

**SUPER EDGE TRIMAGIC TOTAL LABELING OF SOME DISCONNECTED GRAPHS**

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*(Received On: 14-07-15; Revised & Accepted On: 31-07-15)*

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**ABSTRACT**

An edge trimagic total labeling of a  $(p, q)$  graph  $G$  is a bijection  $f: V(G) \cup E(G) \rightarrow \{1, 2, \dots, p+q\}$  such that for each edge  $uv \in E(G)$ , the value of  $f(u)+f(uv)+f(v)$  is equal to either  $k_1$  or  $k_2$  or  $k_3$ . In this paper we prove that the disconnected graphs  $(C_m \odot K_1) \cup P_n$ ,  $(C_m \odot K_1) \cup C_n$  and  $P_m \cup P_n \cup P_r$  admit edge trimagic total labeling and super edge trimagic total labeling.

**Keywords:** Function, Bijection, Labeling, Magic, Trimagic.

**AMS Subject Classification:** 05C78.

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**1. INTRODUCTION**

A Graph labeling is an assignment of integers to the elements of a graph, the vertices or edges or both subject to certain conditions. In 1967 Rosa introduced the concept of graph labeling. In 1970, Kotzig and Rosa[7] defined, the magic labeling of graph  $G$  is a bijection  $f: V \cup E \rightarrow \{1, 2, \dots, p+q\}$  such that for each edge  $uv \in E$ ,  $f(u)+f(uv)+f(v)$  is a magic constant. W. D. Wallis [8] introduced this as edge magic total labeling. J. Baskar Babujee introduced the bimagic labeling of graphs in 2004[1]. In 2013, C. Jayasekaran, M. Regees and C. Davidraj introduced the edge trimagic total labeling of graphs [4]. M. Regees and C. Jayasekaran proved that some classes and families of graphs are edge trimagic total [5, 6]. Some definitions relevant to this paper are given below.

**Definition 1.1:** [4] An edge trimagic total labeling of a  $(p, q)$  graph  $G$  is a bijective function  $f: V(G) \cup E(G) \rightarrow \{1, 2, \dots, p+q\}$  such that for each edge  $xy \in E(G)$ , the value of  $f(x)+f(xy)+f(y)$  is equal to any of the distinct constants  $k_1$  or  $k_2$  or  $k_3$ . A graph  $G$  is said to be edge trimagic total if it admits an edge trimagic total labeling. An edge trimagic total labeling is called a super edge trimagic total labeling if  $G$  has the additional property that the vertices are labeled with smallest positive integers.

**Definition 1.2:** The union of two graphs  $G_1 = (V_1, E_1)$  and  $G_2 = (V_2, E_2)$  is a graph  $G = G_1 \cup G_2$  with vertex set  $V = V_1 \cup V_2$  and the edge set  $E = E_1 \cup E_2$ .

**Definition 1.4:** [4] If  $G$  is of order  $n$ , the corona of  $G$  with  $H$ ,  $G \odot H$  is the graph obtained by taking one copy of  $G$  and  $n$  copies of  $H$  and joining the  $i^{\text{th}}$  vertex of  $G$  with every vertex in the  $i^{\text{th}}$  copy of  $H$ .

The dynamic survey of graph labeling by J.A.Gallian[3] can be used for further references. The notations and terminology are taken from [2]. This paper prove that the graphs  $(C_m \odot K_1) \cup P_n$ ,  $(C_m \odot K_1) \cup C_n$  and  $P_m \cup P_n \cup P_r$  are edge trimagic total and super edge trimagic total.

**2. MAIN RESULTS**

**Theorem 2.1:**  $(C_m \odot K_1) \cup P_n$  admits an edge trimagic total labeling.

**Proof:** Let  $u_1 u_2 \dots u_m u_1$  be the cycle  $C_m$  and let  $v_i$  be the vertex which is joined to the vertex  $u_i$  of the cycle  $C_m$ ,  $1 \leq i \leq m$ . The resultant graph is  $C_m \odot K_1$ . Let  $w_1 w_2 \dots w_n$  be the path  $P_n$ . Then  $(C_m \odot K_1) \cup P_n$  is a disconnected graph with  $2m + n$  vertices and  $2m + n - 1$  edges.

