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A STUDY ON (T, S)-INTUITIONISTIC FUZZY SUBNEARRINGS OF A NEARRING

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ABSTRACT

In this paper, we made an attempt to study the algebraic nature of a (T, S)-intuitionistic fuzzy subnearring of a nearring.

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Key Words: T-fuzzy subnearring, anti S-fuzzy subnearring, (T, S)-intuitionistic fuzzy subnearring, product.

INTRODUCTION

After the introduction of fuzzy sets by L.A.Zadeh[16], several researchers explored on the generalization of the concept of fuzzy sets. The concept of intuitionistic fuzzy subset was introduced by K.T.Atanassov[4, 5], as a generalization of the notion of fuzzy set. Azriel Rosenfeld[6] defined the fuzzy groups. Asok Kumer Ray[3] defined a product of fuzzy subgroups. The notion of homomorphism and anti-homomorphism of fuzzy and anti-fuzzy ideal of a ring was introduced by N.Palaniappan & K.Arjunan [13, 14]. In this paper, we introduce the some Theorems in (T, S)-intuitionistic fuzzy subnearring of a nearring.

1.PRELIMINARIES:

- **1.1 Definition:** A (T, S)-norm is a binary operations T: $[0, 1] \times [0, 1] \to [0, 1]$ and S: $[0, 1] \times [0, 1] \to [0, 1]$ satisfying the following requirements;
- (i) T(0, x)=0, T(1, x)=x (boundary condition)
- (ii) T(x, y) = T(y, x) (commutativity)
- (iii) T(x, T(y, z))=T(T(x,y), z)(associativity)
- (iv) if $x \le y$ and $w \le z$, then $T(x, w) \le T(y, z)$ (monotonicity).
- (v) S(0, x) = x, S(1, x) = 1 (boundary condition)
- (vi) S(x, y) = S(y, x)(commutativity)
- (vii) S(x, S(y, z)) = S(S(x, y), z) (associativity)
- (viii) if $x \le y$ and $w \le z$, then $S(x, w) \le S(y, z)$ (monotonicity).
- **1.2 Definition:** Let (R, +, .) be a nearring. A fuzzy subset A of R is said to be a T-fuzzy subnearring (fuzzy subnearring with respect to T-norm) of R if it satisfies the following conditions:
- (i) $\mu_A(x-y) \ge T(\ \mu_A(x),\ \mu_A(y))$
- (ii) $\mu_A(xy) \ge T(\ \mu_A(x),\ \mu_A(y))$ for all x and y in R.
- **1.3 Definition:** Let (R, +, .) be a nearring. An intuitionistic fuzzy subset A of R is said to be an (T, S)-intuitionistic fuzzy subnearring (intuitionistic fuzzy subnearring with respect to (T, S)-norm) of R if it satisfies the following conditions:
- $(i) \quad \ \mu_A(x-y) \geq T \; (\mu_A(x), \, \mu_A(y))$
- (ii) $\mu_A(xy) \ge T(\mu_A(x), \mu_A(y))$
- (iii) $v_A(x-y) \leq S(v_A(x), v_A(y))$
- (iv) $v_A(xy) \le S(v_A(x), v_A(y))$ for all x and y in R.

- **1.4 Definition:** Let A and B be intuitionistic fuzzy subsets of sets G and H, respectively. The product of A and B, denoted by A×B, is defined as A×B = { $\langle (x, y), \mu_{A\times B}(x, y), \nu_{A\times B}(x, y) \rangle$ / for all x in G and y in H}, where $\mu_{A\times B}(x, y) = \min\{\mu_A(x), \mu_B(y)\}$ and $\nu_{A\times B}(x, y) = \max\{\nu_A(x), \nu_B(y)\}$.
- **1.5 Definition:** Let A be an intuitionistic fuzzy subset in a set S, the strongest intuitionistic fuzzy relation on S, that is an intuitionistic fuzzy relation on A is V given by $\mu_V(x, y) = \min\{\mu_A(x), \mu_A(y)\}$ and $\nu_V(x, y) = \max\{\nu_A(x), \nu_A(y)\}$ for all x and y in S.
- **1.6 Definition:** Let (R, +, .) and $(R^1, +, .)$ be any two nearrings. Let $f : R \to R^1$ be any function and A be an (T, S)-intuitionistic fuzzy subnearring in R, V be an (T, S)-intuitionistic fuzzy subnearring in $f(R) = R^1$, defined by $\mu_V(y) = \sup_{x \in f^{-1}(y)} \mu_A(x)$ and $\nu_V(y) = \inf_{x \in f^{-1}(y)} \nu_A(x)$ for all x in R and y in R^1 . Then A is called a preimage of V under f and is denoted by $f^{-1}(V)$.
- **1.7 Definition:** Let A be an (T, S)-intuitionistic fuzzy subnearring of a nearring (R, +, ·) and a in R. Then the pseudo (T, S)-intuitionistic fuzzy coset $(aA)^p$ is defined by $((a\mu_A)^p)(x) = p(a)\mu_A(x)$ and $((a\nu_A)^p)(x) = p(a)\nu_A(x)$ for every x in R and for some p in P.

2- PROPERTIES

2.1 Theorem: Intersection of any two (T, S)-intuitionistic fuzzy subnearrings of a nearring R is a (T, S)-intuitionistic fuzzy subnearring of a nearring R.

