

SPLIT GEODETIC NUMBER OF A LICT GRAPH

VENKANAGOUDA M GOUDAR

Department of Mathematics,
Sri Siddhartha Institute of Technology, Tumkur, Karnataka, India.

TEJASWINI K.M*

Research Scholar, Sri Gauthama Research Centre, (Affiliated to Kuvempu University),
Sri Siddhartha Institute of Technology, Tumkur, Karnataka, India.

VENKATESHA

Department of Mathematics, Kuvempu University
Shankarghatta, Shimoga, Karnataka, India.

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ABSTRACT

A set $S \subseteq V[\eta(G)]$ is a split geodetic set of (G) , if S is a geodetic set and $\langle V - S \rangle$ is disconnected. The split geodetic number of a lict graph $\eta(G)$, is denoted by $g_s[\eta(G)]$, is the minimum cardinality of a split geodetic set of $\eta(G)$. In this paper we obtain the split geodetic number of lict graph of any graph. Also obtain many bounds on split geodetic number in terms of elements of G and covering number of G . We investigate the relationship between split geodetic number and geodetic number.

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I. INTRODUCTION

In this paper we follow the notations of [3]. As usual $n = |V|$ and $m = |E|$ denote the number of vertices and edges of a graph G respectively. The graphs considered here are undirected and non complete. For any graph $G = (V, E)$, the lict graph $\eta(G)$ whose vertices correspond to the edges of G and two vertices in $\eta(G)$ are adjacent if and only if the corresponding edges in G are adjacent. The distance $d(u, v)$ between two vertices u and v in a connected graph G is the length of a shortest $u - v$ path in G . It is well known that this distance is a metric on the vertex set $V(G)$. For a vertex v of G , the eccentricity $e(v)$ is the distance between v and a vertex farthest from v . The minimum eccentricity among the vertices of G is radius, $rad G$, and the maximum eccentricity is the diameter, $diam G$. A $u - v$ path of length $d(u, v)$ is called a $u - v$ geodesic. We define $I[u, v]$ to the set (interval) of all vertices lying on some $u - v$ geodesic of G and for a nonempty subset S of $V(G)$, $I[S] = \cup_{u, v \in S} I[u, v]$.

A set S of vertices of G is called a geodetic set in G if $I[S] = V(G)$, and a geodetic set of minimum cardinality is a minimum geodetic set. The cardinality of a minimum geodetic set in G is called the geodetic number of G , and we denote it by $g(G)$.

A vertex v is an extreme vertex in a graph G , if the subgraph induced by its neighbours is complete. A vertex cover in a graph G is a set of vertices that covers all edges of G . The minimum number of vertices in a vertex cover of G is the vertex covering number $\alpha_0(G)$ of G . An edge cover of a graph G without isolated vertices is a set of edges of G that covers all the vertices of G . The edge covering number $\alpha_1(G)$ of a graph G is the minimum cardinality of an edge cover of G .

*Corresponding Author: TEJASWINI K.M**

*Research Scholar, Sri Gauthama Research Centre, (Affiliated to Kuvempu University),
Sri Siddhartha Institute of Technology, Tumkur, Karnataka, India.*

Split geodetic number of a graph was studied by in [5]. A geodetic set S of a graph $G = (V, E)$ is a split geodetic set if the induced subgraph $\langle V - S \rangle$ is disconnected. The split geodetic number $g_s(G)$ of G is the minimum cardinality of a split geodetic set. Geodetic number of a lict graph was studied by in [4]. Geodetic number of a lict graph $\eta(G)$ of G is a set S' of vertices of $\eta(G) = H$ is called the geodetic set in H if $I[S'] = V(H)$ and a geodetic set of minimum cardinality is the geodetic number of $\eta(G)$ and is denoted by $g[\eta(G)]$. Now we define split geodetic number of a lict graph. A set S' of vertices of $\eta(G) = H$ is called the split geodetic set in H if the induced subgraph $V(H) - S'$ is disconnected and a split geodetic set of minimum cardinality is the split geodetic number of $\eta(G)$ and is denoted by $g_s[\eta(G)]$.