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Define a bijection  $f: V \cup E \rightarrow \{1, 2, \dots, 4m+2n-1\}$  such that,

**Case-1:**  $n$  is odd.

$$f(u_i) = i, 1 \leq i \leq m, f(v_i) = m+ i, 1 \leq i \leq m,$$

$$f(w_i) = \begin{cases} 2m + \frac{i+1}{2}, & 1 \leq i \leq n \text{ and } i \text{ is odd} \\ 2m + \frac{n+i+1}{2}, & 1 \leq i \leq n \text{ and } i \text{ is even,} \end{cases}$$

$$f(u_i u_{i+1}) = 4m+2n-2i-1, 1 \leq i \leq m-1; f(u_i v_i) = 4m+2n-2i, 1 \leq i \leq m;$$

$$f(w_i w_{i+1}) = 2m+2n - i, 1 \leq i \leq n - 1 \text{ and } f(u_m u_1) = 4m+2n-1.$$

Now we can verify that for each edge  $uv \in E$ , the value of  $f(u)+f(uv)+f(v)$  yields any of the trimagic constants  $\lambda_1 = 4m+2n, \lambda_2 = 5m+2n$  and  $\lambda_3 = \frac{12m+5n+3}{2}$ .

**Case-2:**  $n$  is even.

$$f(u_i) = i, 1 \leq i \leq m, f(v_i) = m+ i, 1 \leq i \leq m,$$

$$f(w_i) = \begin{cases} 2m + \frac{i+1}{2}, & 1 \leq i \leq n \text{ and } i \text{ is odd} \\ 2m + \frac{n+i}{2}, & 1 \leq i \leq n \text{ and } i \text{ is even,} \end{cases}$$

$$f(u_i u_{i+1}) = 4m+2n-2i-1, 1 \leq i \leq m-1; f(u_i v_i) = 4m+2n-2i, 1 \leq i \leq m;$$

$$f(w_i w_{i+1}) = 2m+2n - i, 1 \leq i \leq n - 1 \text{ and } f(u_m u_1) = 4m+2n-1.$$

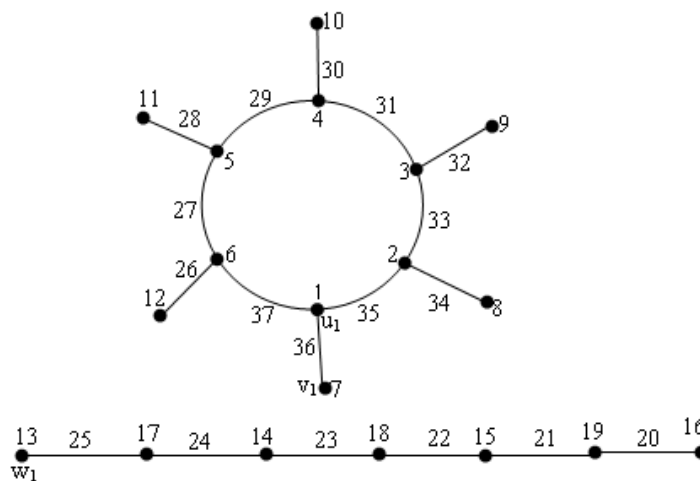
Now we can verify that for each edge  $uv \in E$ , the value of  $f(u)+f(uv)+f(v)$  yields any of the trimagic constants  $\lambda_1 = 4m+2n, \lambda_2 = 5m+2n$  and  $\lambda_3 = \frac{12m+5n+2}{2}$ .

By case 1 and case 2, the graph  $(C_m \odot K_1) \cup P_n$  admits an edge trimagic total labeling for all  $m$  and  $n$ .

