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## ON WEAKLY SEMI CLOSED SETS IN TOPOLOGICAL SPACES

# BASAVARAJ M. ITTANAGI, VEERESHA A SAJJANAR\*

Department of Mathematics, Siddaganga Institute of Technology, Affiliated to VTU, Belagavi, Tumakuru-03, Karnataka State, India.

\*Department of Mathematics, Sri Krishna Institute of Technology, Bangalore, Karnataka State, India.

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## **ABSTRACT**

In this research paper, a new class of closed sets called weakly semi-closed sets (ws-closed sets) in topological spaces are introduced and studied. A subset A of a topological space  $(X, \tau)$  is called ws-closed set if U contains semi-closure of A whenever U contains A and U is w-open set in  $(X, \tau)$ . This new class of sets lies between the class of all semi-closed sets and generalised semi-pre regular closed sets in topological spaces. Also some of their properties have been investigated.

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**Keywords:** Semi-closed sets, w-closed sets, semi pre-closed sets and ws-closed sets.

## 1. INTRODUCTION

In 1970 N. Levine [18], first introduced the concept of generalized closed sets were defined and investigated. In 2000 M. Sheik John [33], introduced and studied w-closed sets in topological space X. Throughout this paper X or  $(X,\tau)$  represent non-empty topological space. Let A be subset of a topological space X. cl(A), int(A), scl(A), acl(A) and spcl(A) denote the closure of A, the interior of A, the semi-closure of A and the semi pre closure of A in X respectively.

### 2. PRELIMINARIES

**Definition 2.1:** A subset A of a topological space  $(X, \tau)$  is called a

- i. Regular open set [32] if A=int(cl(A)) and regular closed if A=cl(int(A))
- ii. Semi-open set [19] if  $A \subseteq cl(int(A))$  and a semi-closed set if  $int(cl(A)) \subseteq A$ .
- iii.  $\alpha$ -open set [20] if A  $\subseteq$ int(cl(int(A))) and a  $\alpha$ -closed set if cl(int(cl(A)))  $\subseteq$  A.
- iv. Generalized semi pre closed set (gsp-closed) [8] if  $spcl(A) \subseteq U$  whenever  $A \subseteq U$  and U is open in  $(X, \tau)$ .
- v. w-closed set[33] if  $cl(A) \subseteq U$  whenever  $A \subseteq U$  and U is semi-open in  $(X, \tau)$ .
- vi. gspr-closed set[10] if  $spcl(A) \subseteq U$  whenever  $A \subseteq U$  and U is regular -open in  $(X, \tau)$ .
- vii.  $\alpha gp\text{-closed set}[11]$  if  $cl(A) \subseteq U$  whenever  $A \subseteq U$  and U is pre-open in  $(X, \tau)$ .
- viii. \*g $\alpha$ -closed set [41] if cl(A)  $\subseteq$  U whenever A  $\subseteq$  U and U is  $g\alpha$  open in (X,  $\tau$ ).
- ix.  $g^*$ s-closed set[40] if scl(A)  $\subseteq$  U whenever A  $\subseteq$  U and U is  $\alpha g$  -open in (X,  $\tau$ ).
- x. rb-closed set[24] if  $cl(A) \subseteq U$  whenever  $A \subseteq U$  and U is b-open in  $(X, \tau)$ .
- xi.  $g\xi^*$  -closed set[17] if  $\alpha cl(A) \subseteq U$  whenever  $A \subseteq U$  and U is  $\#g\alpha$  open in  $(X, \tau)$ .

Corresponding Author: Veeresha A Sajjanar\*,\*Department of Mathematics, Sri Krishna Institute of Technology, Bangalore, Karnataka state, India.

#### 3. BASIC PROPERTIES OF WS-CLOSED SETS IN TOPOLOGICAL SPACE

**Definition 3.1:** A subset A of a topological space  $(X,\tau)$  is called weakly semi closed (ws-closed) set if  $scl(A) \subseteq U$ , whenever  $A \subseteq U$  and U is w-open set in  $(X, \tau)$ . The family of all ws -closed sets X is denoted by WSC(X). the compliment of ws -closed set is called ws-open set in  $(X, \tau)$ . The family of all ws-open sets in X is denoted by WSO(X).

**Example 3.2:** Let  $X = \{a, b, c, d\}, \tau = \{X, \phi, \{a\}, \{b\}, \{a, b\}, \{a, b, c\}\}.$  Then

Closed sets in  $(X,\tau)$  are X,  $\phi$ ,  $\{d\}$ ,  $\{c,d\}$ ,  $\{a,c\}$ ,  $\{a,c,d\}$ ,  $\{b,c,d\}$ .

Semi-closed sets in  $(X, \tau)$  are  $X, \phi, \{a\}, \{b\}, \{c\}, \{d\}, \{a, c\}, \{a, d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{a, c, d\}, \{b, c, d\}$ .

W-closed sets in  $(X,\tau)$  are  $X, \phi, \{d\}, \{c, d\}, \{a, c, d\}, \{b, c, d\}$ .

W-open sets in  $(X,\tau)$  are  $X, \phi, \{a\}, \{b\}, \{a, b\}, \{a, b, c\}$ .

ws-closed sets in  $(X, \tau)$  are  $X, \phi, \{a\}, \{b\}, \{c\}, \{d\}, \{a, c\}, \{a, d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{a, b, d\}, \{a, c, d\}, \{b, c, d\}$ . ws-open sets in  $(X, \tau)$  are  $X, \phi, \{a\}, \{b\}, \{c\}, \{a, d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{a, b, c\}, \{a, b, d\}, \{a, c, d\}, \{b, c, d\}$ .

We prove that the class of ws-closed sets are properly lies between the class of all semi-closed sets and generalised semi-pre regular closed sets in topological spaces.

**Theorem 3.3:-** Every semi-closed [19] set in X is ws-closed set in X.

**Proof**: Let A be a semi-closed set in X. Let U be any w-open set in X such that  $A \subseteq U$ . Since A is semi-closed, we have  $scl(A) = A \subseteq U$ , we have  $scl(A) \subseteq U$ . Hence A is ws-closed set in X.

Remark 3.4: The converse of the above Theorem 3.3 need not be true as seen from the following Example 3.5.

**Example 3.5:** Let  $X = \{a, b, c, d\}$  and  $\mathbb{T} = \{X, \phi, \{a\}, \{b\}, \{a, b\}, \{a, b, c\}\}$  then the set  $A = \{a, b, d\}$  is ws-closed set but not semi-closed in X.