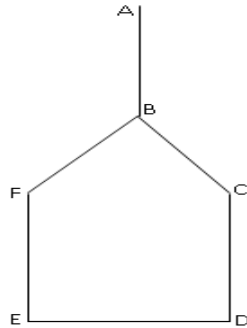


Figure 1.0(a)

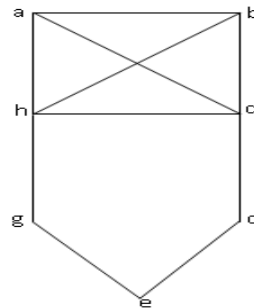


Figure 1.0(b)

For the graph G given in Figure 4.2.1(a), $S = \{A, D, E\}$ is a minimum geodetic set so that $g(G) = 3$ and $S_1 = \{A, D, B, E\}$ is a minimum split geodetic set so that $g_s(G) = 4$. For the graph $\eta(G)$ given in Figure 1.0(b), $S' = \{a, b, e\}$ is a minimum geodetic set so that $g[\eta(G)] = 3$ and $S_2 = \{a, b, e, h\}$ is a minimum split geodetic set so that $g_s[\eta(G)] = 4$.

II. PRELIMINARY NOTES

We need the following results to prove further results.

Theorem 2.1: [1] Every geodetic set of a graph contains its extreme vertices.

Theorem 2.2: [2] For any path P_n of order n , the edge covering number

$$\alpha_1(P_n) = \begin{cases} \frac{n}{2} & \text{if } n \text{ is even} \\ \frac{n+1}{2} & \text{if } n \text{ is odd} \end{cases}$$

Theorem 2.3: [1] Let G be a connected graph of order at least 3. If G contains a minimum geodetic set S with a vertex x such that every vertex of G lies on some $x - w$ geodesic in G for some $w \in S$, then $g(G) = g(G \times K_2)$.

Theorem 2.4: [5] For any graph G , $g(G) \leq g_s(G)$.

III. MAIN RESULTS

Theorem 3.1: For any tree T of order n , $g_s[\eta(T)] = n + 1$.

Proof: Let S be the set of all extreme vertices of a lict graph $\eta(T)$ of a tree T . Let v_i be a cut vertex in $V - S$ and $S' = S \cup \{v_i\}$, by Theorem 2.1 $g_s[\eta(T)] \geq |S'|$. On the other hand, for an internal vertex v of $\eta(T)$, there exists x, y of $\eta(T)$ such that v lies on the unique $x - y$ geodesic in $\eta(T)$. By the definition of lict graph pendant vertices and cut vertices of T are the extreme vertices of $\eta(T)$ and the induced subgraph $V[\eta(T)] - S'$ is a split geodetic set of $\eta(T)$. Thus $g_s[\eta(T)] \leq |S'|$. Also, every split geodetic set S_1 of $\eta(T)$ must contain S' which is the unique minimum split geodetic set. Therefore $|S'| = |S_1| = |S| + |v_i| = n + 1$. Hence $g_s[\eta(T)] = n + 1$.

Corollary 3.2: For any path P_n , $n \geq 6$, $g_s[\eta(P_n)] = n + 1$.

Proof: Clearly the set of two pendant vertices of a path P_n is its unique geodetic set. From Theorem 3.1 the results follow.

Theorem 3.3: For any graph G of order n , $g_s[\eta(G)] \leq n$.

Proof: Let S be the geodetic set of $\eta(G)$ such that $\langle V - S \rangle$ is connected. So S is not a split geodetic set of $\eta(G)$. Now, we consider a set $S' = S \cup \{v_i\}$ where v_i be the vertex in $\langle V - S \rangle$ and is adjacent to at least one vertex in S . Thus $\langle V - S' \rangle$ is a split geodetic set of $\eta(G)$. Therefore $g_s[\eta(G)] \leq n$.

Theorem 3.4: For any path P_n , $n \geq 6$, $g_s[\eta(P_n)] = d + \Delta$ where Δ be the maximum degree and d be the diameter.

Proof: Since the set of two pendant vertices of a path is its unique geodetic set, the distance between those vertices is the diameter i.e $d(u, v) = 1n = d$ and the maximum degree of vertices in path is $\Delta = 2$. Clearly, it follows that $g_s[\eta(P_n)] = n - 1 + 2 = d + \Delta$.

