



## SOME COMMON FIXED POINT THEOREMS FOR OCCASIONALLY WEAKLY COMPATIBLE MAPPINGS IN FUZZY METRIC SPACES

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(Received on: 30-05-11; Accepted on: 09-06-11)

### ABSTRACT

*In this paper we prove some common fixed point theorem for occasionally weakly compatible mapping in fuzzy metric spaces by taking average of some elements.*

**Keywords:** Occasionally weakly compatible (owc) mappings, fuzzy metric space.

### 1. INTRODUCTION:

Fuzzy set was defined by Zadeh [26]. Kramosil and Michalek [14] introduced fuzzy metric space, Gorge and Veermani [6] modified the notion of fuzzy metric spaces with the help of continuous t-norms. Many researchers have obtained common fixed point theorems for mappings satisfying different types of commutativity conditions. Vasuki [25] proved fixed point theorems for R-weakly commuting mappings. Pant [18, 19, 20] introduced the new concept reciprocally continuous mappings and established some common fixed point theorems. Balasubramaniam et al. [4], have shown that Rhoades [22] open problem on the existence of contractive definition which generates a fixed point but does not force the mappings to be continuous at the fixed point. Poses an affirmative answer. Pant and Jha [20] obtained some analogous results proved by Balasubramaniam et al. Recent literature in fixed point in fuzzy metric space can be viewed in [1, 2, 9, 16, 24].

This paper presents some common fixed point theorems for more general commutative condition i.e. occasionally weakly compatible mappings in fuzzy metric space by taking average of some elements.

### 2 PRELIMINARY NOTES:

**Definition: 2.1** [12] A fuzzy set A in X is a function with domain X and values in [0, 1].

**Definition: 2.2** [4] A binary operation  $*$  :  $[0, 1] \times [0, 1] \rightarrow [0, 1]$  is a continuous t-norms if it satisfies the following conditions:

- (i)  $*$  is associative and commutative;
- (ii)  $*$  is continuous;
- (iii)  $a * 1 = a$  for all  $a \in [0, 1]$ ;
- (iv)  $a * b \leq c * d$  whenever  $a \leq c$  and  $b \leq d$ , and  $a, b, c, d \in [0, 1]$ .

**Definition: 2.3** [2] A 3-tuples  $(X, M, *)$  is said to be a fuzzy metric space (shortly FM Space) if X is an arbitrary set,  $*$  is a continuous t-norm and M is a fuzzy set of  $X^2 \times (0, \infty)$  satisfying the following conditions, for all  $x, y, z \in X$  and  $s, t > 0$ ;

- (FM 1):  $M(x, y, t) > 0$ ;
- (FM 2):  $M(x, y, t) = 1$  for all  $t > 0$  if and only if  $x = y$ ;
- (FM 3):  $M(x, y, t) = M(y, x, t)$ ;

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(FM 4):  $M(x, y, t) * M(y, z, s) \leq M(x, z, t + s)$ ;

(FM 5):  $M(x, y, \cdot) : (0, \infty) \rightarrow (0, 1]$  is left continuous.

$(X, M, *)$  denotes a fuzzy metric space,  $M(x, y, t)$  can be thought of as degree of nearness between  $x$  and  $y$  with respect to  $t$ . We identify  $x = y$  with  $M(x, y, t) = 1$  for all  $t > 0$ . In the following example every metric induces a fuzzy metric.

**Example: 2.4** (Induced fuzzy metric [6]) Let  $(X, d)$  be a metric space. Denote  $a * b = a.b$  & for all  $a, b \in [0, 1]$  and let  $M_d$  be fuzzy sets on  $X^2 \times (0, \infty)$  defined as follows.

$$M_d(x, y, t) = \frac{t}{t + d(x, y)}$$

Then  $(X, M, *)$  is a fuzzy metric space. We call this fuzzy metric induced by a metric  $d$  as the standard intuitionistic fuzzy metric.