**Corollary 3.6**: In a topological space  $(X,\tau)$ ,

- i) Every regular closed [32] set in X is ws-closed set in X.
- ii) Every closed set in X is ws-closed set in X.
- iii) Every α-closed [20] set in X is ws-closed set in X.
- iv) Every g\*-closed [37] set in X is ws-closed set in X.
- v) Every  $*g\alpha$  -closed [41] set in X is ws-closed set in X.
- vi) Every g<sup>#</sup>s –closed [40] set in X is ws-closed set in X.
- vii) Every rb -closed [24] set in X is ws-closed set in X.
- viii) Every **g**-closed set in X is ws-closed set in X.
- ix) Every  $g\xi^*$  -closed [17]] set in X is ws-closed set in X.
- x) Every  $\alpha gp$  -closed [11] set in X is ws-closed set in X.

# Proof:

- i) In view of the fact that every regular closed is semi-closed, therefore by 3.3 every regular closed is ws-closed set.
- ii) In view of the fact that every closed set is semi-closed, therefore by 3.3 every closed set is ws-closed set.
- iii) in view of the fact that every  $\alpha$  closed is semi-closed, therefore by 3.3 every  $\alpha$  closed is ws-closed set.
- iv) Let A be  $g^{\#}$ -closed set in X. Let U be any w-open set in X s.t A  $\subseteq$  U. Since A is  $g^{\#}$ -closed, we have  $cl(A) = A \subseteq U$ , we have  $scl(A) \subseteq U$ . Hence A is ws-closed set in X.
- v) Let A be \*g\alpha -closed set in X. Let U be any w-open set in X s.t A  $\subseteq$  U. Since A is \*g\alpha -closed, we have  $scl(A) = A \subseteq U$ , we have  $scl(A) \subseteq U$ . Hence A is ws-closed set in X.
- vi) Let A be  $g^{\sharp}s$  -closed set in X. Let U be any w-open set in X s.t A  $\subseteq$  U. Since A is  $g^{\sharp}s$  -closed, we have  $scl(A) = A \subseteq U$ , we have  $scl(A) \subseteq U$ . Hence A is ws-closed set in X.
- vii) Let A be rb -closed set in X. Let U be any w-open set in X s.t  $A \subseteq U$ . Since A is rb -closed, we have  $scl(A) = A \subseteq U$ , we have  $scl(A) \subseteq U$ . Hence A is ws-closed set in X.
- viii) Let A be  $\ddot{g}$  -closed set in X. Let U be any w-open set in X s.t A  $\subseteq$  U. Since A is  $\ddot{g}$  -closed, we have  $scl(A) = A \subseteq U$ , we have  $scl(A) \subseteq U$ . Hence A is ws-closed set in X.
- ix) Let A be  $g\xi^*$  -closed set in X. Let U be any w-open set in X s.t A  $\subseteq$  U. Since A is  $g\xi^*$  -closed, we have  $scl(A) = A \subseteq U$ , we have  $scl(A) \subseteq U$ . Hence A is ws-closed set in X.
- x) Let A be  $\alpha gp$  -closed set in X. Let U be any w-open set in X s.t A  $\subseteq$  U. Since A is  $\alpha gp$  -closed, we have  $scl(A) = A \subseteq U$ , we have  $scl(A) \subseteq U$ . Hence A is ws-closed set in X.

Remark 3.7: The converse of the above Corollary 3.6 need not be true as seen from the following Example 3.8.

**Example 3.8:** Let  $X = \{a, b, c, d\}$  and  $T = \{X, \phi, \{a\}, \{b\}, \{a, b\}, \{a, b, c\}\}$  then the sets

- i. regular-closed sets in  $(X, \tau)$  are  $X, \phi, \{a, c, d\}, \{b, c, d\}$ .
- ii. closed sets in  $(X, \tau)$  are  $X, \phi, \{d\}, \{c, d\}, \{a, c, d\}, \{b, c, d\}$ .
- iii.  $\alpha$  -closed, sets in  $(X, \tau)$  are  $X, \phi, \{c\}, \{d\}, \{c, d\}, \{a, c, d\}, \{b, c, d\}$ .
- iv.  $g^{\#}$ -closed sets in  $(X, \tau)$  are  $X, \phi, \{d\}, \{c, d\}, \{a, c, d\}, \{b, c, d\}$ .
- v. \*g\alpha -closed sets in (X, \tau) are X,\phi,\{d\},\{c, d\},\{a, c, d\},\{b, c, d\}.
- vi.  $g^{\#}s$  -closed sets in  $(X, \tau)$  are  $X, \phi, \{a\}, \{b\}, \{c\}, \{d\}, \{a, c\}, \{a, d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{a, c, d\}, \{b, c, d\}$ .
- vii. rb -closed sets in  $(X, \tau)$  are  $X, \phi, \{c, d\}, \{a, c, d\}, \{b, c, d\}$ .
- viii.  $\ddot{g}$  -closed sets in  $(X, \tau)$  are  $X, \phi, \{d\}, \{c, d\}, \{a, c, d\}, \{b, c, d\}$ .
- ix.  $g\xi^*$  -closed sets in  $(X, \tau)$  are  $X, \phi, \{d\}, \{c, d\}, \{a, c, d\}, \{b, c, d\}$ .
- x.  $\alpha gp$  -closed sets in  $(X, \tau)$  are  $X, \phi, \{c\}, \{d\}, \{c, d\}, \{a, c, d\}, \{b, c, d\}$ . and

ws-closed sets in  $(X, \tau)$  are  $X, \phi, \{a\}, \{b\}, \{c\}, \{d\}, \{a, c\}, \{a, d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{a, b, d\}, \{a, c, d\}, \{b, c, d\}$ .

It is observed that set  $A=\{a,b,d\}$  is ws-closed set but not regular closed (closed,  $\alpha$  - closed,  $g^{\#}$ -closed,  $g^{\#}$ -cl

**Theorem 3.9:** Every ws-closed set in X is gspr-closed [10] set in X.

**Proof:** Let A be a ws-closed set in X. Let U be any regular open set in X such that  $A \subseteq U$ . Since every regular open set is w- open set and A is ws-closed set, we have  $scl(A) \subseteq U$ . Therefore  $scl(A) \subseteq U$ . Therefore U is regular open in X. Hence A is gspr-closed in X.