Proof: Let A and B be any two (T, S)-intuitionistic fuzzy subnearrings of a nearring R and x and y in R. Let $A = \{(x, \mu_A(x), \nu_A(x)) \mid x \in R\}$ and $B = \{(x, \mu_B(x), \nu_B(x)) \mid x \in R\}$ and also let $C = A \cap B = \{(x, \mu_C(x), \nu_C(x)) \mid x \in R\}$ where $\min\{\mu_A(x), \mu_B(x)\} = \mu_C(x)$ and $\max\{\nu_A(x), \nu_B(x)\} = \nu_C(x)$. Now $\mu_C(x-y) = \min\{\mu_A(x-y), \mu_B(x-y)\} \geq \min\{T(\mu_A(x), \mu_A(y)), T(\mu_B(x), \mu_B(y))\} \geq T(\min\{\mu_A(x), \mu_B(x)\}, \min\{\mu_A(y), \mu_B(y)\}) = T(\mu_C(x), \mu_C(y))$. Therefore $\mu_C(x-y) \geq T(\mu_C(x), \mu_C(y))$ for all x and y in R. And $\mu_C(xy) = \min\{\mu_A(xy), \mu_B(xy)\} \geq \min\{T(\mu_A(x), \mu_A(y)), T(\mu_B(x), \mu_B(y))\} \geq T(\min\{\mu_A(x), \mu_B(x)\}, \min\{\mu_A(y), \mu_B(y)\}) = T(\mu_C(x), \mu_C(y))$. Therefore $\mu_C(xy) \geq T(\mu_C(x), \mu_C(y))$ for all x and y in R. Now $\nu_C(x-y) = \max\{\nu_A(x-y), \nu_B(x-y)\} \leq \max\{S(\nu_A(x), \nu_A(y)), S(\nu_B(x), \nu_B(y))\} \leq S(\max\{\nu_A(x), \nu_B(x)\}, \max\{\nu_A(y), \nu_B(y)\}) = S(\nu_C(x), \nu_C(y))$. Therefore $\nu_C(x-y) \leq S(\nu_C(x), \nu_C(y))$ for all x and y in R. And $\nu_C(xy) = \max\{\nu_A(xy), \nu_B(xy)\} \leq \max\{S(\nu_A(x), \nu_B(y))\} \leq S(\max\{\nu_A(x), \nu_B(y)\}) = S(\nu_C(x), \nu_C(y))$. Therefore $\nu_C(x-y) \leq S(\nu_C(x), \nu_C(y))$ for all x and y in R. And $\nu_C(xy) = \max\{\nu_A(xy), \nu_B(xy)\} \leq \max\{S(\nu_A(x), \nu_B(y))\} \leq S(\max\{\nu_A(x), \nu_B(y)\}) = S(\nu_C(x), \nu_C(y))$. Therefore $\nu_C(x-y) \leq S(\nu_C(x), \nu_C(y))$ for all x and y in R. Therefore C is an $\nu_A(x) = \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{j=1}^{$

2.2 Theorem: The intersection of a family of (T, S)-intuitionistic fuzzy subnearrings of nearring R is an (T, S)-intuitionistic fuzzy subnearring of a nearring R.

Proof: It is trivial.

2.3 Theorem: If A and B are any two (T, S)-intuitionistic fuzzy subnearrings of the nearrings R_1 and R_2 respectively, then $A \times B$ is an (T, S)-intuitionistic fuzzy subnearring of $R_1 \times R_2$.

Proof: Let A and B be two (T, S)-intuitionistic fuzzy subnearrings of the nearrings R₁ and R₂ respectively. Let x₁ and x₂ be in R₁, y₁ and y₂ be in R₂. Then (x₁, y₁) and (x₂, y₂) are in R₁×R₂. Now $μ_{A×B}[(x₁, y₁)-(x₂, y₂)] = μ_{A×B}(x₁-x₂, y₁-y₂) = min {μ_A(x₁-x₂), μ_B(y₁-y₂)} ≥ min{T(μ_A(x₁), μ_A(x₂)), T(μ_B(y₁), μ_B(y₂))} ≥ T(min{μ_A(x₁), μ_B(y₁)}, min{μ_A(x₂), μ_B(y₂)}) = T(μ_{A×B}(x₁, y₁), μ_{A×B}(x₂, y₂)). Therefore <math>μ_{A×B}[(x₁, y₁) - (x₂, y₂)] ≥ T(μ_{A×B}(x₁, y₁), μ_{A×B}(x₂, y₂))$. Also $μ_{A×B}[(x₁, y₁) (x₂, y₂)] = μ_{A×B}(x₁x₂, y₁y₂) = min{μ_A(x₁x₂), μ_B(y₁y₂)} ≥ min {T(μ_A(x₁), μ_A(x₂)), T(μ_B(y₁), μ_B(y₂))} ≥ T(min {μ_A(x₁), μ_B(y₁)}, min {μ_A(x₂), μ_B(y₂)}) ≥ T(min {μ_A(x₁), μ_A(x₂)}, T(μ_B(y₁), μ_B(y₂))} ≥ T(min {μ_A(x₁), μ_B(y₁)}, min {μ_A(x₂), μ_B(y₂)}) = T(μ_{A×B}(x₁, y₁), μ_{A×B}(x₂, y₂))$. Therefore $μ_{A×B}[(x₁, y₁)(x₂, y₂)] ≥ T(μ_{A×B}(x₁, y₁), μ_{A×B}(x₂, y₂))$. Now $ν_{A×B}[(x₁, y₁) - (x₂, y₂)] = ν_{A×B}(x₁-x₂, y₁-y₂) = max{ν_A(x₁-x₂), ν_B(y₁-y₂)} ≤ max {S(ν_A(x₁), ν_A(x₂)), S(ν_B(y₁), ν_B(y₂)} = S(ν_{A×B}(x₁, y₁), ν_{A×B}(x₂, y₂))$. Therefore $ν_{A×B}[(x₁, y₁) - (x₂, y₂)] ≤ S(ν_{A×B}(x₁, y₁), ν_{A×B}(x₂, y₂))$. Also $ν_{A×B}[(x₁, y₁)(x₂, y₂)] = ν_{A×B}(x₁x₂, y₁y₂) = max {ν_A(x₁x₂), ν_B(y₁y₂)} ≤ max {S(ν_A(x₁), ν_A(x₂)), S(ν_B(y₁), ν_B(y₂))} ≤ S(max {ν_A(x₁), ν_B(y₁)}, max{ν_A(x₂), ν_B(y₁)}, max{ν_A(x₂), ν_B(y₁)}, max{ν_A(x₂), ν_B(y₂)}) = S(ν_{A×B}(x₁, y₁), ν_{A×B}(x₂, y₂))$. Therefore $ν_{A×B}[(x₁, y₁) - (x₂, y₂)] ≤ S(ν_{A×B}(x₁, y₁), ν_{A×B}(x₂, y₂))$. Also $ν_{A×B}[(x₁, y₁) - (x₂, y₂)] = ν_{A×B}(x₁x₂, y₁y₂) = max {ν_A(x₁x₂), ν_B(y₂)} ≤ S(ν_{A×B}(x₁, y₁), ν_{A×B}(x₂, y₂))$. Also $ν_{A×B}[(x₁, y₁) - (x₂, y₂)] ≤ S(ν_{A×B}(x₁, y₁), ν_{A×B}(x₂, y₂))$. Hence A×B is an (T, S)-intuitionistic fuzzy subnearring of nearring of nearr

2.4 Theorem: If A is a (T, S)-intuitionistic fuzzy subnearring of a nearring $(R, +, \cdot)$, then $\mu_A(x) \le \mu_A(0)$ and $\nu_A(x) \ge \nu_A(0)$ for x in R, the identity element 0 in R.