**Corollary 2.2:** The graph  $(C_m \odot K_1) \cup P_n$  admits a super edge trimagic total labeling.

**Proof:** We proved that the graph  $(C_m \odot K_1) \cup P_n$  admits an edge trimagic total labeling. The labeling given in the proof of Theorem 2.1, the vertices get labels  $1, 2, \dots, 2m+n$ . Since the graph  $(C_m \odot K_1) \cup P_n$  has  $2m+n$  vertices and all the vertices are labeled with smallest positive integers, the graph  $(C_m \odot K_1) \cup P_n$  admits a super edge trimagic total labeling.

**Example 2.3:** The super edge trimagic total labeling of  $(C_6 \odot K_1) \cup P_7$  is given in figure 1.



**Figure-1:**  $(C_6 \odot K_1) \cup P_7$  with  $\lambda_1 = 38, \lambda_2 = 44$  and  $\lambda_3 = 55$ .

**Theorem 2.4:**  $(C_m \odot K_1) \cup C_n$  admits an edge trimagic total labeling.

**Proof:** Let  $u_1 u_2 \dots u_m u_1$  be the cycle  $C_m$  and let  $v_i$  be the vertex which is joined to the vertex  $u_i$  of the cycle  $C_m$ ,  $1 \leq i \leq m$ . The resultant graph is  $C_m \odot K_1$ . Let  $w_1 w_2 \dots w_n w_1$  be the cycle  $C_n$ . Then  $G = (C_m \odot K_1) \cup C_n$  is a disconnected graph with  $2m + n$  vertices and  $2m + n$  edges.

Define a bijection  $f: V \cup E \rightarrow \{1, 2, \dots, 4m+2n\}$  such that,

**Case-1:**  $n$  is odd.

$$f(u_i) = i, 1 \leq i \leq m, f(v_i) = m + i, 1 \leq i \leq m,$$

$$f(w_i) = \begin{cases} 2m + \frac{i+1}{2}, 1 \leq i \leq n \text{ and } i \text{ is odd} \\ 2m + \frac{n+i+1}{2}, 1 \leq i \leq n \text{ and } i \text{ is even,} \end{cases}$$

$$f(u_i u_{i+1}) = 4m + 2n - 2i, 1 \leq i \leq m-1; f(u_i v_i) = 4m + 2n - 2i + 1, 1 \leq i \leq m;$$

$$f(w_i w_{i+1}) = 2m + 2n - i, 1 \leq i \leq n - 1, f(u_m u_1) = 4m + 2n \text{ and } f(w_n w_1) = 2m + 2n.$$

Now we can verify that for each edge  $uv \in E$ , the value of  $f(u) + f(uv) + f(v)$  yields any of the trimagic constants  $\lambda_1 = 4m + 2n + 1, \lambda_2 = 5m + 2n + 1$  and  $\lambda_3 = \frac{12m + 5n + 3}{2}$ .

**Case-2:**  $n$  is even.

$$f(u_i) = i, 1 \leq i \leq m, f(v_i) = m + i, 1 \leq i \leq m,$$

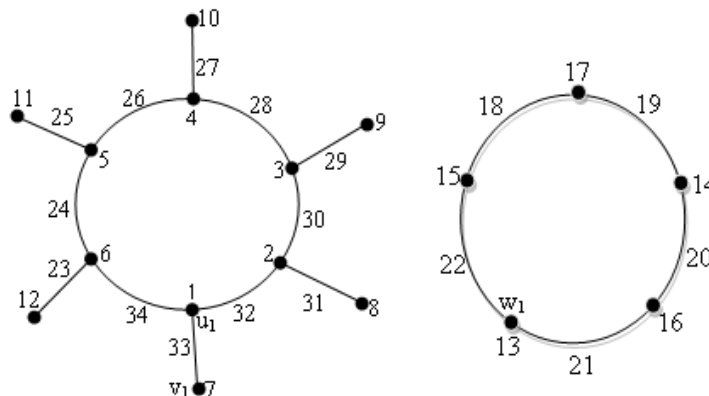
$$f(w_i) = \begin{cases} 2m + \frac{i+1}{2}, 1 \leq i \leq n \text{ and } i \text{ is odd} \\ 2m + \frac{n+i}{2}, 1 \leq i \leq n \text{ and } i \text{ is even,} \end{cases}$$

$$f(u_i u_{i+1}) = 4m + 2n - 2i, 1 \leq i \leq m-1; f(u_i v_i) = 4m + 2n - 2i + 1, 1 \leq i \leq m;$$

$$f(w_i w_{i+1}) = 2m + 2n - i, 1 \leq i \leq n - 1, f(u_m u_1) = 4m + 2n \text{ and } f(w_n w_1) = 2m + 2n.$$