Remark 3.10: The converse of the above Theorem 3.9 need not be true as seen from the following Example 3.11.

**Example 3.11:** Let  $X = \{a, b, c d\}$ ,  $\tau = \{X, \phi, \{a, b\}, \{c, d\}\}$ . Then the set  $A = \{b\}$  is gspr -closed set but not ws-closed set in X.

## Corollary 3.12:

- i) Every ws-closed set is gsp-closed [8] set in X.
- ii) Every ws-closed set is rgb-closed [22] set in X.

## Proof:

- i) Follow from Govindappa Navalagi et all[8], every gspr-closed set is gsp-closed set and then follows from Theorem 3.9
- ii) Let A be a ws-closed set in X. Let U be any regular open set in X such that  $A \subseteq U$ . Since every regular open set is w- open set and A is ws-closed set, we have  $scl(A) \subseteq U$ . Therefore  $scl(A) \subseteq U$ . Therefore U is regular open in X. Hence A is rgb -closed in X

The converse of the Corollary 3.12 is need not be true in general as seen from the following Example 3.13.

**Example 3.13:** Let  $X = \{a, b, c d\}$ ,  $\tau = \{X, \phi, \{a, b\}, \{c, d\}\}$ . Then the set  $A = \{b\}$  is gsp (rgb) -closed set but not ws-closed set in X.

**Remark 3.14:** The following Example 3.15, shows that ws-closed sets are independent of gpr-closed [9] sets, wgr $\alpha$ -closed [16] sets, pgr $\alpha$ -closed [5] sets,  $\widehat{rg}$ -closed sets [31], gp closed [30] sets, rgw-closed [29] sets, rw-closed [2] sets, rg $\alpha$ -closed [36] sets,  $\beta$ -closed [35] sets.

**Example 3.15:** Let  $X = \{a, b, c, d\}, \tau = \{X, \phi, \{a\}, \{b\}, \{a, b\}, \{a, b, c\}\}$ . Then

- i) closed sets in  $(X, \tau)$  are  $X, \phi, \{d\}, \{c, d\}, \{a, c, d\}, \{b, c, d\}$ .
- ii) ws-closed sets in  $(X, \tau)$  are  $X, \phi, \{a\},\{b\},\{c\},\{d\},\{a, c\},\{a, d\},\{b, c\},\{b, d\},\{c, d\},\{a, b, d\},\{a, c, d\},\{b, c, d\}.$
- iii) gpr -closed sets in  $(X, \tau)$  are  $X, \phi, \{c\}, \{d\}, \{a, b\}, \{a, c\}, \{a, d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{a, b, d\}, \{a, c, d\}, \{b, c, d\}.$
- iv)  $wgr\alpha$  -closed sets in  $(X, \tau)$  are  $X, \phi, \{c\}, \{d\}, \{a, b\}, \{a, c\}, \{a, d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{a, b, c\}, \{a, c, d\}, \{b, c, d\}.$
- v)  $pgr\alpha$  -closed sets in  $(X, \tau)$  are  $X, \phi, \{c\}, \{d\}, \{a, b\}, \{a, c\}, \{a, d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{a, b, c\}, \{a, b, d\}, \{a, c, d\}, \{b, c, d\}.$

- vi) rg-closed sets in  $(X, \tau)$  are  $X, \phi, \{c\}, \{d\}, \{a, b\}, \{a, c\}, \{a, d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{a, b, c\}, \{a, b, d\}, \{a, c, d\}, \{b, c, d\}.$
- vii) gprw-closed sets in  $(X, \tau)$  are  $X, \phi, \{c\}, \{d\}, \{a, b\}, \{c, d\}, \{a, b, c\}, \{a, b, d\}, \{a, c, d\}, \{b, c, d\}$ .
- viii) rgw-closed sets in  $(X, \tau)$  are  $X, \phi, \{c\}, \{d\}, \{a, b\}, \{c, d\}, \{a, b, c\}, \{a, b, d\}, \{a, c, d\}, \{b, c, d\}.$
- ix) rw-closed sets in  $(X, \tau)$  are  $X, \phi, \{d\}, \{a, b\}, \{c, d\}, \{a, b, c\}, \{a, b, d\}, \{a, c, d\}, \{b, c, d\}.$
- x)  $rg\alpha$ -closed sets in  $(X, \tau)$  are  $X, \phi, \{c\}\{d\}, \{a, b\}, \{a, c\}, \{a, d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{a, b, c\}, \{a, b, d\}, \{a, c, d\}, \{b, c, d\}.$
- xi)  $\beta wg^{**}$ -closed sets in  $(X, \tau)$  are  $X, \phi, \{c\}\{d\}, \{a, b\}, \{a, c\}, \{a, d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{a, b, c\}, \{a, c, d\}, \{b, c, d\}.$

Therefore {a} is ws-closed in X but not gpr-closed (resp. wgra-closed, pgra-closed, rg-closed, gprw-closed, rgw-closed, rgc-closed, pgra-closed, pgra-closed,

Remark 3.16: The following Example 3.17, shows that ws-closed sets are independent of sets, wg-closed[23], gwa-closed [3] sets, g\*p-closed[39] sets,  $\beta$ wg\*-closed[7] sets,\*\*ga-closed[41] sets,  $\hat{g}$ -closed[38] sets,  $\tilde{g}$ -closed[14]sets, #ga-closed [6] sets, g\*-preclosed [39] sets and g#p#-closed sets [28].

**Example 3.17:** Let  $X = \{a, b, c\}$ ,  $\tau_1 = \{X, \phi, \{a\}, \{b\}, \{a, b\}\}$  and  $\tau_2 = \{X, \phi, \{a\}, \{b, c\}\}$ . Then