**Definition: 2.5** [8] Two self mappings  $f$  and  $g$  of a fuzzy metric space  $(X, M, *)$  are called compatible if  $\lim_{n \rightarrow \infty} M(fg x_n, gf x_n, t) = 1$  wherever  $\{x_n\}$  is sequence in  $X$  such that

$$\lim_{n \rightarrow \infty} f x_n = \lim_{n \rightarrow \infty} g x_n = x \text{ for some } x \text{ in } X$$

**Definition: 2.6** [24] Two self maps  $f$  and  $g$  of a fuzzy metric space  $(X, M, *)$  are called reciprocally continuous on  $X$  if  $\lim_{n \rightarrow \infty} f x_n = fx$  and  $\lim_{n \rightarrow \infty} gf x_n = gx$  wherever,  $\{x_n\}$  is sequence in  $X$  such that

$$\lim_{n \rightarrow \infty} f x_n = \lim_{n \rightarrow \infty} g x_n = x \text{ for some } x \text{ in } X.$$

**Definition: 2.7** [6] Let  $(X, M, *)$  be a fuzzy metric space. Then

- (a) A sequence  $\{x_n\}$  in  $X$  is said to converges to  $x$  in  $X$  if for each  $\epsilon > 0$  and each  $t > 0$ , there exist  $n_0 \in \mathbb{N}$  such that  $M(x_n, x, t) > 1 - \epsilon$  for all  $n \geq n_0$ .
- (b) A sequence  $\{x_n\}$  in  $X$  is said to be Cauchy if for each  $\epsilon > 0$  and each  $t > 0$ , there exist  $n_0 \in \mathbb{N}$  such that  $M(x_n, x_m, t) > 1 - \epsilon$  for all  $n, m \geq n_0$ .
- (c) A fuzzy metric space in which every Cauchy sequence is convergent is said to be complete.

**Definition: 2.8** Two self maps  $f$  and  $g$  of a set  $X$  are occasionally weakly compatible (owc) iff there is a point  $x$  in  $X$  which is a coincidence point of  $f$  and  $g$  at which  $f$  and  $g$  commute. A.Al-Thagafi and Naseer Shahzad [15] shown that occasionally weakly is weakly compatible but converse is not true.

**Example: 2.9** Let  $R$  be the usual metric space. Define  $S, T: R \rightarrow R$  by  $Sx = 3x$  and  $Tx = x^2$  for all  $x \in R$ . Then  $Sx = Tx$  for  $x = 0, 3$  but  $ST0 = TS0$ , and  $ST3 \neq TS3$ . Hence  $S$  and  $T$  are occasionally weakly compatible self maps but not weakly compatible.

**Example: 2.10** [3] Let  $R$  be the usual metric space. Define  $S, T: R \rightarrow R$  by  $Sx = 2x$  and  $Tx = x^2$  for all  $x \in R$ . Then  $Sx = Tx$  for  $x = 0, 2$ , but  $ST0 = TS0$ , and  $ST2 \neq TS2$ . Hence  $S$  and  $T$  are occasionally weakly compatible self maps but not weakly compatible.

**Lemma: 2.11** [12] Let  $X$  be a set and  $f, g$  owc self maps of  $X$ . If  $f$  and  $g$  have a unique point of coincidence,  $w = fx = gx$ , then  $w$  is the unique common fixed point of  $f$  and  $g$ .

**Lemma: 2.12** Let  $(X, M, *)$  be a fuzzy metric space. If then exist  $q \in (0, 1)$  such that

$$M(x, y, qt) \geq M(x, y, t) \text{ for all } x, y \in X \text{ \& } t > 0 \text{ then } x = y.$$

### 3 MAIN RESULTS:

#### Theorem: 3.1

Let  $(X, M, *)$  be a complete fuzzy metric space and let  $P, Q, S$  and  $T$  are self-mapping of  $X$ . Let the pairs  $\{P, S\}$  and  $\{Q, T\}$  be owc. If there exists  $q \in (0, 1)$  such that

$$M(Px, Qy, qt) \geq \min\left\{\frac{M(Sx, Ty, t) + M(Px, Ty, t) + M(Qy, Sx, t)}{3}, M(Sx, Px, t), M(Qy, Ty, t)\right\} \quad (1)$$

for all  $x, y \in X$  and for all  $t > 0$ , then there exists a unique point  $w \in X$  such that  $Pw = Sw = w$  and a unique point  $z \in X$  such that  $Qz = Tz = z$ . Moreover,  $z = w$ , so that there is a unique common fixed point of  $P, Q, S$  and  $T$ .