Now we can verify that for each edge  $uv \in E$ , the value of  $f(u) + f(uv) + f(v)$  yields any of the trimagic constants  $\lambda_1 = 4m + 2n + 1, \lambda_2 = 5m + 2n + 1$  and  $\lambda_3 = \frac{12m + 5n + 2}{2}$ .

**Example 2.5:** The super edge trimagic total labeling of  $(C_6 \odot K_1) \cup C_5$  is given in figure 2.



**Figure-2:**  $(C_6 \odot K_1) \cup C_5$  with  $\lambda_1 = 35, \lambda_2 = 41$  and  $\lambda_3 = 50$ .

**Corollary 2.6:** The graph  $(C_m \odot K_1) \cup C_n$  admits a super edge trimagic total labeling.

**Proof:** We proved that the graph  $(C_m \odot K_1) \cup C_n$  admits an edge trimagic total labeling. The labeling given in the proof of Theorem 2.4, the vertices get labels  $1, 2, \dots, 2m+n$ . Since the graph  $(C_m \odot K_1) \cup C_n$  has  $2m+n$  vertices and all the vertices are labeled with smallest positive integers, the graph  $(C_m \odot K_1) \cup C_n$  admits a super edge trimagic total labeling.

**Theorem 2.7:** The graph  $P_m \cup P_n \cup P_r$  admits an edge trimagic total labeling.

**Proof:** Let  $V = \{u_i / 1 \leq i \leq m\} \cup \{v_j / 1 \leq j \leq n\} \cup \{w_k / 1 \leq k \leq r\}$  be the vertex set and  $E = \{u_i u_{i+1} / 1 \leq i \leq m-1\} \cup \{v_j v_{j+1} / 1 \leq j \leq n-1\} \cup \{w_k w_{k+1} / 1 \leq k \leq r-1\}$  be the edge set of the graph  $P_m \cup P_n \cup P_r$ . The disconnected graph  $P_m \cup P_n \cup P_r$  has  $m+n+r$  vertices and  $m+n+r-3$  edges.

Define a bijection  $f: V \cup E \rightarrow \{1, 2, \dots, 2m+2n+2r-3\}$  such that,

For all cases the edge labels are  $f(u_i u_{i+1}) = 2m+2n+2r-i-2, 1 \leq i \leq m-1,$

$$f(v_j v_{j+1}) = m+2n+2r-i-1, 1 \leq j \leq n-1 \text{ and } f(w_k w_{k+1}) = m+n+2r-k, 1 \leq k \leq r-1.$$

**Case-1:** m odd, n is even and r odd.

$$f(u_i) = \begin{cases} \frac{i+1}{2}, 1 \leq i \leq m \text{ and } i \text{ is odd} \\ \frac{m+i+1}{2}, 1 \leq i \leq m \text{ and } i \text{ is even,} \end{cases}$$

$$f(v_j) = \begin{cases} m + \frac{j+1}{2}, 1 \leq j \leq n \text{ and } j \text{ is odd} \\ m + \frac{n+j}{2}, 1 \leq j \leq n \text{ and } j \text{ is even,} \end{cases}$$

$$f(w_k) = \begin{cases} m+n + \frac{k+1}{2}, 1 \leq k \leq r \text{ and } k \text{ is odd} \\ m+n + \frac{r+k+1}{2}, 1 \leq k \leq r \text{ and } k \text{ is even,} \end{cases}$$

It is easy to verify that for each edge  $uv \in E$ , the value of  $f(u)+f(uv)+f(v)$  yields any of the trimagic constants  $\lambda_1 = \frac{5m+4n+4r-1}{2}, \lambda_2 = \frac{6m+5n+4r}{2}$  and  $\lambda_3 = \frac{6m+6n+5r+3}{2}$ . Therefore, the graph  $P_m \cup P_n \cup P_r$  admits an edge trimagic total labeling for odd m, even n and odd r.