- i) closed sets in  $(X, \tau_1)$  are  $X, \phi, \{c\}, \{a, c\}, \{b, c\}$ .
- ii) ws-closed sets in  $(X, \tau_1)$  are  $X, \phi, \{a\}, \{b\}, \{c\}, \{a, c\}, \{b, c\}.$
- iii) wg-closed sets in  $(X, \tau_1)$  are  $X, \phi, \{c\}, \{a, c\}, \{b, c\}$ .
- iv) gwa-closed sets in  $(X, \tau_1)$  are  $X, \phi, \{c\}, \{a, c\}, \{b, c\}$ .
- v) g\*p-closed sets in  $(X, \tau_1)$  are  $X, \phi, \{c\}, \{a, c\}, \{b, c\}$ .
- vi)  $\beta$ wg\*-closed sets in  $(X, \tau_1)$  are  $X, \phi, \{c\}, \{a, c\}, \{b, c\}$ .
- vii) \*\* $g\alpha$ -closed sets in  $(X, \tau_1)$  are  $X, \phi, \{c\}, \{a, c\}, \{b, c\}$ .
- viii)  $\hat{g}$ -closed sets, in  $(X, \tau_1)$  are  $X, \phi, \{c\}, \{a, c\}, \{b, c\}$ .
- ix)  $\hat{g}$ -closed sets, in  $(X, \tau_1)$  are  $X, \phi, \{c\}, \{a, c\}, \{b, c\}$ .
- x)  $\#g\alpha$ -closed sets in  $(X, \tau_1)$  are  $X, \phi, \{c\}, \{a, c\}, \{b, c\}$ .
- xi) g\*-preclosed sets in  $(X, \tau_1)$  are  $X, \phi, \{c\}, \{a, c\}, \{b, c\}$ .
- xii) g#p#-closed sets in  $(X, \tau_1)$  are  $X, \phi, \{c\}, \{a, c\}, \{b, c\}$ . and also
- i) closed sets in  $(X, \tau_2)$  are  $X, \phi, \{a\}, \{b, c\}$ .
- ii) ws-closed sets in ( X,  $\tau_2$ ) are X,  $\phi$ ,{a},,{b, c}.
- iii) wg-closed set in  $(X, \tau_2)$  are  $X, \phi, \{a\}, \{b\}, \{c\}, \{a, b\}, \{a, c\}, \{b, c\}.$
- iv) gwa-closed sets in  $(X, \tau_2)$  are  $X, \phi, \{a\}, \{b\}, \{c\}, \{a, b\}, \{a, c\}, \{b, c\}.$
- v) g\*p-closed sets in  $(X, \tau_2)$  are  $X, \phi, \{a\}, \{b\}, \{c\}, \{a, b\}, \{a, c\}, \{b, c\}.$
- vi)  $\beta wg^*$ -closed sets in  $(X, \tau_2)$  are  $X, \phi, \{a\}, \{b\}, \{c\}, \{a, b\}, \{a, c\}, \{b, c\}.$
- vii) \*\*g\$\alpha\$-closed sets in (X, \$\tau\_2\$) are X, \$\phi\$, \$\{a}\$, \$\{b}\$, \$\{c}\$, \$\{a}\$, \$b\}, \$\{a}\$, \$\{b}\$, \$\{c}\$.
- viii)  $\hat{g}$ -closed sets in  $(X, \tau_2)$  are  $X, \phi, \{a\}, \{b\}, \{c\}, \{a, b\}, \{a, c\}, \{b, c\}.$
- ix)  $\tilde{g}$ -closed sets in  $(X, \tau_2)$  are  $X, \phi, \{a\}, \{b\}, \{c\}, \{a, b\}, \{a, c\}, \{b, c\}$ .
- x)  $\#g\alpha$ -closed sets in  $(X, \tau_2)$  are  $X, \phi, \{a\}, \{b\}, \{c\}, \{a, b\}, \{a, c\}, \{b, c\}.$
- xi)  $g^*$ -preclosed sets in  $(X, \tau_2)$  are  $X, \phi, \{a\}, \{b\}, \{c\}, \{a, b\}, \{a, c\}, \{b, c\}.$
- xii) g#p#-closed sets in (X,  $\tau_2$ ) are X,  $\phi$ , {a}, {b},{c},{a, b},{a, c},{b, c}.

Therefore {b} is ws-closed set in  $(X, \tau_1)$  but not in wg-closed (resp., gwa-closed, g\*p-closed,  $\beta$ wg\*-closed, \*\*ga-closed,  $\widetilde{g}$  -closed,  $\widetilde{g}$  -closed, #ga-closed, g\*-preclosed, g#p#-closed) set in  $(X, \tau_1)$ .

Meanwhile {b} in in wg-closed (resp., gwa-closed, g\*p-closed,  $\beta$ wg\*-closed, \*\*ga-closed, g-closed, g-closed, #ga-closed, g\*-preclosed, g#p#-closed )set in (X,  $\tau_2$ ) but not ws-closed set in (X,  $\tau_2$ ).

Remark 3.18: The following Example 3.19 shows that ws-closed sets are independent of sets g-closed[18] sets,  $g\alpha$ -closed[14] sets,  $g\alpha$ -closed[21] sets,  $g\alpha$ -closed[21] sets,  $g\alpha$ -closed[12] sets,  $g\alpha$ -closed[13] sets,  $g\alpha$ -closed[14] sets,  $g\alpha$ -closed[15] sets,  $g\alpha$ -closed[16] sets,  $g\alpha$ -closed[17] sets,  $g\alpha$ -closed[18] sets,  $g\alpha$ -closed[18] sets,  $g\alpha$ -closed[18] sets,  $g\alpha$ -closed[18] sets,  $g\alpha$ -closed[19] sets,

**Example 3.19:** Let  $X = \{a, b, c, d\}$ ,  $\tau_1 = \{X, \phi, \{a\}, \{a, b\}, \{a, b, c\}\}$  and  $\tau_2 = \{X, \phi, \{a, b\}, \{c, d\}\}$ . Then

- i) closed sets in  $(X, \tau_1)$  are  $X, \phi, \{d\}, \{c, d\}, \{b, c, d\}$ .
- ii) ws-closed sets in  $(X, \tau_1)$  are  $X, \phi, \{a\}, \{c\}, \{d\}, \{a, c\}, \{a, d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{a, b, d\}, \{a, c, d\}, \{b, c, d\}.$