**Proof:** Let the pairs  $\{P, S\}$  and  $\{Q, T\}$  be owc so there are points  $x, y \in X$  such that  $Px = Sx$  and  $Qy = Ty$ . We claim that  $Px = Qy$ . If not by inequality (1)

$$\begin{aligned} M(Px, Qy, qt) &\geq \min\left\{\frac{M(Sx, Ty, t) + M(Px, Ty, t) + M(Qy, Sx, t)}{3}, M(Sx, Px, t), M(Qy, Ty, t)\right\} \\ &= \min\left\{\frac{M(Px, Qy, t) + M(Px, Qy, t) + M(Qy, Px, t)}{3}, M(Px, Px, t), M(Qy, Qy, t)\right\} \\ &= \min\left\{\frac{M(Px, Qy, t) + M(Px, Qy, t) + M(Qy, Px, t)}{3}, 1, 1\right\} \\ &= M(Px, Qy, t) \end{aligned}$$

Therefore  $Px = Qy$ , i.e.  $Px = Sx = Qy = Ty$ . Suppose that  $z$  such that  $Pz = Sz$  then by (1) we have  $Pz = Sz = Qy = Ty$  so  $Px = Pz$  and  $w = Px = Sx$  is the unique point of coincidence of  $P$  and  $S$ .

Similarly there is a unique point  $z \in X$  such that  $z = Qz = Tz$ .

Assume that  $w \neq z$ . We have

$$\begin{aligned} M(w, z, qt) &= M(Pw, Qz, qt) \\ M(Px, Qy, qt) &\geq \min\left\{\frac{M(Sx, Tz, t) + M(Pw, Tz, t) + M(Qz, Sw, t)}{3}, M(Sw, Pz, t), M(Qz, Tz, t)\right\} \\ &= \min\left\{\frac{M(w, z, t) + M(w, z, t) + M(w, z, t)}{3}, M(w, z, t), M(z, z, t)\right\} \\ &= M(w, z, t) \end{aligned}$$

Therefore we have  $z = w$  by Lemma 2.14 and  $z$  is a common fixed point of  $P, Q, S$  and  $T$ . The uniqueness of fixed point holds from (1)

### Theorem: 3.2

Let  $(X, M, *)$  be complete fuzzy metric space and let  $P, Q, S$  and  $T$  be self mappings of  $X$ . Let the pairs  $\{P, S\}$  and  $\{Q, T\}$  be owc. If there exists  $q \in (0, 1)$  such that

$$M(Px, Qy, qt) \geq \emptyset \left[ \min\left\{\frac{M(Sx, Ty, t) + M(Px, Ty, t) + M(Qy, Sx, t)}{3}, M(Sx, Px, t), M(Qy, Ty, t)\right\} \right] \quad (2)$$

for all  $x, y \in X$  and  $\emptyset : [0, 1] \rightarrow [0, 1]$  such that  $\emptyset(t) > t$  for all  $0 < t < 1$ , then there exist a unique common fixed point of  $P, Q, S$  and  $T$

**Proof:**

$$\begin{aligned} M(Px, Qy, qt) &\geq \emptyset \left[ \min\left\{\frac{M(Sx, Ty, t) + M(Px, Ty, t) + M(Qy, Sx, t)}{3}, M(Sx, Px, t), M(Qy, Ty, t)\right\} \right] \\ &\geq \emptyset [M(Px, Qy, t)] \quad \text{from theorem 3.1} \\ &\geq \emptyset [M(Px, Qy, t)] \end{aligned}$$

Now proof follows by (3.1)

### Theorem: 3.3

Let  $(X, M, *)$  be a complete fuzzy metric space and let  $P, Q, S$  and  $T$  are self mappings of  $X$ .

Let the pairs {P, S} and {Q, T} be owc . If there exists  $q \in (0, 1)$  such that

$$M(Px, Qy, qt) \geq \emptyset \left[ \min \left\{ \frac{M(Sx, Ty, t) + M(Px, Ty, t) + M(Qy, Sx, t)}{3}, M(Sx, Px, t), M(Qy, Ty, t) \right\} \right] \quad (3)$$

For all  $x, y \in X$  and  $\emptyset: [0, 1]^4 \rightarrow [0, 1]$  such that  $\emptyset(t, 1, t, t) > t$  for all  $0 < t < 1$  then there exists a unique common fixed point of P, Q, S and T.