**Case-2:** m, n and r are odd.

$$f(u_i) = \begin{cases} \frac{i+1}{2}, 1 \leq i \leq m \text{ and } i \text{ is odd} \\ \frac{m+i+1}{2}, 1 \leq i \leq m \text{ and } i \text{ is even,} \end{cases}$$

$$f(v_j) = \begin{cases} m + \frac{j+1}{2}, 1 \leq j \leq n \text{ and } j \text{ is odd} \\ m + \frac{n+j+1}{2}, 1 \leq j \leq n \text{ and } j \text{ is even,} \end{cases}$$

$$f(w_k) = \begin{cases} m+n + \frac{k+1}{2}, 1 \leq k \leq r \text{ and } k \text{ is odd} \\ m+n + \frac{r+k+1}{2}, 1 \leq k \leq r \text{ and } k \text{ is even,} \end{cases}$$

It is easy to verify that for each edge  $uv \in E$ , the value of  $f(u)+f(uv)+f(v)$  yields any of the trimagic constants  $\lambda_1 = \frac{5m+4n+4r-1}{2}, \lambda_2 = \frac{6m+5n+4r+1}{2}$  and  $\lambda_3 = \frac{6m+6n+5r+3}{2}$ . Therefore, the graph  $P_m \cup P_n \cup P_r$  admits an edge trimagic total labeling for m, n and r are odd.

**Case-3:** m, n odd and r even.

$$f(u_i) = \begin{cases} \frac{i+1}{2}, 1 \leq i \leq m \text{ and } i \text{ is odd} \\ \frac{m+i+1}{2}, 1 \leq i \leq m \text{ and } i \text{ is even,} \end{cases}$$

$$f(v_j) = \begin{cases} m + \frac{j+1}{2}, 1 \leq j \leq n \text{ and } j \text{ is odd} \\ m + \frac{n+j+1}{2}, 1 \leq j \leq n \text{ and } j \text{ is even,} \end{cases}$$

$$f(w_k) = \begin{cases} m+n + \frac{k+1}{2}, 1 \leq k \leq r \text{ and } k \text{ is odd} \\ m+n + \frac{r+k}{2}, 1 \leq k \leq r \text{ and } k \text{ is even,} \end{cases}$$

It is easy to verify that for each edge  $uv \in E$ , the value of  $f(u)+f(uv)+f(v)$  yields any of the trimagic constants  $\lambda_1 = \frac{5m+4n+4r-1}{2}$ ,  $\lambda_2 = \frac{6m+5n+4r+1}{2}$  and  $\lambda_3 = \frac{6m+6n+5r+2}{2}$ . Therefore, the graph  $P_m \cup P_n \cup P_r$  admits an edge trimagic total labeling for  $m, n$  odd and  $r$  even. .

**Case-4:**  $m$  odd and  $n, r$  even.

$$f(u_i) = \begin{cases} \frac{i+1}{2}, 1 \leq i \leq m \text{ and } i \text{ is odd} \\ \frac{m+i+1}{2}, 1 \leq i \leq m \text{ and } i \text{ is even,} \end{cases}$$

$$f(v_j) = \begin{cases} m + \frac{j+1}{2}, 1 \leq j \leq n \text{ and } j \text{ is odd} \\ m + \frac{n+j}{2}, 1 \leq j \leq n \text{ and } j \text{ is even,} \end{cases}$$

$$f(w_k) = \begin{cases} m+n + \frac{k+1}{2}, 1 \leq k \leq r \text{ and } k \text{ is odd} \\ m+n + \frac{r+k}{2}, 1 \leq k \leq r \text{ and } k \text{ is even,} \end{cases}$$

It is easy to verify that for each edge  $uv \in E$ , the value of  $f(u)+f(uv)+f(v)$  yields any of the trimagic constants  $\lambda_1 = \frac{5m+4n+4r-1}{2}$ ,  $\lambda_2 = \frac{6m+5n+4r-1}{2}$  and  $\lambda_3 = \frac{6m+6n+5r+2}{2}$ . Therefore, the graph  $P_m \cup P_n \cup P_r$  admits an edge trimagic total labeling for  $m$  odd and  $n, r$  even.