- iii) g-closed sets in  $(X, \tau_1)$  are  $X, \phi, \{d\}, \{a, d\}, \{b, d\}, \{c, d\}, \{a, c, d\}, \{b, c, d\}$ .
- iv) sg-closed sets in  $(X, \tau_1)$  are  $X, \phi, \{b\}, \{c\}, \{d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{b, c, d\}$ .
- v)  $g\alpha$  closed sets in  $(X, \tau_1)$  are  $X, \phi, \{b\}, \{c\}, \{d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{b, c, d\}$ .
- vi) sgb -closed sets in  $(X, \tau_1)$  are  $X, \phi, \{b\}, \{c\}, \{d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{b, c, d\}$ .
- vii)  $rg*b-closed sets in (X, \tau_1) \ are \ X, \phi, \{b\}, \{c\}, \{d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{b, c, d\}$
- viii) pgpr- closed sets in  $(X, \tau_1)$  are  $X, \phi, \{b\}, \{c\}, \{d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{b, c, d\}$
- ix) gab- closed sets in  $(X, \tau_1)$  are  $X, \phi, \{b\}, \{c\}, \{d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{b, c, d\}$
- x) rps- closed sets in  $(X, \tau_1)$  are  $X, \phi, \{b\}, \{c\}, \{d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{b, c, d\}$  and also
- xi) closed sets in  $(X, \tau_2)$  are  $X, \phi, \{c, d\}, \{a, b\}$ .
- xii) ws-closed sets in  $(X, \tau_2)$  are  $X, \phi, \{a, b\}, \{c, d\}$ .
- xiii) g-closed sets in  $(X, \tau_2)$  are  $X, \phi, \{a\}, \{b\}, \{c\}, \{d\}, \{a, b\}, \{a, c\}, \{a, d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{a, b, d\}, \{a, c, d\}, \{b, c, d\}.$
- xiv) sg- closed sets in  $(X, \tau_2)$  are  $X, \phi, \{a\}, \{b\}, \{c\}, \{d\}, \{a, b\}, \{a, c\}, \{a, d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{a, b, d\}, \{a, c, d\}, \{b, c, d\}.$
- xv)  $g\alpha$  closed sets in  $(X, \tau_2)$  are  $X, \phi, \{a\}, \{b\}, \{c\}, \{d\}, \{a, b\}, \{a, c\}, \{a, d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{a, b, d\}, \{a, c, d\}, \{b, c, d\}.$
- xvi) sgb -closed sets in  $(X, \tau_2)$  are  $X, \phi, \{a\}, \{b\}, \{c\}, \{d\}, \{a, b\}, \{a, c\}, \{a, d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{a, b, d\}, \{a, c, d\}, \{b, c, d\}.$
- xvii) rg\*b- closed sets in  $(X, \tau_2)$  are  $X, \phi, \{a\}, \{b\}, \{c\}, \{d\}, \{a, c\}, \{a, d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{a, b, d\}, \{a, c, d\}, \{b, c, d\}.$
- xviii) pgpr- closed sets in  $(X, \tau_2)$  are  $X, \phi, \{a\}, \{b\}, \{c\}, \{d\}, \{a, b\}, \{a, c\}, \{a, d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{a, b, d\}, \{a, c, d\}, \{b, c, d\}.$
- xix) gab- closed sets in  $(X, \tau_2)$  are  $X, \phi, \{a\}, \{b\}, \{c\}, \{d\}, \{a, b\}, \{a, c\}, \{a, d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{a, b, d\}, \{a, c, d\}, \{b, c, d\}.$
- xx) rps- closed sets in  $(X, \tau_2)$  are  $X, \phi, \{a\}, \{b\}, \{c\}, \{d\}, \{a, c\}, \{a, d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{a, b, d\}, \{a, c, d\}, \{b, c, d\}.$

Therefore {a} is ws-closed set in  $(X, \tau_1)$  but not g-closed (resp. sg-closed, ga-closed, sgb-closed sets, rg\*b-closed, pgpr-closed, gab-closed, pgb-closed) set in  $(X, \tau_1)$ .

Meanwhile {a} is g-closed (resp. sg-closed, ga-closed, sgb-closed, rg\*b-closed, pgpr-closed, gab-closed, rps-closed) set in  $(X, \tau_2)$  but not ws-closed set in  $(X, \tau_2)$ .

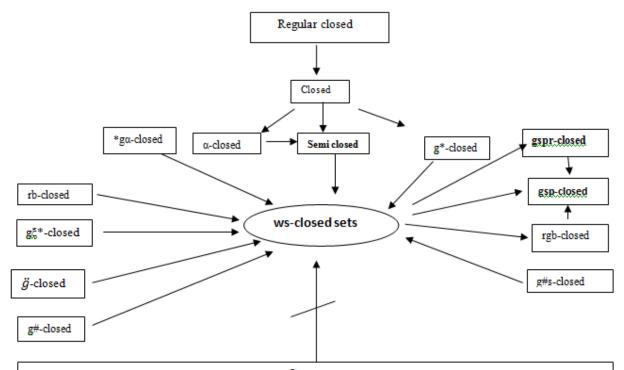
**Remark 3.20:** The following Example 3.21, shows that ws-closed sets are independent of R\*-closed[15] sets,  $rg\beta$ -closed[26] sets,  $pgr\alpha$ -closed[5] sets, rgw-closed[29] sets and gprw-closed[30] sets.

**Example 3.21:** Let  $X = \{a, b, c\}, \tau = \{X, \phi, \{a\}, \{b\}, \{a, b\}\}.$  Then

- i) closed sets in  $(X, \tau)$  are  $X, \phi, \{c\}, \{a, c\}, \{b, c\}$ .
- ii) ws-closed sets in  $(X, \tau)$  are  $X, \phi, \{a\}, \{b\}, \{c\}, \{b, c\}, \{a, c\}.$
- iii) R\* -closed sets in (X,  $\tau$ ) are X,  $\phi$ ,{c},{a, b},{b, c},{a, c}.
- iv) rg $\beta$  -closed sets in  $(X, \tau)$  are  $X, \phi, \{c\}, \{a, b\}, \{b, c\}, \{a, c\}$ .
- v) pgr $\alpha$  closed sets in  $(X, \tau)$  are  $X, \phi, \{c\}, \{a, b\}, \{b, c\}, \{a, c\}$
- vi) rgw- closed sets in  $(X, \tau)$  are  $X, \phi, \{c\}, \{a, b\}, \{b, c\}, \{a, c\}$
- vii) gprw -closed sets in  $(X, \tau)$  are  $X, \phi, \{c\}, \{a, b\}, \{b, c\}, \{a, c\}$

Therefore  $\{a\}$  is ws-closed set in X but not  $R^*$ -closed (resp.  $rg\beta$ - closed,  $pgr\alpha$ -closed, rgw-closed, gprw-closed) set in X.

**Remark 3.22**: From the above discussion and results we have the following implications.



rg-closed, gpr-closed, wgra-closed, pgra-closed,  $\widehat{rg}$ -closed,  $\alpha^**g$ -closed, gprw-closed, rgw-closed, rw-closed, rwg-closed, ggra-closed, gwa\*-closed,  $\beta$ -closed,  $\beta$ -cl

A \_\_\_\_\_ B means A implies B, but converse is not true.