**Proof:** Let the pairs {P, S} and {Q, T} are owc ,there are points  $x, y \in X$  such that  $Px = Sx$  and  $Qy = Ty$  are claim that  $Px = Qy$ . By inequality (3) we have

$$\begin{aligned} M(Px, Qy, qt) &\geq \emptyset \left[ \min \left\{ \frac{M(Sx, Ty, t) + M(Px, Ty, t) + M(Qy, Sx, t)}{3}, M(Sx, Px, t), M(Qy, Ty, t) \right\} \right] \\ &= \emptyset \left[ \min \left\{ \frac{M(Px, Qy, t) + M(Px, Qy, t) + M(Qy, Px, t)}{3}, M(Px, Px, t), M(Qy, Qy, t) \right\} \right] \\ &= \emptyset [\min \{M(Px, Qy, t), 1, 1\}], [\because M(Px, Px, t) = 1, M(Qy, Qy, t) = 1] \\ &> M(Px, Qy, t) \end{aligned}$$

a contradiction , therefore  $Px = Qy$  i.e.  $Px = Sx = Qy = Ty$  suppose that there is another point  $z$  such that  $Pz = Sz$  then by (3) we have

$Pz = Sz = Qy = Ty$  so  $Px = Pz$  and  $w = Px = Tx$  is unique point of coincidence of P and T. Qy Lemma 2.14  $w$  is a unique common fixed point of P and S, similarly there is a unique point  $z \in X$  such that  $z = Qz = Tz$ . Thus  $z$  is common fixed point of P, Q, S, and T. The uniqueness of fixed point holds from (3).

#### Theorem: 3.4

Let  $(X, M, *)$  be complete fuzzy metric space and let P, Q, S and T be self mappings of X, let the pairs {P, S} and {Q, T} are owc. If there exists a points  $q \in (0, 1)$  for all  $x, y \in X$  and  $t > 0$

$$M(Px, Qy, qt) > \left\{ \frac{M(Sx, Ty, t) + M(Px, Ty, t) + M(Sx, Qy, t)}{3}, M(Px, Sx, t), M(Qy, Ty, t) \right\} \quad (4)$$

then there exists a unique common fixed points of P, Q, S and T.

**Proof:** Let the points {P, S} and {Q, T} are owc and there are points  $x, y \in X$  such that  $Px = Sx$  and  $Qy = Ty$  and claim that  $Px = Qy$  By inequality (4)

We have

$$\begin{aligned} M(Px, Qy, qt) &> \left\{ \frac{M(Sx, Ty, t) + M(Px, Ty, t) + M(Sx, Qy, t)}{3}, M(Px, Sx, t), M(Qy, Ty, t) \right\} \\ &= \left\{ \frac{M(Px, Qy, t) + M(Px, Qy, t) + M(Px, Qy, t)}{3}, M(Px, Px, t), M(Qy, Qy, t) \right\} \\ &\geq M(Px, Qy, t) * 1 * 1 \\ &\geq M(Px, Qy, t) \end{aligned}$$

Thus we have  $Px = Qy$  i.e.  $Px = Sx = Qy = Ty$ . Suppose that there is another point  $z$  such that  $Pz = Sz$  then by (4) we have  $Pz = Sz = Qy = Ty$  so  $Px = Pz$  and  $w = Px = Sx$  is unique point of coincidence of P and S.

Similarly there is a unique point  $z \in X$  such that  $z = Qz = Tz$ . Thus  $w$  is a common fixed point of P, Q, S and T.

#### Corollary: 3.5

Let  $(X, M, *)$  be a complete fuzzy metric space and let  $P, Q, S$  and  $T$  be self mappings of  $X$ . Let the pairs  $\{P, S\}$  and  $\{Q, T\}$  are owc. If there exists a point  $q \in (0, 1)$  for all  $x, y \in X$  and  $t > 0$

$$M(Px, Qy, qt) \geq \left\{ \frac{M(Sx, Ty, t) + M(Qy, Sx, 2t) + M(Px, Ty, t)}{3} \right\} * M(Px, Sx, t) * M(Qy, Ty, t) \quad (5)$$

then there exists a unique common fixed point of  $P, Q, S$  and  $T$ .