**Case-5:**  $m, n$  and  $r$  are even.

$$f(u_i) = \begin{cases} \frac{i+1}{2}, 1 \leq i \leq m \text{ and } i \text{ is odd} \\ \frac{m+i}{2}, 1 \leq i \leq m \text{ and } i \text{ is even,} \end{cases}$$

$$f(v_j) = \begin{cases} m + \frac{j+1}{2}, 1 \leq j \leq n \text{ and } j \text{ is odd} \\ m + \frac{n+j}{2}, 1 \leq j \leq n \text{ and } j \text{ is even,} \end{cases}$$

$$f(w_k) = \begin{cases} m+n + \frac{k+1}{2}, 1 \leq k \leq r \text{ and } k \text{ is odd} \\ m+n + \frac{r+k}{2}, 1 \leq k \leq r \text{ and } k \text{ is even,} \end{cases}$$

It is easy to verify that for each edge  $uv \in E$ , the value of  $f(u)+f(uv)+f(v)$  yields any of the trimagic constants  $\lambda_1 = \frac{5m+4n+4r-2}{2}$ ,  $\lambda_2 = \frac{6m+5n+4r-1}{2}$  and  $\lambda_3 = \frac{6m+6n+5r+2}{2}$ . Therefore, the graph  $P_m \cup P_n \cup P_r$  admits an edge trimagic total labeling for  $m, n$  and  $r$  are even.

**Case-6:**  $m, n$  even and  $r$  odd.

$$f(u_i) = \begin{cases} \frac{i+1}{2}, 1 \leq i \leq m \text{ and } i \text{ is odd} \\ \frac{m+i}{2}, 1 \leq i \leq m \text{ and } i \text{ is even,} \end{cases}$$

$$f(v_j) = \begin{cases} m + \frac{j+1}{2}, 1 \leq j \leq n \text{ and } j \text{ is odd} \\ m + \frac{n+j}{2}, 1 \leq j \leq n \text{ and } j \text{ is even,} \end{cases}$$

$$f(w_k) = \begin{cases} m+n + \frac{k+1}{2}, 1 \leq k \leq r \text{ and } k \text{ is odd} \\ m+n + \frac{r+k+1}{2}, 1 \leq k \leq r \text{ and } k \text{ is even,} \end{cases}$$

It is easy to verify that for each edge  $uv \in E$ , the value of  $f(u)+f(uv)+f(v)$  yields any of the trimagic constants  $\lambda_1 = \frac{5m+4n+4r-2}{2}$ ,  $\lambda_2 = \frac{6m+5n+4r-1}{2}$  and  $\lambda_3 = \frac{6m+6n+5r+3}{2}$ . Therefore, the graph  $P_m \cup P_n \cup P_r$  admits an edge trimagic total labeling for  $m, n$  even and  $r$  odd.

**Case-7:** m even and n, r odd.

$$f(u_i) = \begin{cases} \frac{i+1}{2}, & 1 \leq i \leq m \text{ and } i \text{ is odd} \\ \frac{m+i}{2}, & 1 \leq i \leq m \text{ and } i \text{ is even,} \end{cases}$$

$$f(v_j) = \begin{cases} m + \frac{j+1}{2}, & 1 \leq j \leq n \text{ and } j \text{ is odd} \\ m + \frac{n+j+1}{2}, & 1 \leq j \leq n \text{ and } j \text{ is even,} \end{cases}$$

$$f(w_k) = \begin{cases} m+n + \frac{k+1}{2}, & 1 \leq k \leq r \text{ and } k \text{ is odd} \\ m+n + \frac{r+k+1}{2}, & 1 \leq k \leq r \text{ and } k \text{ is even,} \end{cases}$$