 $A \longrightarrow B$  means A and B are independent of each other

**Theorem 3.23:** The intersection of two ws-closed subsets of X is ws-closed set in X.

**Proof:** Let A and B be are ws-closed sets in X. Let U be any semiopen set in X such that  $(A \cap B) \subseteq U$  that is  $A \subseteq U$  and  $B \subseteq U$ . Since A and B are ws-closed sets then  $scl(A) \subseteq U$  and  $scl(B) \subseteq U$  and we know that  $(scl(A) \cap scl(B)) = scl(A \cap B) \subseteq U$ . Therefore  $A \cap B$  is ws-closed set in X.

Remark 3.24: The union of two ws-closed sets in X is generally not a ws-closed set in X.

**Example 3.25:** Let  $X = \{a, b, c\}$  and  $\tau = \{\phi, X, \{a\}, \{b\}, \{a, b\}\}$  then the sets  $A = \{a\}$  and  $B = \{b\}$  are ws-closed sets in X but  $A \cup B = \{a, b\}$  is not a ws-closed set in X.

**Theorem 3.26:** If a subset A of a topological space X is ws-closed set in X then scl(A)-A does not contain any non-empty open set in X but converse is not true.

**Proof:** Let A is an ws-closed set in X and suppose F be an non empty w-closed subset of scl(A)-A.

 $F \subseteq scl(A) - A \Longrightarrow F \subseteq scl(A) \cap (X - A) \Longrightarrow F \subseteq scl(A) \longrightarrow (1) \& F \subseteq X - A$ 

- $\implies$  A $\subseteq$ X-F and X-F is w-open set and A is a ws-closed set, scl(A) $\subseteq$ X-F
- $\Longrightarrow$  F $\subseteq$ X-scl(A) $\longrightarrow$ (2) from equations (1) and (2) we get F $\subseteq$ scl(A) $\cap$ (X-scl(A))= $\phi$
- $\Rightarrow$  F= $\Phi$  thus scl(A)-A does not contain any non-empty w-closed set in X.

**Remark 3.27:** The converse of the above Theorem need not be true as seen from the following Example 3.28.

**Example 3.28:** Let  $X = \{a, b, c, d\}$   $\tau = \{X, \phi, \{a\}, \{a, b\}, \{a, b, c\}\}$  then the set  $A = \{b\}$  scl $\{b\} = \{b\}$ , scl $\{A\}$ - $A = \{b\}$  does not contain any non-empty w-closed set in X but A is not ws-closed set.

**Theorem 3.29:** If A is a ws-closed set in X and  $A \subseteq B \subseteq scl(A)$  then B is also ws-closed set in X.

**Proof:** Let A be a ws-closed set in X such that  $B\subseteq scl(A)$ . Let U be a w-open set of X such that  $B\subseteq U$  then  $A\subseteq U$ . Since A is ws-closed set, we have  $scl(A)\subseteq U$  and  $A\subseteq U$ . Now  $B\subseteq scl(A) \Longrightarrow scl(B)\subseteq scl(scl(A))=scl(A)\subseteq U$ . That is  $scl(B)\subseteq U$ . Therefore B is a ws-closed set in X.

**Remark 3.30:** The converse of the above Theorem 3.29 is need not be true as seen from the following Example 3.31.

**Example 3.31:** Let  $X = \{a, b, c\}$ ,  $\tau = \{\phi, X, \{a\}, \{b\}, \{a, b\}\}$ , then the set  $A = \{a\}$ ,  $B = \{a, c\}$  such that A and B are wsclosed sets in X but  $A \subset B \nsubseteq scl(A)$  because  $scl(A) = \{a\}$ .

**Theorem 3.32:** Let  $(X,\tau)$  be a topological space then for each  $x \in X$  the set  $X - \{x\}$  is ws-closed or semi open.

**Proof:** Let  $x \in X$ . Suppose  $X - \{x\}$  is not a semiopen set. Then X is the only semiopen set containing  $X - \{x\}$ , that is  $X - \{x\} \subseteq X \implies cl(X - \{x\}) \subseteq cl(X) \implies cl(X - \{x\}) \subseteq X$ . Therefore  $X - \{x\}$  is ws-closed set in X.

**Theorem 3.33:** Let X and Y are topological spees and  $A \subseteq Y \subseteq X$ . Suppose that A is ws-closed set in X then A is ws-closed relative to Y.

**Proof:** Let  $A \subseteq Y \cap G$ , where G is a w-open. Since A is a ws-closed set in X, then  $A \subseteq G$  and  $scl(A) \subseteq G$ . This implies that  $Y \cap scl(A) \subseteq Y \cap G$  where  $Y \cap scl(A)$  is closed set of A in Y. Thus A is a ws-closed relative to Y.

**Theorem 3.34:** In a topological space X if  $SO(X) = \{X, \phi\}$  then every subset of X is a ws-closed set.

**Proof:** Let X be a topological space and  $SO(X) = \{X, \phi\}$ . Let A be any subset of X. Suppose  $A = \phi$ . Then  $\phi$  is ws-closed set. Suppose  $A \neq \phi$ . Then X is the only semiopen set containing A and so  $scl(A) \subseteq X$ . Hence A is a ws-closed set in X.

**Remark 3.35:** The converse of the above Theorem need not be true in general as seen from the following Example 3.36..

**Example 3.36:** Let  $X = \{a, b, c\}, \tau = \{\phi, X, \{a\}, \{b, c\}\}.$  Then every subset of  $(X,\tau)$  is a ws-closed set in X but  $SO=\{\phi, X, \{a\}, \{b, c\}\}.$ 

**Theorem 3.37:** If A is regular open and gspr-closed set in X then A is ws-closed set in X.

**Proof:** Let A be a regular open and gspr-closed set in X. Let U be any w-open set in X such that  $A \subseteq U$ . Since A is regular open and gspr-closed set in X, by definition,  $scl(A) \subseteq A$  then  $scl(A) \subseteq A \subseteq U$ . Hence A is ws-closed set in X.