Proof: For x in R and 0 is the identity element of R. Now $\mu_A(0) = \mu_A(x-x) \ge T(\ \mu_A(x),\ \mu_A(x)) \ge \mu_A(x)$ for all x in R. So $\mu_A(x) \le \mu_A(0)$. And $\nu_A(0) = \nu_A(x-x) \le S(\ \nu_A(x),\ \nu_A(x)) \le \nu_A(x)$ for all x in R. So $\nu_A(x) \ge \nu_A(0)$.

2.5 Theorem: Let A and B be (T, S)-intuitionistic fuzzy subnearring of the nearrings R_1 and R_2 respectively. Suppose that 0 and 0_1 are the identity element of R_1 and R_2 respectively. If $A \times B$ is an (T, S)-intuitionistic fuzzy subnearring of $R_1 \times R_2$, then at least one of the following two statements must hold. (i) $\mu_B(0_1) \ge \mu_A(x)$ and $\nu_B(0_1) \le \nu_A(x)$ for all x in R_1 (ii) $\mu_A(0) \ge \mu_B(y)$ and $\nu_A(0) \le \nu_B(y)$ for all y in R_2 .

Proof: Let A×B be an (T, S)-intuitionistic fuzzy subnearring of $R_1 \times R_2$. By contraposition, suppose that none of the statements (i) and (ii) holds. Then we can find a in R_1 and b in R_2 such that $\mu_A(a) > \mu_B(0_l)$, $\nu_A(a) < \nu_B(0_l)$ and $\mu_B(b) > \mu_A(0)$, $\nu_B(b) < \nu_A(0)$. We have $\mu_{A\times B}(a, b) = \min\{\mu_A(a), \mu_B(b)\} > \min\{\mu_B(0_l), \mu_A(0)\} = \min\{\mu_A(0), \mu_B(0_l)\} = \mu_{A\times B}(0, 0_l)$. And $\nu_{A\times B}(a, b) = \max\{\nu_A(a), \nu_B(b)\} < \max\{\nu_B(0_l), \nu_A(0)\} = \max\{\nu_A(0), \nu_B(0_l)\} = \nu_{A\times B}(0, 0_l)$. Thus A×B is not an (T, S)-intuitionistic fuzzy subnearring of $R_1 \times R_2$. Hence either $\mu_B(0_l) \ge \mu_A(x)$ and $\nu_B(0_l) \le \nu_A(x)$ for all x in R_1 or $\mu_A(0) \ge \mu_B(y)$ and $\nu_A(0) \le \nu_B(y)$ for all y in R_2 .

- **2.6 Theorem:** Let A and B be two intuitionistic fuzzy subsets of the nearrings R_1 and R_2 respectively and $A \times B$ is an (T, S)-intuitionistic fuzzy subnearring of $R_1 \times R_2$. Then the following are true:
- (i) if $\mu_A(x) \le \mu_B(0_1)$ and $\nu_A(x) \ge \nu_B(0_1)$, then A is an (T, S)-intuitionistic fuzzy subnearring of R_1 .
- (ii) if $\mu_B(x) \le \mu_A(0)$ and $\nu_B(x) \ge \nu_A(0)$, then B is an (T, S)-intuitionistic fuzzy subnearing of R_2 .
- (iii) either A is an (T, S)-intuitionistic fuzzy subnearring of R₁ or B is an (T, S)-intuitionistic fuzzy subnearring of R₂.