It is easy to verify that for each edge  $uv \in E$ , the value of  $f(u)+f(uv)+f(v)$  yields any of the trimagic constants  $\lambda_1 = \frac{5m+4n+4r-2}{2}$ ,  $\lambda_2 = \frac{6m+5n+4r+1}{2}$  and  $\lambda_3 = \frac{6m+6n+5r+3}{2}$ . Therefore, the graph  $P_m \cup P_n \cup P_r$  admits an edge trimagic total labeling for m even and n, r odd.

**Case-8:** m even, n odd and r even.

$$f(u_i) = \begin{cases} \frac{i+1}{2}, & 1 \leq i \leq m \text{ and } i \text{ is odd} \\ \frac{m+i}{2}, & 1 \leq i \leq m \text{ and } i \text{ is even,} \end{cases}$$

$$f(v_j) = \begin{cases} m + \frac{j+1}{2}, & 1 \leq j \leq n \text{ and } j \text{ is odd} \\ m + \frac{n+j+1}{2}, & 1 \leq j \leq n \text{ and } j \text{ is even,} \end{cases}$$

$$f(w_k) = \begin{cases} m+n + \frac{k+1}{2}, & 1 \leq k \leq r \text{ and } k \text{ is odd} \\ m+n + \frac{r+k}{2}, & 1 \leq k \leq r \text{ and } k \text{ is even,} \end{cases}$$

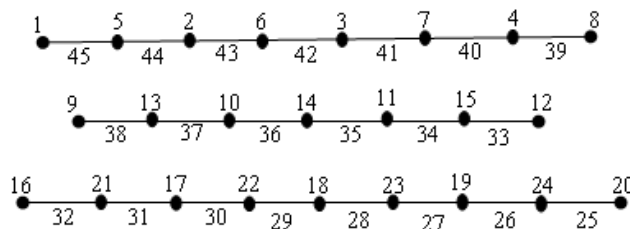
It is easy to verify that for each edge  $uv \in E$ , the value of  $f(u)+f(uv)+f(v)$  yields any of the trimagic constants  $\lambda_1 = \frac{5m+4n+4r-2}{2}$ ,  $\lambda_2 = \frac{6m+5n+4r+1}{2}$  and  $\lambda_3 = \frac{6m+6n+5r+3}{2}$ . Therefore, the graph  $P_m \cup P_n \cup P_r$  admits an edge trimagic total labeling for m even and n, r odd.

The above cases prove that the graph  $P_m \cup P_n \cup P_r$  admits an edge trimagic total labeling for all m, n and r.

**Corollary 2.8:** The graph  $P_m \cup P_n \cup P_r$  admits a super edge trimagic total labeling.

**Proof:** We proved that the graph  $P_m \cup P_n \cup P_r$  admits an edge trimagic total labeling. The labeling given in the proof of Theorem 2.7, the vertices get labels 1, 2, ..., m+n+r. Since the graph  $P_m \cup P_n \cup P_r$  has m+n+r vertices and all the vertices are labeled with smallest positive integers, the graph  $P_m \cup P_n \cup P_r$  admits a super edge trimagic total labeling.

**Example 2.9:** The super edge trimagic total labeling of  $P_8 \cup P_7 \cup P_9$  is given in figure 3.



**Figure-3:**  $P_8 \cup P_7 \cup P_9$  with  $\lambda_1 = 51$ ,  $\lambda_2 = 60$  and  $\lambda_3 = 69$ .

### 3. CONCLUSION

Here we presented some results concerning edge trimagic total labeling and super edge trimagic total labeling for disconnected graphs  $(C_m \odot K_1) \cup P_n$ ,  $(C_m \odot K_1) \cup C_n$  and  $P_m \cup P_n \cup P_r$ . However, there are many graphs which were not been studied. We believe that these results can be extended to vertex trimagic total labeling of graphs.

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**Source of support: Nil, Conflict of interest: None Declared**

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