**Theorem 3.38:** If A is regular open and rgb-closed set then A is ws-closed set in X.

**Proof:** Let A be a regular open and rgb-closed in X. Let U be any w-open set in X such that  $A \subseteq U$ . Since A is regular open and rgb-closed in X, by definition,  $scl(A) \subseteq A$  then  $scl(A) \subseteq A \subseteq U$ . Hence A is ws-closed set in X.

**Theorem 3.39:** If A is semiopen and swg\*-closed then A is ws-closed set in X.

**Proof:** Let A be a semiopen and swg\*-closed in X. Let U be any w- open set in X such that  $A \subseteq U$ . Since A is semiopen and swg\*-closed in X, by definition,  $scl(A) \subseteq A$  then  $scl(A) \subseteq A \subseteq U$ . Hence A is ws-closed set in X.

**Theorem 3.40:** If A is semiopen and swg-closed then A is ws-closed set in X.

**Proof:** Let A be a semiopen and swg-closed in X. Let U be any w- open set in X such that  $A \subseteq U$ . Since A is semiopen and swg-closed in X, by definition,  $scl(A) \subseteq A \subseteq U$ . Hence A is ws-closed set in X.

**Theorem 3.41:** If A is semiopen and sg-closed then A is ws-closed set in X.

**Proof:** Let A be a semiopen and sg-closed in X. Let U be any w- open set in X such that  $A \subseteq U$ . Since A is semiopen and sg-closed in X, by definition,  $scl(A) \subseteq A$  then  $scl(A) \subseteq A \subseteq U$ . Hence A is ws-closed set in X.

**Theorem 3.42:** If A is semiopen and sgb-closed then A is ws-closed set in X.

**Proof:** Let A be a semiopen and sgb-closed in X. Let U be any w- open set in X such that  $A \subseteq U$ . Since A is semiopen and sgb-closed in X, by definition,  $scl(A) \subseteq A$  then  $scl(A) \subseteq A \subseteq U$ . Hence A is ws-closed set in X.

**Theorem 3.43:** If A is semiopen and αgs-closed then A is ws-closed set in X.

**Proof:** Let A be a semiopen and  $\alpha gs$  -closed in X. Let U be any w- open set in X such that A $\subseteq$ U. Since A is semiopen and  $\alpha gs$  -closed in X, by definition,  $scl(A)\subseteq A$  then  $scl(A)\subseteq A\subseteq U$ . Hence A is ws-closed set in X.

**Theorem 3.44:** If A is  $\beta$ -open and  $\beta$ wg\*-closed then A is ws-closed set in X.

**Proof:** Let A be a  $\beta$ -open and  $\beta$ wg\*-closed in X. Let U be any regular semiopen set in X such that A $\subseteq$ U. Since A is  $\beta$ -open and  $\beta$ wg\*-closed in X, by definition, gcl(A) $\subseteq$ A then gcl(A) $\subseteq$ A $\subseteq$ U. Hence A is ws-closed set in X.

**Theorem 3.45:** If A is both open and g-closed then A is ws-closed set in X.

**Proof:** Let A be open and g-closed set in X. Let U be any regular open set in X such that  $A \subseteq U$ . By definition,  $cl(A) \subseteq A \subseteq U$  and gcl(A) = A. This implies that  $cl(A) \subseteq gcl(A) \subseteq A \subseteq U \Longrightarrow gcl(A) \subseteq U$ . Hence A is ws-closed set.

**Theorem 3.46:** If A is regular semiopen and rw-closed then A is ws-closed set in X.

**Proof:** Let A be a regular semiopen and rw-closed set in X. Let U be any w-open set in X such that  $A \subseteq U$ . Now  $A \subseteq A$  by hypothesis  $cl(A) \subseteq A$  then we know that  $cl(A) \subseteq scl(A) \subseteq A$ . Hence  $scl(A) \subseteq U$  therefore A is ws-closed set in X.

**Theorem 3.47:** If A is regular semiopen and R\*-closed then A is ws-closed set in X.

**Proof:** Let A be a regular semiopen and R\*-closed set in X. Let U be any w-open set in X such that  $A \subseteq U$ . Now  $A \subseteq A$  by hypothesis  $cl(A) \subseteq A$  then we know that  $cl(A) \subseteq scl(A) \subseteq A$ . Hence  $scl(A) \subseteq U$  therefore A is ws-closed set in X.

**Theorem 3.48:** If A is regular semiopen and gprw-closed then A is ws-closed set in X.

**Proof:** Let A be a regular semiopen and gprw -closed set in X. Let U be any w-open set in X such that  $A \subseteq U$ . Now  $A \subseteq A$  by hypothesis  $cl(A) \subseteq A$  then we know that  $cl(A) \subseteq scl(A) \subseteq A$ . Hence  $scl(A) \subseteq U$  therefore A is ws-closed set in X.

**Theorem 3.49:** If A is regular semiopen and rgw-closed then A is ws-closed set in X.

**Proof:** Let A be a regular semiopen and rgw -closed set in X. Let U be any w-open set in X such that  $A \subseteq U$ . Now  $A \subseteq A$  by hypothesis  $cl(A) \subset A$  then we know that  $cl(A) \subset scl(A) \subset A$ . Hence  $scl(A) \subset U$  therefore A is ws-closed set in X.

#### REFERENCES

- M.Anitha and P.Thangavelu, On Pre-Generalized pre-regular closed sets, Acta Ciencia Indica, 31M(4)(2005), 1035 – 1040
- 2. S.S. Benchalli and R.S. Wali, On RW-closed sets in topological spaces, Malays. Math. sci. Soc. 30 (2007), 99-
- 3. S. S. Benchalli, P. G. Patil and P. M. Nalwad. Genaralized ωα-Closed sets is Topological Spaces, The journal of new results in science Number: 7, Year: 2014, Pages: 7-19.
- 4. P.Bhattacharyya and B.K.Lahiri, Semi-generalized closed sets in topology, Indian J. Math., 29 (1987), 376-382.
- 5. K. Binoy Balan and C. Janaki, On pgrα closed sets in topological spaces, IJMA-3(5), 2012, 2114-2121.
- 6. R.Devi, H.Maki and V.Kokilavani, The Group Structure of #gα-Closed Sets in Topological Spaces. International Journal of general topology, 2(1), 21-30
- 7. C. Dhanapakyam , J. Subashini and K. Indirani, ON  $\beta$ wg\* set and continuity in topological spaces, IJMA-5(5), 2014, 222-233
- 8. J.Dontchev, On generalized semi-preopen sets, Mem. Fac. Sci. Kochi Univ. Ser.A. Math., 16(1995), 35-48.
- 9. Y.Gnanambal, On generalized pre-regular closed sets in topological spaces, Indian J. Pure Appl. Math., 28 (1997), 351-360.
- 10. Govindappa Navalagi and Chandrashekarappa, On gspr closed sets in topological spaces International Journal of Mathematics and Computing Applications, Vol. 2, Nos 1-2, (2010), pp. 51-58
- 11. Govindappa Navalagi, S.V. Gurushantanavar, and Chandrashekarappa A.S, ON  $\alpha$  Generalized preclosed sets in topological spaces, International Journal of Mathematics and Computing Applications, Vol. 2, Nos 1-2, January-December 2010, pp. 35-44
- 12. K Indirani and G Sindhu, On Regular Generalized Star B closed sets, IJMA. International Journal of general topology, 2(1) (2009), 21-30.
- 13. D.Iyappan and N.Nagaveni,On semi generalized b-closed set, Nat. Sem. On Math and Comp. Sci,,(2010) Proc.6.

