closed and irresolute map.

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