Theorem 3.5: For any graph G of order n , $g_s[\eta(G)] > m - \alpha_1(G) + 1$. Where α_1 is the edge covering number.

Proof: Suppose $S = \{e_1, e_2, \dots, e_k\}$ be the set of all pendant edges in G . Then $S \cup J$ where $J \subseteq E(G) - S$, be the minimal set of edges which covers all the vertices of G such that $|S \cup J| = \alpha_1(G)$. Now without loss of generality in $\eta(G)$, let $I = \{u_1, u_2, \dots, u_p\} \subseteq V[\eta(G)]$ be the set of vertices in $\eta(G)$ formed by the pendant vertices and cut vertices in G . Suppose $H = \{u_1, u_2, \dots, u_j\} \subseteq V[\eta(G)] - I$. Then $I \cup \{u_j\}$, where $u_j \in H$, forms a minimum split geodetic set of $\eta(G)$. Clearly it follows that $|I \cup \{u_j\}| > |E(G)| - |S \cup J| + 1$. Therefore $g_s[\eta(G)] > m - \alpha_1(G) + 1$.

Theorem 3.6: For any graph G of order n , $g_s[\eta(G)] \leq 3\alpha_0(G) + 1$.

Proof: Let S be a minimum set of vertices in G . Then S has at least two vertices and every vertex in S adjacent to some vertex in $\langle V - S \rangle$. Thus $\langle V - S \rangle$ is disconnected. Hence S is a split geodetic set of $\eta(G)$. Hence $g_s[\eta(G)] \leq 3\alpha_0(G) + 1$.

Theorem 3.7: For any graph G of order n , $g_s[\eta(G)] < n_1 - k[\eta(G)]$, where n_1 be the number of vertices in $\eta(G)$ and $k[\eta(G)]$ is a vertex connectivity.

Proof: Let $k(G) = k$. Since $\eta(G)$ is connected and each block is complete, $l \leq k(G) \leq n_1 - 2$. Let $U = \{u_1, u_2, \dots, u_k\}$ be a minimum cutset of G , G_1, G_2, \dots, G_r ($r \geq 2$) be the components of $G - U$ and let $W = V[\eta(G)] - U$ then every vertex u_i ($1 \leq i \leq k$) is adjacent to at least one vertex of G_j for every ($i \leq j \leq r$). Therefore, every vertex u_i belongs to a W geodesic path. Thus $g_s[\eta(G)] < n_1 - k[\eta(G)]$.

Theorem 3.8: For any tree G of order n and diameter d then $g_s[\eta(G)] \leq n + d - 2$.

Proof: Let $S = \{v_1, v_2, \dots, v_i, u_1, u_2, \dots, u_j\}$ be the geodetic set of $\eta(G)$ such that v_1, v_2, \dots, v_i be the set of vertices in $\eta(G)$ corresponding to the pendant edges of G and also $u_1, u_2, \dots, u_j \in \eta(G)$ corresponds to the cut vertices of G . Now, consider a set $S' = S \cup w_k$, where $w_k \in \langle v[\eta(G)] - S \rangle$. Hence $\langle v[\eta(G)] - S' \rangle$ be a split geodetic set of $\eta(G)$. It follows that $|S'| = |S| + 1$. Hence $g_s[\eta(G)] \leq n + d - 2$.

Theorem 3.9: For any graph G of order n , $g_s[\eta(G)] \leq \alpha_1[\eta(G)] + 4$.

Proof: Let S be the minimum set of edges covers all the vertices in $\eta(G)$. Then S has at least two vertices and every vertex in S is adjacent to some vertex in $\langle V[\eta(G)] - S \rangle$. Thus $\langle V[\eta(G)] - S \rangle$ is disconnected. Hence S is a split geodetic set of $\eta(G)$. Hence $g_s[\eta(G)] \leq \alpha_1[\eta(G)] + 4$.

Theorem 3.10: For any graph G of order n , $g[\eta(G)] + g_s[\eta(G)] > n$.