**Proof:** We have

$$\begin{aligned} M(Px, Qy, qt) &\geq \left\{ \frac{M(Sx, Ty, t) + M(Qy, Sx, 2t) + M(Px, Ty, t)}{3} \right\} * M(Px, Sx, t) * M(Qy, Ty, t) \\ &\geq \left\{ \frac{M(Sx, Ty, t) + M(Sx, Ty, t) * M(Ty, Qy, t) + M(Px, Ty, t)}{3} \right\} * M(Px, Sx, t) * M(Qy, Ty, t) \\ &\geq \left\{ \frac{M(Sx, Ty, t) + M(Sx, Ty, t) * M(Qy, Qy, t) + M(Px, Ty, t)}{3} \right\} * M(Px, Sx, t) * M(Qy, Ty, t) \\ &\geq \left\{ \frac{M(Sx, Ty, t) + M(Sx, Ty, t) * 1 + M(Px, Ty, t)}{3} \right\} * 1 * 1 \\ &\geq \left\{ \frac{M(Sx, Ty, t) + M(Sx, Ty, t) + M(Px, Ty, t)}{3} \right\} * 1 * 1 \\ &\geq M(Px, Px, t), [\because Px = Sx \text{ and } Qy = Ty] \end{aligned}$$

and therefore from Theorem 3.4,  $P, Q, S$  and  $T$  have common fixed point.

**Corollary: 3.6**

Let  $(X, M, *)$  be complete fuzzy metric space and let  $P, Q, S$  and  $T$  be self-mapping of  $X$ . Let the pairs  $\{P, S\}$  and  $\{Q, T\}$  are owc. If there exist point  $q \in (0, 1)$  for all  $x, y \in X$  and  $t > 0$

$$M(Px, Qy, qt) \geq M(Sx, Ty, t) \quad (6)$$

then there exists a unique common fixed point of  $P, Q, S$  and  $T$ .

**Proof:** The proof follows from Corollary 3.5

**Theorem:3.7**

Let  $(X, M, *)$  be complete fuzzy metric space. Then continues self mappings  $S$  and  $T$  of  $X$  have a common fixed point in  $X$  if and only if there exists a self mapping  $P$  of  $X$  such that the following conditions are satisfied

- (i)  $PX \subset TX \cap SX$
- (ii) pairs  $\{P, S\}$  and  $\{P, T\}$  are weakly compatible,
- (iii) there exists a point  $q \in (0, 1)$  such that for every  $x, y \in X$  and  $t > 0$

$$M(Px, Qy, qt) \geq \left\{ \frac{M(Sx, Ty, t) + M(Px, Sx, t) + M(Px, Ty, t)}{3} \right\} * M(Py, Ty, t) \quad (7)$$

then  $P, S$  and  $T$  have a unique common fixed point.

**Proof:** Since compatible implies owc, the result follows from 3.4

**Theorem: 3.8**

Let  $(X, M, *)$  be a complete fuzzy metric space and let  $P$  and  $Q$  be self mapping of  $X$ . Let  $P$  and  $Q$  are owc. If there exists a point  $q \in (0, 1)$  for all  $x, y \in X$  and  $t > 0$

$$M(Sx, Sy, qt) \geq \alpha M(Px, Py, t) + \beta \left\{ \frac{M(Px, Py, t) + M(Sy, Px, t) + M(Sx, Py, t)}{3} \right\} \quad (8)$$

for all  $x, y \in X$ , where  $\alpha, \beta > 0$ ,  $\alpha + \beta > 1$ . Then  $P$  and  $S$  have a unique common fixed point.

**Proof:** Let the pairs  $\{P, S\}$  be owc, so there is a point  $x \in X$  such that  $Px = Sx$ . Suppose that there exist another point  $y \in X$  for which  $Py = Sy$ . We claim that  $Sx = Sy$  by equation (8) we have

$$\begin{aligned} M(Sx, Sy, qt) &\geq \alpha M(Px, Py, t) + \beta \left\{ \frac{M(Px, Py, t) + M(Sy, Px, t) + M(Sx, Py, t)}{3} \right\} \\ M(Sx, Sy, qt) &\geq \alpha M(Sx, Sy, t) + \beta \left\{ \frac{M(Sx, Sy, t) + M(Sy, Sx, t) + M(Sx, Sy, t)}{3} \right\} \\ &= (\alpha + \beta) M(Sx, Sy, t) \end{aligned}$$

A contradiction, since  $(\alpha + \beta) > 1$  therefore  $Sx = Sy$ . Therefore  $Px = Py$  and  $Px$  is unique. From lemma 2.14,  $P$  and  $S$  have a unique fixed point.

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