Proof: Let A×B be an (T, S)-intuitionistic fuzzy subnearring of $R_1 \times R_2$ and x and y in R_1 and R_2 . Then (x, 0) and $(y, 0_1)$ are in $R_1 \times R_2$. Now using the property that $\mu_A(x) \le \mu_B(0_1)$ and $\nu_A(x) \ge \nu_B(0_1)$ for all x in R_1 . We get $\mu_{A}(x-y) = \min\{\mu_{A}(x-y), \quad \mu_{B}(0_{1}-0_{1})\} = \mu_{A\times B}((x-y), (0_{1}-0_{1})) = \mu_{A\times B}[(x, 0_{1}), -(y, 0_{1})] \geq T(\mu_{A\times B}(x, 0_{1}), \mu_{A\times B}(y, 0_{1})) = T(\mu_{A\times B}(x, 0_{1}), \mu_{A\times B}(y$ $T(\min\{\mu_A(x), \mu_B(0_1)\}, \min\{\mu_A(y), \mu_B(0_1)\}) = T(\mu_A(x), \mu_A(y)).$ Therefore $\mu_A(x-y) \ge T(\mu_A(x), \mu_A(y))$ for all x and y in R_1 . Also $\mu_A(xy) = \min\{ \mu_A(xy), \mu_B(0_10_1) \} = \mu_{A\times B}((xy), (0_10_1)) = \mu_{A\times B}[(x, 0_1)(y, 0_1)] \ge T(\mu_{A\times B}(x, 0_1), \mu_{A\times B}(y, 0_1)) = T(\mu_{A\times B}(x, 0_1), \mu_{A\times$ $T(\min\{\mu_A(x), \mu_B(0_l)\}, \min\{\mu_A(y), \mu_B(0_l)\}) = T(\mu_A(x), \mu_A(y)).$ Therefore $\mu_A(xy) \ge T(\mu_A(x), \mu_A(y)),$ for all x and y in R_1 . And $v_A(x-y) = \max\{v_A(x-y), v_B(0_|-0_l)\} = v_{A\times B}((x-y), (0_|-0_l)) = v_{A\times B}[(x, 0_l)-(y, 0_l)] \le S(v_{A\times B}(x, 0_l), v_{A\times B}(y, 0_l)) = v_{A\times B}(x, 0_l) = v_$ $S(\max\{v_A(x), v_B(0_l)\}, \max\{v_A(y), v_B(0_l)\}) = S(v_A(x), v_A(y)).$ Therefore $v_A(x-y) \le S(v_A(x), v_A(y))$ for all x and y in R_1 . Also $v_A(xy) = \max\{v_A(xy), v_B(0_10_1)\} = v_{A\times B}((xy), (0_10_1)) = v_{A\times B}[(x, 0_1), (y, 0_1)] \le S(v_{A\times B}(x, 0_1), v_{A\times B}(y, 0_1)) = V_{A\times B}(y, 0_1)$ $S(\max\{\nu_A(x), \nu_B(0_i)\}, \max\{\nu_A(y), \nu_B(0_i)\}) = S(\nu_A(x), \nu_A(y)).$ Therefore $\nu_A(xy) \le S(\nu_A(x), \nu_A(y)),$ for all x and y in R_1 . Hence A is an (T, S)-intuitionistic fuzzy subnearring of R₁. Thus (i) is proved. Now using the property that $\mu_R(x) \le \mu_A(0)$ and $\nu_R(x) \ge \nu_A(0)$, for all x in R_2 , let x and y in R_2 and 0 in R_1 . Then (0, x) and (0, y) are in $R_1 \times R_2$. We get $\mu_B(x-y) = \min\{\mu_B(x-y), \ \mu_A(0-0)\} = \min\{\mu_A(0-0), \ \mu_B(x-y)\} = \mu_{A\times B}(\ (0-0), \ (x-y)) = \mu_{A\times B}[\ (0, \ x) - (0, \ y)] \geq T(\ \mu_{A\times B}(0, \ x), \ (0-0), \ (x-y)) = \mu_{A\times B}[\ (0, \ x) - (0, \ y)] \geq T(\ \mu_{A\times B}(0, \ x), \ (x-y)) = \mu_{A\times B}[\ (0, \ x) - (0, \ y)] \geq T(\ \mu_{A\times B}(0, \ x), \ (x-y)) = \mu_{A\times B}[\ (0, \ x) - (0, \ y)] \geq T(\ \mu_{A\times B}(0, \ x), \ (x-y)) = \mu_{A\times B}[\ (0, \ x) - (0, \ y)] \geq T(\ \mu_{A\times B}(0, \ x), \ (x-y)) = \mu_{A\times B}[\ (0, \ x) - (0, \ y)] \geq T(\ \mu_{A\times B}(0, \ x), \ (x-y)) = \mu_{A\times B}[\ (0, \ x) - (0, \ y)] \geq T(\ \mu_{A\times B}(0, \ x), \ (x-y)) = \mu_{A\times B}[\ (0, \ x) - (0, \ y)] \geq T(\ \mu_{A\times B}(0, \ x), \ (x-y)) = \mu_{A\times B}[\ (0, \ x) - (0, \ y)] \geq T(\ \mu_{A\times B}(0, \ x), \ (x-y)) = \mu_{A\times B}[\ (0, \ x) - (0, \ y)] \geq T(\ \mu_{A\times B}(0, \ x), \ (x-y)) = \mu_{A\times B}[\ (0, \ x) - (0, \ y)] \geq T(\ \mu_{A\times B}(0, \ x), \ (x-y)) = \mu_{A\times B}[\ (0, \ x) - (0, \ y)] \geq T(\ \mu_{A\times B}(0, \ x), \ (x-y)) = \mu_{A\times B}[\ (0, \ x) - (0, \ y)] = \mu_{A\times B}[\ (0, \$ $\mu_{A \times B}(0, y) = T(\min\{\mu_A(0), \mu_B(x)\}, \min\{\mu_A(0), \mu_B(y)\} = T(\mu_B(x), \mu_B(y)).$ Therefore $\mu_B(x-y) \ge S(\mu_B(x), \mu_B(y))$ for all $x = T(\mu_B(x), \mu_B(y))$ and y in R₂. Also $\mu_B(xy) = \min\{\mu_B(xy), \mu_A(00)\} = \min\{\mu_A(00), \mu_B(xy)\} = \mu_{A\times B}((00), (xy)) = \mu_{A\times B}[(0, x), (0, y)] \ge 1$ $T(\mu_{A\times B}(0, x), \ \mu_{A\times B}(0, y)) = T(\min\{\mu_A(0), \ \mu_B(x)\}, \ \min\{\mu_A(0), \ \mu_B(y)\}) = T(\mu_B(x), \ \mu_B(y)). \ Therefore \ \mu_B(xy) \ge T(\mu_B(x), \ \mu_B(y))$ $\mu_B(y)$) for all x and y in R_2 . And $\nu_B(x-y) = \max\{\nu_B(x-y), \nu_A(0-0)\} = \max\{\nu_A(0-0), \nu_B(x-y)\} = \nu_{A\times B}((0-0), (x-y)) = \max\{\nu_B(x-y), \nu_A(0-0)\} = \max\{\nu_B(x-y), \nu_B(x-y)\} = \nu_{A\times B}((0-0), \nu_B(x-y)) = \nu_{A\times B}((0-0), \nu_B(x-y)$ $v_{A\times B}[(0, x) - (0, y)] \le S(v_{A\times B}(0, x), v_{A\times B}(0, y)) = S(\max\{v_A(0), v_B(x)\}, \max\{v_A(0), v_B(y)\}) = S(v_B(x), v_B(y)).$ Therefore $v_B(x-y) \le S(v_B(x), v_B(y))$ for all x and y in R_2 . Also $v_B(xy) = \max\{v_B(xy), v_A(00)\} = \max\{v_A(00), v_B(xy)\} = v_{A\times B}((00), v_B(xy))$ $(xy) = v_{A\times B}[(0, x)(0, y)] \le S(v_{A\times B}(0, x), v_{A\times B}(0, y)) = S(\max\{v_A(0), v_B(x)\}, \max\{v_A(0), v_B(y)\}) = S(v_B(x), v_B(y)).$ Therefore $v_B(xy) \leq S(v_B(x), v_B(y))$, for all x and y in R₂. Hence B is an (T, S)-intuitionistic fuzzy subnearring of a nearring R_2 . Thus (ii) is proved. (iii) is clear.

2.7 Theorem: Let A be an intuitionistic fuzzy subset of a nearring R and V be the strongest intuitionistic fuzzy relation of R. Then A is an (T, S)-intuitionistic fuzzy subnearring of R if and only if V is an (T, S)-intuitionistic fuzzy subnearring of R×R.