Proof: Let $S = \{v_1, v_2, \dots, v_n\} \subseteq V[\eta(G)]$ be the minimum split geodetic set of $\eta(G)$. Now without loss of generality in $\eta(G)$, if $F = \{u_1, u_2, \dots, u_p\}$ be the set of all extreme vertices in $\eta(G)$. Then $F \cup I$ where $I \subseteq V[\eta(G)] - F$ forms a minimum split geodetic set of $\eta(G)$. Clearly, $|S \cup I \cup F \cup H| > n$. Therefore, $g[\eta(G)] + g_s[\eta(G)] > n$.

IV. ADDING AN PENDANT EDGE

Definition: For an edge $e = \{u, v\}$ of a graph G with $\deg(u) = 1$ and $\deg(v) > 1$, we call e an pendant edge and u an pendant-vertex. Let G' be the graph obtained by adding an pendant-edge $\{u, v\}$ to a cycle $C_n = G$ of order $n \geq 5$, with $u \in G$ and $v \notin G$.

Let G' be the graph obtained by adding pendant edge (u_i, v_j) , $i = 1, 2 \dots n$, $j = 1, 2, \dots, k$ to each vertex of G of order $n \geq 5$ such that $u_i \in G$, $v_j \notin G$.

Theorem 4.1: G' be the graph obtained by adding k pendant edges $\{(u, v_1), (u, v_2), \dots, (u, v_k)\}$ to a cycle $C_n = G$ of order $n \geq 5$, with $u \in G$ and $\{v_1, v_2, \dots, v_k\} \notin G$. Then

$$g_s[\eta(G')] = \begin{cases} K + 4 & \text{if } n \text{ is even} \\ k + 3 & \text{if } n \text{ is odd} \end{cases}$$

Proof: Let $\{e_1, e_2, \dots, e_n, e_1\}$ be a cycle with n vertices and let G' be the graph obtained from $G = C_n$ by adding pendant edges (u, v_i) , $i = 1, 2, \dots, k$. Such that $u \in G$ and $v_i \notin G$.

Case-1: Consider n is even.

By the definition of lict graph, $\eta(G')$ as an $\langle K_{k+3} \rangle$ as an induced subgraph. Also the edges $(u, v_i) = e_i, i = 1, 2, \dots, k$ and the cut vertices u_i becomes the vertices of $\eta(G')$ and these belongs to some geodetic set of $\eta(G')$. Hence $\{e_1, e_2, \dots, e_k, e_l, e_m, u_i\}$ are the vertices of $\eta(G')$ where e_l, e_m are the edges incident on the antipodal vertex of u in G' and these vertices belongs to some geodetic set of $\eta(G')$, also $\eta(G') = C_n \cup K_{k+3}$. Let $S = \{e_1, e_2, \dots, e_k, e_l, e_m, u_i\}$ be the geodetic set of $\eta(G')$. Since $V[\eta(G')] - S$ is connected, we consider a set $S' = S \cup e_j$ where e_j be the edge incident on the cut vertex of G' . Such that $V[\eta(G')] - S'$ is disconnected. So S' is the minimum split geodetic set of $\eta(G')$. Therefore $g_s[\eta(G')] = k + 4$.

Case-2: Consider n is odd.

By the definition of lict graph, $\eta(G')$ has $\langle K_{k+3} \rangle$ as an induced subgraph, also the edges $(u, v_i) = \{e_1, e_2, \dots, e_k\}$ becomes vertices of $\eta(G')$. Let $e_l = (a, b) \in G$ such that $d(u, a) = d(u, b)$ in the graph $\eta(G')$. Let $S = \{e_1, e_2, \dots, e_k, e_l\}$ be the geodetic set of $\eta(G')$.

Now, consider a set $S' = S \cup \{e_j\}$ is a split geodetic set of $\eta(G')$ where e_j is the vertex from $V[\eta(G')] - S$ having $\deg = 2$. It is clear that S' is the minimum split geodetic set of $\eta(G')$. Therefore $g_s[\eta(G')] = k+3$.

Theorem 4.2: Let G' be the graph obtained by adding pendant edge $(u_i, v_j), i = 1, 2, \dots, n, j = 1, 2, \dots, k$ to each vertex of $G = C_n$ of order $n \geq 5$ such that $u_i \in G, v_j \notin G$. Then, $g_s[\eta(G')] = n_1 + 2$, where n_1 be the number of vertices in G' .