- 14. S. Jafari, T. Noiri, N.rajesh and M.L. Thivagar, Another generalization of closed sets, KOCHI j. Math, 3, 25-38, 2008.
- 15. C. Janaki and Renu Thomas, On R\* closed sets in topological space s, IJMA-3(8), 2012, 3067-3074.
- 16. A. Jayalakshmi & C. Janaki, On wgrα-Closed Sets in Topological Spaces, International Journal of Mathematical Archive-3(6), 2012, 2386-2392
- 17. V.Kokilavani, M.Myvizhi and M.Vivek Prabu, Generalized  $\zeta$  \* -closed sets in topological spaces, International journal of mathematical archive, 4(5)(2013), 274-279.
- 18. N.Levine, Generalized closed sets in topology, Rend. Circ. Mat. Palermo, 19(2) (1970), 89-96.
- 19. N.Levine, Semi-open sets and semi-continuity in topological spaces, Amer. Math. Monthly, 70(1963), 36-41.
- 20. H.Maki, R.Devi and K.Balachandran, Associated topologies of generalized  $\alpha$ -closed sets and  $\alpha$ -generalized closed sets, Mem. Fac. Sci. Kochi Univ. Ser. A. Math., 15 (1994), 51-63.
- 21. H.Maki, R.Devi and K.Balachandran, Generalized  $\alpha$ -closed sets in topology, Bull. Fukuoka Univ. Ed. Part III, 42(1993), 13-21.
- 22. K. Mariappa, S. Sekar, On Regular Generalized b Closed Set, Int. Journal of Math. Analysis, Vol. 7, 2013, no. 13,613-624.
- 23. C. Mukundhan and N. Nagaveni, A Weaker Form of a Generalized Closed Set, Int. J. Contemp. Math. Sciences, Vol. 6, 2011, no. 20, 949 961
- 24. A. Narmadha, N. Nagaveni and T. Noiri, On Regular b-Open Sets in Topological Spaces Int. Journal of Math. Analysis, Vol. 7, 2013, no. 19, 937 948
- 25. N.Palaniappan and K.C.Rao, Regular generalized closed sets, Kyungpook, Math. J., 33 (1993), 211-219.
- 26. Y.Palaniappan, On regular generalised β-closed sets, International Journal of Scientific & Engineering Research, Volume 4, Issue 4, April-2013 1410.
- 27. R. Parimelazhagan and V. Subramonia Pillai, "Strongly g\* closed sets in topological spaces", Int. Journal of Math. Analysis, Vol. 6, 2012, no. 30, 1481-1489.
- 28. S. Pious Missier, K. Ali, and A. Subramanian, "g#p# Closed Sets in Topological Spaces", International Journal of Mathematical Archive, 4 (1) (2013) 176-181.
- 29. Sanjay Mishra, Nitin Bhardwaj and Varun Joshi, On Regular Generalized weakly (rgw)-Closed Sets in Topological Spaces, Int. Journal of Math. Analysis, Vol. 6, 2012, no. 39, 1939 1952
- 30. Sanjay Mishra, Nitin Bhardwaj and Varun Joshi, On Generalized Pre Regular Weakly (gprw)-Closed Sets in Topological Spaces, International Mathematical Forum, Vol. 7, 2012, no. 40, 1981 1992
- 31. Savithiri D and Janaki C, .On Regular ^Generalized closed sets in topological spaces International Journal of Mathematical Archive-4(4), 2013, 162-169
- 32. Sharmistha Bhattacharya, On Generalized Regular Closed Sets, Int. J. Contemp. Math. Sciences, Vol. 6, 2011, no. 3, 145 152.
- 33. M.Sheik John, On w-closed sets in Topology, Acta Ciencia Indica, 4 (2000), 389-392.
- 34. T. Shyla Isac Mary and P. Thangavelu, On Regular Pre-Semiclosed sets in topological spaces, KBM J. Of Math. Sci and Comp. Applications (1), 9-17
- 35. Subashini jesu rajan, On βwg\*\* set and Continuity in Topological Spaces, International journal of computing, Vol 4 Issue 3, July 2014.
- 36. A. Vadivel and K. Vairamanickam, rgα-Closed Sets and rgα-Open Sets in Topological Spaces, Int. Journal of Math. Analysis, Vol. 3, 2009, no. 37, 1803 1819.
- 37. M.K.R.S. Veera kumar, g#-closed sets in topological spaces, Mem. Fac. Sci. Kochi Univ. Ser. A. Math 24(2003), 1-13.
- 38. M.K.R.S. Veera Kumar, On  $g^{\Lambda}$  closed sets in topological spaces, Bulletin Allahabad Math. Soc.18(2003), 99-112
- 39. M. K. R. S. Veerakumar, g\*-pre closed sets Acta Ciencia Indica (Mathematics) Meerut,
- 40. Veerakumar M.K.R.S, g# semi-closed sets in topological spaces. International Journal of Scientific&Research Publications, Vol 2, Issue 6, June 2012 ISSN 2250-3153.
- 41. M. Vigneshwaran and A. Singaravelan, Applications of \*\* $g\alpha$ -closed sets in Topological Spaces, IJMA-5(10), 2014, 139-150
- 42. L. Vinayagamoorthi, N.Nagaveni, On Generalized-αb closed sets, Proceeding ICMD Allahabad, Puspha Publication Vol.1. 2010-11.Vol.3, No.3, (2013), 55-60

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