 $\begin{array}{l} \textbf{Proof:} \ \, \text{Suppose that A is an } (T,\,S)\text{-intuitionistic fuzzy subnearring of a nearring } R. \ \, \text{Then for any } x = (x_1,\,x_2) \ \text{and } y = (y_1,\,y_2) \ \text{are in } R \times R. \ \, \text{We have } \mu_V(x-y) = \mu_V[(x_1,\,x_2) - (y_1,\,y_2)] = \mu_V(x_1-y_1,\,x_2-y_2) = \min\{\mu_A(x_1-y_1),\,\mu_A(x_2-y_2)\} \geq \min\{T(\mu_A(x_1),\,\mu_A(y_1)),\,T(\,\mu_A(x_2),\,\mu_A(y_2))\} \geq T(\min\{\mu_A(x_1),\,\mu_A(x_2)\},\,\min\{\mu_A(y_1),\,\mu_A(y_2)\}) = T(\mu_V(x_1,\,x_2),\,\mu_V(y_1,\,y_2)) = T(\mu_V(x),\,\mu_V(y)). \ \, \text{Therefore } \mu_V(x-y) \geq T(\mu_V(x),\,\mu_V(y)),\,\text{for all } x \,\text{and } y \,\text{in } R \times R. \ \, \text{And } \mu_V(xy) = \mu_V[(x_1,\,x_2)(y_1,\,y_2)] = \mu_V(x_1y_1,\,x_2y_2) = \min\{\mu_A(x_1y_1),\,\mu_A(x_2y_2)\} \geq \min\{T(\mu_A(x_1),\,\mu_A(y_1)),\,T(\mu_A(x_2),\,\mu_A(y_2))\} \geq T(\min\{\mu_A(x_1),\,\mu_A(x_2)\},\,\min\{\mu_A(y_1),\,\mu_A(y_2)\}) = T(\mu_V(x_1,\,x_2),\,\mu_V(y_1,\,y_2)) = T(\mu_V(x),\,\mu_V(y))\,. \ \, \text{Therefore } \mu_V(xy) \geq T(\mu_V(x),\,\mu_V(y)),\,\text{for all } x \,\text{and } y \,\text{in } R \times R. \ \, \text{We have } \nu_V(x-y) = \nu_V\left[(x_1,\,x_2)-(y_1,\,y_2)\right] = \nu_V(x_1-y_1,\,x_2-y_2) = \max\{\nu_A(x_1-y_1),\,\nu_A(x_2-y_2)\} \leq \max\{S(\nu_A(x_1),\,\nu_A(y_1)),\,S(\nu_A(x_2),\,\nu_A(y_2))\} \leq S(\max\{\nu_A(x_1),\,\nu_A(x_2)\},\,\max\{\nu_A(y_1),\,\nu_A(y_2)\}) = S(\nu_V(x_1,\,x_2),\,\nu_V(y_1,\,y_2)) = S(\nu_V(x),\,\nu_V(y)). \ \, \text{Therefore } \nu_V(x-y) \leq S(\nu_V(x),\,\nu_V(y)),\,\text{for all } x \,\text{and } y \,\text{in } R \times R. \ \, \text{And } \nu_V(xy) = \nu_V[(x_1,\,x_2),\,\nu_V(y_1,\,y_2)] = \nu_V(x_1,\,x_2) = \nu_V(x_1,\,x_2),\,\nu_V(y_1,\,y_2) = \nu_V(x_1,\,x_2),\,\nu_V(y_1,\,x_2) = \nu_V(x_1,\,x_2),\,\nu_V(y_1,\,x_2) = \nu_V(x_1,\,x_2),\,\nu_V(y_1,\,x_2) = \nu_V(x_1,\,x_2),\,\nu_V(y_1,\,x_2) = \nu_V(x_1,\,x_2),\,\nu_V(y_1,\,x_2) = \nu_V(x_1,\,x$

 $\max \left\{ v_A(x_1y_1), \, v_A(x_2y_2) \right\} \leq \max \left\{ S(v_A(x_1), \, v_A(y_1)), \, S\left(v_A(x_2), \, v_A(y_2)\right) \right\} \leq S(\max\{v_A(x_1), \, v_A(x_2)\}, \, \max\{v_A(y_1), \, v_A(y_2)\}) = \\ S(v_V(x_1, \, x_2), \, v_V(y_1, \, y_2)) = S(v_V(x), \, v_V(y)). \, \text{Therefore, } v_V(xy) \leq S(v_V(x), \, v_V(y)), \, \text{for all } x \, \text{and } y \, \text{in } R \times R. \, \text{This proves that } V \, \text{is an } (T, \, S)\text{-intuitionistic fuzzy subnearring of } R \times R. \, \text{Conversely assume that } V \, \text{is an } (T, \, S)\text{-intuitionistic fuzzy subnearring of } R \times R. \, \text{Conversely assume that } V \, \text{is an } (T, \, S)\text{-intuitionistic fuzzy subnearring of } R \times R. \, \text{Conversely assume that } V \, \text{is an } (T, \, S)\text{-intuitionistic fuzzy subnearring of } R \times R. \, \text{Conversely assume that } V \, \text{is an } (T, \, S)\text{-intuitionistic fuzzy subnearring of } R \times R. \, \text{Conversely assume that } V \, \text{is an } (T, \, S)\text{-intuitionistic fuzzy subnearring of } R \times R. \, \text{Conversely assume that } V \, \text{is an } (T, \, S)\text{-intuitionistic fuzzy subnearring of } R \times R. \, \text{Conversely assume that } V \, \text{is an } (T, \, S)\text{-intuitionistic fuzzy subnearring of } R \times R. \, \text{Conversely assume that } V \, \text{is an } (T, \, S)\text{-intuitionistic fuzzy subnearring of } R \times R. \, \text{Conversely assume that } V \, \text{is an } (T, \, S)\text{-intuitionistic fuzzy subnearring of } R \times R. \, \text{Conversely assume that } V \, \text{is an } (T, \, S)\text{-intuitionistic fuzzy subnearring of } R \times R. \, \text{Conversely assume that } V \, \text{is an } (T, \, S)\text{-intuitionistic fuzzy} \text{subnearring of } R \times R. \, \text{Conversely assume that } V \, \text{is an } (T, \, S)\text{-intuitionistic fuzzy} \text{subnearring of } R \times R. \, \text{Conversely assume that } V \, \text{is an } (T, \, S)\text{-intuitionistic fuzzy} \text{subnearring of } R \times R. \, \text{Conversely assume that } V \, \text{is an } (T, \, S)\text{-intuitionistic fuzzy} \text{subnearring of } R \times R. \, \text{Conversely assume that } V \, \text{is an } (T, \, S)\text{-intuitionistic fuzzy} \text{subnearring of } R \times R. \, \text{Conversely assume that } V \, \text{is an } (T, \, S)\text{-intuitionistic fuzzy} \text{subnearring of } R \times R. \, \text{Conversely assume that } V \, \text{is$

2.8 Theorem: If A is an (T, S)-intuitionistic fuzzy subnearring of a nearring (R, +, .), then $H = \{x \mid x \in R: \mu_A(x) = 1, \nu_A(x) = 0\}$ is either empty or is a subnearring of R.