Proof: Let $\{e_1, e_2, \dots, e_n, e_1\}$ be a cycle with n vertices and $G = C_n$. Let G' be the graph obtained by adding pendant vertex $(u_i, v_j), i = 1, 2, \dots, n, j = 1, 2, \dots, k$ to each vertex of G , such that $u_i \in G, v_j \notin G$. Clearly k be the number of end vertices of G' . By the definition of lict graph $\eta(G')$ have n copies of K_4 as an induced subgraph. The edges $(u_i, v_j) = e_j$ for all j and u_i becomes vertices of $\eta(G')$ and those lies on geodetic set of $\eta(G')$. Since they forms the extreme vertices of $\eta(G')$. By Theorem 2.1 $S = \{e_1, e_2, \dots, e_k, u_1, u_2, \dots, u_i\}$ forms geodetic set. Now consider any two vertices $\{e_l, e_m\} \in V - S$ which are not adjacent. $S' = \{e_1, e_2, \dots, e_k, u_1, u_2, \dots, u_i, e_l, e_m\}$ forms a split geodetic set of S' . Suppose $P = \{e_1, e_2, \dots, e_k, u_1, u_2, \dots, u_i, e_l\}$ be the set of vertices of $\eta(G')$, such that $|P| < |S'|$, then $V - P$ is connected. Hence it is clear that S' is the minimum split geodetic set of S' . Therefore $g_s[\eta(G')] = n_1 + 2$.

Theorem 4.3: Let G' be the graph obtained by adding k end edges $\{(u, v_1), (u, v_2), \dots, (u, v_k)\}$ to a cycle $C_n = G$ of order $n \geq 5$, with $u \in G$ and $\{v_1, v_2, \dots, v_k\} \notin G$. Then $g_s[\eta(G')] \leq \alpha_1[\eta(G')]$, where α_1 be the edge covering number of G' .

Proof: Let S be the minimum set of edges which covers all the vertices in $\eta(G')$. Then S has at least two vertices and every vertex in S is adjacent to some vertex in $(V[\eta(G')] - S)$. Thus $(V[\eta(G')] - S)$ is disconnected. Hence S is a split geodetic set of $\eta(G')$. Hence $g_s[\eta(G')] \leq \alpha_1[\eta(G')]$.

Theorem 4.4: Let G' be the graph obtained by adding pendant edge $(u_i, v_j), i = 1, 2, \dots, n, j = 1, 2, \dots, k$ to each vertex of $G = C_n$ of order $n \geq 5$, such that $u_i \in G, v_j \notin G$. Then $g_s[\eta(G')] = \alpha_1[\eta(G')] + 4$, where α_1 be the edge covering number of $\eta(G')$.

Proof: Let S be the minimum set of edges which covers all the vertices in $\eta(G')$. Then S has at least two vertices and every vertex in S is adjacent to some vertex in $(V[\eta(G')] - S)$. Thus $(V[\eta(G')] - S)$ is disconnected. Hence S is a split geodetic set of $\eta(G')$. Hence $g_s[\eta(G')] = \alpha_1[\eta(G')] + 4$.

Theorem 4.5: Let G' be the graph obtained by adding k pendant edges $\{(u, v_1), (u, v_2), \dots, (u, v_k)\}$ to a cycle $C_n = G$ of order $n \geq 5$, with $u \in G$ and $\{v_1, v_2, \dots, v_k\} \notin G$. Then $g_s[\eta(G')] < n_1 - \kappa(G')$, where $\kappa(G')$ be the vertex connectivity of G' .

Proof: Let $\kappa(G') = k$. Since G' is connected but not complete. Let u_k be a cutset of G' and $G_1, G_2, \dots, G_r, r \geq 2$ be the components of $G - u_k$ and let $P = V(G') - u_k$ then every vertex is adjacent to at least one vertex of $G_j (1 \leq j \leq r)$. Therefore every vertex u_i belongs to some geodetic set. Hence $g_s[\eta(G')] < n_1 - \kappa(G')$.

V. CARTESIAN PRODUCT

The Cartesian product of the graphs H_1 and H_2 , written as $H_1 \times H_2$, is the graph with vertex set $V(H_1) \times V(H_2)$, two vertices u_1, u_2 and v_1, v_2 being adjacent in $H_1 \times H_2$ if and only if either $u_1 = v_1$ and $(u_2, v_2) \in E(H_2)$, or $u_2 = v_2$ and $(u_1, v_1) \in E(H_1)$.