Proof: It is trivial.

2.9 Theorem: If A be an (T, S)-intuitionistic fuzzy subnearring of a nearring (R, +, .), then (i) if $\mu_A(x-y)=0$, then either $\mu_A(x)=0$ or $\mu_A(y)=0$ for all x and y in R. (ii) if $\mu_A(xy)=0$, then either $\mu_A(x)=0$ or $\mu_A(y)=0$ for all x and y in R. (iii) if $\nu_A(x-y)=1$, then either $\nu_A(x)=1$ for all x and y in R. (iv) if $\nu_A(xy)=1$, then either $\nu_A(x)=1$ or $\nu_A(y)=1$ for all x and y in R.

Proof: It is trivial.

2.10 Theorem: If A is an (T, S)-intuitionistic fuzzy subnearring of a nearring (R,+, .), then $\Box A$ is an (T, S)-intuitionistic fuzzy subnearring of R.

Proof: Let A be an (T, S)-intuitionistic fuzzy subnearring of a nearring R. Consider $A = \{\langle x, \mu_A(x), \nu_A(x) \rangle\}$, for all x in R, we take $\Box A = B = \{\langle x, \mu_B(x), \nu_B(x) \rangle\}$, where $\mu_B(x) = \mu_A(x)$, $\nu_B(x) = 1 - \mu_A(x)$. Clearly $\mu_B(x-y) \geq T(\mu_B(x), \mu_B(y))$ for all x and y in R and $\mu_B(xy) \geq T(\mu_B(x), \mu_B(y))$ for all x and y in R. Since A is an (T, S)-intuitionistic fuzzy subnearring of R, we have $\mu_A(x-y) \geq T(\mu_A(x), \mu_A(y))$ for all x and y in R, which implies that $1 - \nu_B(x-y) \geq T((1 - \nu_B(x)), (1 - \nu_B(y)))$, which implies that $\nu_B(x-y) \leq 1 - T((1 - \nu_B(x)), (1 - \nu_B(y))) \leq S(\nu_B(x), \nu_B(y))$. Therefore $\nu_B(x-y) \leq S(\nu_B(x), \nu_B(y))$, for all x and y in R. And $\mu_A(xy) \geq T(\mu_A(x), \mu_A(y))$ for all x and y in R, which implies that $1 - \nu_B(xy) \geq T((1 - \nu_B(x)), (1 - \nu_B(y)))$ which implies that $\nu_B(xy) \leq 1 - T((1 - \nu_B(x)), (1 - \nu_B(y))) \leq S(\nu_B(x), \nu_B(y))$. Therefore $\nu_B(xy) \leq S(\nu_B(x), \nu_B(y))$ for all x and y in R. Hence $\nu_B(xy) \leq S(\nu_B(x), \nu_B(y))$ for all x and y in R. Hence $\nu_B(xy) \leq S(\nu_B(x), \nu_B(y))$.

2.11 Theorem: If A is an (T, S)-intuitionistic fuzzy subnearring of a nearring (R, +, .), then $\Diamond A$ is an (T, S)-intuitionistic fuzzy subnearring of R.

Proof: Let A be an (T, S)-intuitionistic fuzzy subnearring of a nearring R. That is $A = \{\langle x, \mu_A(x), \nu_A(x) \rangle\}$ for all x in R. Let $\Diamond A = B = \{\langle x, \mu_B(x), \nu_B(x) \rangle\}$ where $\mu_B(x) = 1 - \nu_A(x), \nu_B(x) = \nu_A(x)$. Clearly $\nu_B(x-y) \leq S(\nu_B(x), \nu_B(y))$ for all x and y in R and $\nu_B(xy) \leq S(\nu_B(x), \nu_B(y))$ for all x and y in R. Since A is an (T, S)-intuitionistic fuzzy subnearring of R, we have $\nu_A(x-y) \leq S(\nu_A(x), \nu_A(y))$ for all x and y in R, which implies that $1 - \mu_B(x-y) \leq S((1 - \mu_B(x)), (1 - \mu_B(y)))$ which implies that $\mu_B(x-y) \geq 1 - S((1 - \mu_B(x)), (1 - \mu_B(y))) \geq T(\mu_B(x), \mu_B(y))$. Therefore $\mu_B(x-y) \geq T(\mu_B(x), \mu_B(y))$ for all x and y in R. And $\nu_A(xy) \leq S(\nu_A(x), \nu_A(y))$ for all x and y in R, which implies that $1 - \mu_B(xy) \leq S((1 - \mu_B(x)), (1 - \mu_B(y)))$ which implies that $\mu_B(xy) \geq 1 - S((1 - \mu_B(x)), (1 - \mu_B(y))) \geq T(\mu_B(x), \mu_B(y))$. Therefore $\mu_B(xy) \geq T(\mu_B(x), \mu_B(y))$ for all x and y in R. Hence $y \in A$ is an $y \in A$ in $y \in A$ in $y \in A$ in $y \in A$ is an $y \in A$ in $y \in A$ in

2.12 Theorem: Let A be an (T, S)-intuitionistic fuzzy subnearring of a nearing (R, +, .), then the pseudo (T, S)-intuitionistic fuzzy coset $(aA)^p$ is an (T, S)-intuitionistic fuzzy subnearring of a nearring R, for every a in R.

Proof: Let A be an (T, S)-intuitionistic fuzzy subnearring of a nearring R.

For every x and y in R, we have $((a\mu_A)^p)(x-y) = p(a)\mu_A(x-y) \ge p(a)T((\mu_A(x), \mu_A(y)) = T(p(a)\mu_A(x), p(a)\mu_A(y)) = T(((a\mu_A)^p)(x), ((a\mu_A)^p)(x))$. Therefore $((a\mu_A)^p)(x-y) \ge T(((a\mu_A)^p)(x), ((a\mu_A)^p)(y))$. Now $((a\mu_A)^p)(xy) = p(a)\mu_A(xy) \ge p(a)T(\mu_A(x), \mu_A(y)) = T(p(a)\mu_A(x), p(a)\mu_A(y)) = T(((a\mu_A)^p)(x), ((a\mu_A)^p)(y))$. Therefore $((a\mu_A)^p)(xy) \ge T(((a\mu_A)^p)(x), ((a\mu_A)^p)(y))$. For every x and y in R, we have $((a\nu_A)^p)(x-y) = p(a)\nu_A(x-y) \le p(a)S((\nu_A(x), \nu_A(y)) = S(p(a)\nu_A(x), \mu_A(y)) = S(((a\nu_A)^p)(x), ((a\nu_A)^p)(x))$. Therefore $((a\nu_A)^p)(x-y) \le S(((a\nu_A)^p)(x), ((a\nu_A)^p)(y))$.

Now $((av_A)^p)(xy) = p(a)v_A(xy) \le p(a)$ $S(v_A(x), v_A(y)) = S(p(a)v_A(x), p(a)v_A(y)) = S(((av_A)^p)(x), ((av_A)^p)(y))$. Therefore $((av_A)^p)(xy) \le S(((av_A)^p)(x), ((av_A)^p)(y))$. Hence $(aA)^p$ is an (T, S)-intuitionistic fuzzy subnearring of a nearring R.

In the following Theorem • is the composition operation of functions:

2.13 Theorem: Let A be an (T, S)-intuitionistic fuzzy subnearring of a nearring H and f is an isomorphism from a nearring R onto H. Then $A \circ f$ is an (T, S)-intuitionistic fuzzy subnearring of R.

 $\begin{array}{l} \textbf{Proof:} \ \text{Let} \ x \ \text{and} \ y \ \text{in} \ R \ \text{and} \ A \ \text{be} \ \text{an} \ (T, S)\text{-intuitionistic} \ \text{fuzzy} \ \text{subnearring} \ \text{of} \ \text{a} \ \text{nearring} \ H. \ \text{Then} \ \text{we have} \ (\mu_{A^\circ}f)(x-y) \\ = \ \mu_A(f(x-y)) \ = \ \mu_A(f(x) - f(y)) \ \geq \ T(\mu_A(f(x)), \ \mu_A(f(y))) \ = \ T((\mu_{A^\circ}f)(x), \ (\mu_{A^\circ}f)(y)) \ \text{which} \ \text{implies} \ \text{that} \ (\mu_{A^\circ}f)(x-y) \geq \\ T((\mu_{A^\circ}f)(x), \ (\mu_{A^\circ}f)(y)). \ \text{And} \ (\mu_{A^\circ}f)(xy) \ = \ \mu_A(f(xy)) \ = \ \mu_A(f(x)f(y)) \geq T(\mu_A(f(x)), \ \mu_A(f(y))) \ = \ T((\mu_{A^\circ}f)(x), \ (\mu_{A^\circ}f)(y)) \ \text{which} \ \text{implies} \ \text{that} \ (\mu_{A^\circ}f)(x), \ (\mu_{A^\circ}f)(y)) \ \text{which} \ \text{implies} \ \text{that} \ (\nu_{A^\circ}f)(x), \ (\nu_{A^\circ}f)(y)). \ \text{And} \ (\nu_{A^\circ}f)(xy) \ = \ \nu_A(f(x)f(y)) \ = \ S((\nu_{A^\circ}f)(x), \ (\nu_{A^\circ}f)(y)) \ \text{which} \ \text{implies} \ \text{that} \ (\nu_{A^\circ}f)(xy) \ \leq \ S((\nu_{A^\circ}f)(x), \ (\nu_{A^\circ}f)(y)). \ \text{Therefore} \ (A^\circ f) \ \text{is an} \ (T, S)\text{-intuitionistic fuzzy subnearring} \ \text{of} \ \text{a nearring} \ R. \end{array}$

2.14 Theorem: Let A be an (T, S)-intuitionistic fuzzy subnearring of a nearring H and f is an anti-isomorphism from a nearring R onto H. Then $A \circ f$ is an (T, S)-intuitionistic fuzzy subnearring of R.

Proof: Let x and y in R and A be an (T, S)-intuitionistic fuzzy subnearring of a nearring H. Then we have $(\mu_A \circ f)(x-y) = \mu_A(f(x-y)) = \mu_A(f(y)-f(x)) \ge T(\mu_A(f(x)), \ \mu_A(f(y))) = T((\mu_A \circ f)(x), \ (\mu_A \circ f)(y))$ which implies that $(\mu_A \circ f)(x-y) \ge T(\mu_A \circ f)(x), \ (\mu_A \circ f)(x)$. And $(\mu_A \circ f)(xy) = \mu_A(f(xy)) = \mu_A(f(y)f(x)) \ge T(\mu_A(f(x)), \mu_A(f(y))) = T((\mu_A \circ f)(x), \ (\mu_A \circ f)(x))$ which implies that $(\mu_A \circ f)(xy) \ge T((\mu_A \circ f)(x), \ (\mu_A \circ f)(y))$. Then we have $(\nu_A \circ f)(x-y) = \nu_A(f(x-y)) = \nu_A(f(y)-f(x)) \le S(\nu_A(f(x)), \nu_A(f(y))) = S((\nu_A \circ f)(x), (\nu_A \circ f)(x))$ which implies that $(\nu_A \circ f)(x-y) \le S((\nu_A \circ f)(x), (\nu_A \circ f)(y))$. And $(\nu_A \circ f)(xy) = \nu_A(f(y)f(x)) \le S(\nu_A(f(x)), \nu_A(f(y))) = S((\nu_A \circ f)(x), (\nu_A \circ f)(y))$, which implies that $(\nu_A \circ f)(x)$ which implies that $(\nu_A \circ f)(x)$ is an (T, S)-intuitionistic fuzzy subnearing of the nearing R.

2.15 Theorem: Let (R, +, .) and $(R^1, +, .)$ be any two nearrings. The homomorphic image of an (T, S)-intuitionistic fuzzy subnearring of R is an (T, S)-intuitionistic fuzzy subnearring of R^1 .