Theorem 5.1: For any path P_n of order n , $g_s[K_3 \times \eta(P_n)] = n + 2$.

Proof: By the definition of lict graph $\eta(P_n) = K_3, K_3, \dots, (n - 2)$ factors ($n \geq 3$). Consider $G = \eta(P_n)$, let $K_3 \times G$ be the graph formed from three copies G_1, G_2 and G_3 of G and S be a minimum geodetic set of $K_3 \times G$. Now, we define S' be the union of those vertices of G belonging to S . Let $v \in V(G_1)$ lies on some $x - y$ geodesic for any $x, y \in S$. Since S is a geodetic set by the Theorem 2.1 we have $g[\eta(P_n)] = n$ at least one of x and y belongs to V_1 . If both $x, y \in V_1$, then $x, y \in S'$. Hence we may assume that $x \in V_1$ and $y \in V_2$. If corresponds to x then $v = x \in S'$ where $y \neq x$. Since $d(x, y) = d(x, y') + 1$ and the vertex v lies on an $x - y$ geodesic in $K_3 \times G$. Let S contains a vertex x with the property that every vertex of G_1 lies on an $x - w$ geodesic in G_1 for some $w \in S$. Let S' consists of x together with those vertices of G_3 and G_2 corresponding to those vertices in $S - x$. Thus $|S'| = |S| \cup \{a, b\}$ where $\{a, b\}$ be the vertices in G_3 and G_2 . Hence, S' is a split geodetic set of $K_3 \times G$.

$$\begin{aligned} \text{Therefore } |S'| &= g[\eta(P_n)] + \{a, b\} \\ \Rightarrow g_s[K_3 \times G] &= n + 2 \\ \Rightarrow g_s[K_3 \times [\eta(P_n)]] &= n + 2. \end{aligned}$$

Theorem 5.2: For any path P_n of order n , then

$$g_s[K_3 \times [\eta(P_n)]] = \begin{cases} 2\alpha_1(P_n) + 1 & \text{if } n \text{ is even} \\ 2\alpha_1(P_n) + 2 & \text{if } n \text{ is odd} \end{cases}, \text{ where } \alpha_1 \text{ be the edge covering number.}$$

Proof: Let $\alpha_1(P_n)$ be a edge covering of a graph is a minimum cardinality of an edge cover of a path P_n . We have the following cases.

Case-1: Suppose n is odd, we have $\alpha_1(P_n) = \frac{n+1}{2}$

$$\Rightarrow 2\alpha_1(P_n) = n+1$$

$$\begin{aligned} \text{Since } g_s[K_3 \times \eta(G')] &= n + 2 \\ \Rightarrow g_s[K_3 \times \eta(G')] &= n+1 + 1 \end{aligned}$$

$$\Rightarrow g_s[K_3 \times \eta(G')] = 2\alpha_1(P_n) + 1.$$

Case-2: Suppose n is even, we have $\alpha_1(P_n) = \frac{n}{2}$

$$\Rightarrow 2\alpha_1(P_n) = n$$

$$\begin{aligned} \text{Since } g_s[K_3 \times \eta(G')] &= n + 2 \\ \Rightarrow g_s[K_3 \times \eta(G')] &= 2\alpha_1(P_n) + 2. \end{aligned}$$

Theorem 5.3: For any path P_n of order n , $g_s[K_3 \times [\eta(P_n)]] \leq 3\alpha_0(P_n) + 1$, where α_0 is a vertex covering number.

Proof: Let S be a minimum set of vertices in P_n . Then S has at least two vertices and every vertex in S adjacent to some vertex in $(V - S)$. Thus $(V - S)$ is disconnected. Hence S is a split geodetic set of $K_3 \times \eta(P_n)$.

$$\text{Hence } g_s[K_3 \times [\eta(P_n)]] \leq 3\alpha_0(P_n) + 1.$$

Corollary 5.4: For any path P_n of order n , $g_s[K_3 \times \eta(P_n)] > g_{ns}[K_3 \times \eta(P_n)]$.

Proof: Proof follows from the above Theorem.

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