Proof: Let (R, +, ...) and $(R^1, +, ...)$ be any two nearrings. Let $f: R \to R^1$ be a homomorphism. Let V = f(A) where A is an (T, S)-intuitionistic fuzzy subnearring of R. We have to prove that V is an (T, S)-intuitionistic fuzzy subnearring of R^1 . Now for f(x), f(y) in R^1 , $\mu_v(f(x)-f(y)) = \mu_v(f(x-y)) \ge \mu_A(x-y) \ge T(\mu_A(x), \mu_A(y))$ which implies that $\mu_v(f(x)-f(y)) \ge T(\mu_v(f(x)), \mu_v(f(y)))$. Again $\mu_v(f(x)f(y)) = \mu_v(f(xy)) \ge \mu_A(xy) \ge T(\mu_A(x), \mu_A(y))$ which implies that $\mu_v(f(x)f(y)) \ge T(\mu_v(f(x)), \mu_v(f(y)))$. And $\nu_v(f(x)-f(y)) = \nu_v(f(x-y)) \le \nu_A(x-y) \le S(\nu_A(x), \nu_A(y))$. Therefore $\nu_v(f(x)-f(y)) \le S(\nu_v(f(x)), \nu_v(f(y)))$. Again $\nu_v(f(x)f(y)) = \nu_v(f(xy)) \le \nu_A(xy) \le S(\nu_A(x), \nu_A(y))$ which implies that $\nu_v(f(x)f(y)) \le S(\nu_v(f(x)), \nu_v(f(y)))$. Hence V is an (T, S)-intuitionistic fuzzy subnearring of R^1 .

2.16 Theorem: Let (R, +, .) and $(R^1, +, .)$ be any two nearrings. The homomorphic preimage of an (T, S)-intuitionistic fuzzy subnearring of R^1 is a (T, S)-intuitionistic fuzzy subnearring of R.

Proof: Let V = f(A), where V is an (T, S)-intuitionistic fuzzy subnearring of R^1 . We have to prove that A is an (T, S)-intuitionistic fuzzy subnearring of R. Let x and y in R. Then $\mu_A(x-y) = \mu_v(f(x-y)) = \mu_v(f(x)-f(y)) \geq T(\mu_v(f(x)), \mu_v(f(y))) = T(\mu_A(x), \mu_A(y))$ which implies that $\mu_A(x-y) \geq T(\mu_A(x), \mu_A(y))$. Again $\mu_A(xy) = \mu_v(f(xy)) = \mu_v(f(x)f(y)) \geq T(\mu_v(f(x)), \mu_v(f(y))) = T(\mu_A(x), \mu_A(y))$ which implies that $\mu_A(xy) \geq T(\mu_A(x), \mu_A(y))$. And $\nu_A(x-y) = \nu_v(f(x-y)) = \nu_v(f(x)-f(y)) \leq S(\nu_v(f(x)), \nu_v(f(y))) = S(\nu_A(x), \nu_A(y))$ which implies that $\nu_A(x-y) \leq S(\nu_A(x), \nu_A(y))$. Again $\nu_A(xy) = \nu_v(f(xy)) = \nu_v(f(x)-f(y)) \leq \nu_v(f(x))$. Where $\nu_A(x) = \nu_A(x)$ is an $\nu_A(x) = \nu_A(x)$ which implies that $\nu_A(x) \leq S(\nu_A(x), \nu_A(y))$. Hence $\nu_A(x) = \nu_A(x)$ is an $\nu_A(x) = \nu_A(x)$ intuitionistic fuzzy subnearing of $\nu_A(x)$.

2.17 Theorem: Let (R, +, .) and $(R^1, +, .)$ be any two nearrings. The anti-homomorphic image of an (T, S)-intuitionistic fuzzy subnearring of R is an (T, S)-intuitionistic fuzzy subnearring of R^1 .

Proof: Let (R, +, .) and $(R^l, +, .)$ be any two nearrings. Let $f: R \to R^l$ be an anti-homomorphism. Then f(x+y) = f(y) + f(x) and f(xy) = f(y)f(x) for all x and y in R. Let V = f(A) where A is an (T, S)-intuitionistic fuzzy subnearring of R. We have to prove that V is an (T, S)-intuitionistic fuzzy subnearring of R^l . Now for f(x), f(y) in R^l , $\mu_v(f(x)-f(y)) = \mu_v(f(y-x)) \ge \mu_A(y-x) \ge T(\mu_A(y), \, \mu_A(x)) = T(\mu_A(x), \, \mu_A(y))$, which implies that $\mu_v(f(x)-f(y)) \ge T(\mu_v(f(x)), \, \mu_v(f(y)))$. Again $\mu_v(f(x)f(y)) = \mu_v(f(yx)) \ge \mu_A(yx) \ge T(\mu_A(y), \, \mu_A(x)) = T(\mu_A(x), \, \mu_A(y))$ which implies that $\mu_v(f(x)f(y)) \ge T(\mu_v(f(x)), \, \mu_v(f(y)))$. And $\nu_v(f(x)-f(y)) = \nu_v(f(y-x)) \le \nu_A(y-x) \le S(\nu_A(y), \, \nu_A(x)) = S(\nu_A(x), \, \nu_A(y))$ which implies that $\nu_v(f(x)-f(y)) \le S(\nu_v(f(x)), \, \nu_v(f(x)))$. Again $\nu_v(f(x)f(y)) = \nu_v(f(yx)) \le \nu_A(yx) \le S(\nu_A(y), \, \nu_A(x)) = S(\nu_A(x), \, \nu_A(y))$ which implies that $\nu_v(f(x)-f(y)) \le S(\nu_v(f(x)), \, \nu_v(f(x)))$. Hence V is an (T, S)-intuitionistic fuzzy subnearring of R^l .

2.18 Theorem: Let (R, +, ...) and $(R^1, +, ...)$ be any two nearrings. The anti-homomorphic preimage of an (T, S)-intuitionistic fuzzy subnearring of R^1 is an (T, S)-intuitionistic fuzzy subnearring of R^2 .

Proof: Let V = f(A), where V is an (T, S)-intuitionistic fuzzy subnearring of $R^{!}$. We have to prove that A is an (T, S)-intuitionistic fuzzy subnearring of R. Let x and y in R. Then $\mu_A(x-y)=\mu_v(f(x-y))=\mu_v(f(y)-f(x))\geq T(\mu_v(f(y)),\,\mu_v(f(x)))=T(\mu_v(f(x)),\,\mu_v(f(x)))=T(\mu_v(f(x)),\,\mu_v(f(x)))=T(\mu_v(f(x)),\,\mu_v(f(x)))=T(\mu_v(f(x)),\,\mu_v(f(x)))=T(\mu_v(f(x)),\,\mu_v(f(y)))=T(\mu_v(f(x)),\,\mu_v(f(y)))=T(\mu_v(f(x)),\,\mu_v(f(y)))=T(\mu_v(f(x)),\,\mu_v(f(x)))=T$

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