

ON Tg'' -SPACES

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ABSTRACT

The aim of this paper is to introduce Tg'' -spaces, ${}_gTg''$ -spaces and $\alpha Tg''$ -spaces. Moreover, we obtain certain new characterizations for the Tg'' -spaces, ${}_gTg''$ -spaces and $\alpha Tg''$ -spaces.

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1. INTRODUCTION:

Levine [10] introduced the notion of $T_{1/2}$ -spaces which properly lie between T_1 -spaces and T_0 -spaces. Many authors studied properties of $T_{1/2}$ -spaces: Dunham [8], Arenas et al. [3] etc. In this paper, we introduce the notions called Tg'' -spaces, ${}_gTg''$ -spaces and $\alpha Tg''$ -spaces and obtain their properties and characterizations.

2. PRELIMINARIES:

Throughout this paper (X, τ) (or X) represent topological spaces on which no separation axioms are assumed unless otherwise mentioned. For a subset A of a space (X, τ) , $\text{cl}(A)$, $\text{int}(A)$ and A^c denote the closure of A , the interior of A and the complement of A respectively.

We recall the following definitions which are useful in the sequel.

Definition: 2.1

A subset A of a space (X, τ) is called:

(i) semi-open set [11] if $A \subseteq \text{cl}(\text{int}(A))$;

(ii) preopen set [13] if $A \subseteq \text{int}(\text{cl}(A))$;

(iii) α -open set [15] if $A \subseteq \text{int}(\text{cl}(\text{int}(A)))$;

(iv) β -open set [1] (= semi-preopen [2]) if $A \subseteq \text{cl}(\text{int}(\text{cl}(A)))$.

The complements of the above mentioned open sets are called their respective closed sets.

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The preclosure [16] (resp. semi-closure [5], α -closure [15], semi-pre-closure [2]) of a subset A of X, denoted by $\text{pcl}(A)$ (resp. $\text{scl}(A)$, $\alpha \text{cl}(A)$, $\text{spcl}(A)$), is defined to be the intersection of all preclosed (resp. semi-closed, α -closed, semi-preclosed) sets of (X, τ) containing A. It is known that $\text{pcl}(A)$ (resp. $\text{scl}(A)$, $\alpha \text{cl}(A)$, $\text{spcl}(A)$) is a preclosed (resp. semi-closed, α -closed, semi-preclosed) set. For any subset A of an arbitrarily chosen topological space, the semi-interior [5] (resp. α -interior [15], preinterior [16]) of A, denoted by $\text{sint}(A)$ (resp. $\alpha \text{int}(A)$, $\text{pint}(A)$), is defined to be the union of all semi-open (resp. α -open, preopen) sets of (X, τ) contained in A.

Definition: 2.2

A subset A of a space (X, τ) is called:

- (i) a generalized closed (briefly g-closed) set [10] if $\text{cl}(A) \subseteq U$ whenever $A \subseteq U$ and U is open in (X, τ) . The complement of g-closed set is called g-open set;
- (ii) a generalized semi-closed (briefly gs-closed) set [4] if $\text{scl}(A) \subseteq U$ whenever $A \subseteq U$ and U is open in (X, τ) . The complement of gs-closed set is called gs-open set;
- (iii) an α -generalized closed (briefly α g-closed) set [12] if $\alpha \text{cl}(A) \subseteq U$ whenever $A \subseteq U$ and U is open in (X, τ) . The complement of α g-closed set is called α g-open set;
- (iv) a generalized semi-preclosed (briefly gsp-closed) set [16] if $\text{spcl}(A) \subseteq U$ whenever $A \subseteq U$ and U is open in (X, τ) . The complement of gsp-closed set is called gsp-open set;
- (v) a \hat{g} -closed set [19] (= ω -closed [18]) if $\text{cl}(A) \subseteq U$ whenever $A \subseteq U$ and U is semi-open in (X, τ) . The complement of \hat{g} -closed set is called \hat{g} -open set;
- (vi) a $\mathcal{G}^{\#}$ -closed set [17] if $\text{cl}(A) \subseteq U$ whenever $A \subseteq U$ and U is $\mathcal{G}^{\#}$ -open in (X, τ) . The complement of $\mathcal{G}^{\#}$ -closed set is called $\mathcal{G}^{\#}$ -open set;
- (vii) a g^* -preclosed (briefly g^*p -closed) set [20] if $\text{pcl}(A) \subseteq U$ whenever $A \subseteq U$ and U is g^* -open in (X, τ) . The complement of g^*p -closed set is called g^*p -open set.

The collection of all $\mathcal{G}^{\#}$ -closed (resp. ω -closed, α g-closed, gsp-closed, gs-closed, α -closed, g^*p -closed) sets is denoted by $\mathcal{G}^{\#}C(X)$ (resp. $\omega C(X)$, $\alpha G C(X)$, $GSP C(X)$, $GS C(X)$, $\alpha C(X)$, $G^*P C(X)$).

The collection of all $\mathcal{G}^{\#}$ -open (resp. ω -open, α g-open, gsp-open, gs-open, α -open, g^*p -open) sets is denoted by $\mathcal{G}^{\#}O(X)$ (resp. $\omega O(X)$, $\alpha G O(X)$, $GSP O(X)$, $GS O(X)$, $\alpha O(X)$, $G^*P O(X)$).

We denote the power set of X by $P(X)$.

Definition: 2.3

A space (X, τ) is called:

- (i) $T_{1/2}$ -space [10] if every g-closed set is closed.
- (ii) T_b -space [7] if every gs-closed set is closed.
- (iii) αT_b -space [6] if every α g-closed set is closed.
- (iv) T_{ω} -space [18] if every ω -closed set is closed.
- (v) T_{p^*} -space [20] if every g^*p -closed set in it is closed.
- (vi) ${}^*_s T_p$ -space [20] if every gsp-closed set in it is g^*p -closed.
- (vii) αT_d -space [6] if every α g-closed set is g-closed.

(viii) α -space [15] if every α -closed set is closed.

Definition: 2.4 [14]

Let (X, τ) be a topological space and $A \subseteq X$. We define the gs -closure of A (briefly $gs-cl(A)$) to be the intersection of all gs -closed sets containing A .

Result: 2.5 [17]

For a topological space X , the following hold:

- (i) Every closed set is g'' -closed but not conversely.
- (ii) Every g'' -closed set is ω -closed but not conversely.
- (iii) Every g'' -closed set is g -closed but not conversely.
- (iv) Every g'' -closed set is α g -closed but not conversely.
- (v) Every g'' -closed set is gs -closed but not conversely.
- (vi) Every g'' -closed set is gsp -closed but not conversely.

Theorem: 2.6[17]

A set A is g'' -closed if and only if $cl(A) - A$ contains no nonempty gs -closed set.

3. PROPERTIES OF T g'' -SPACES:

We introduce the following definition:

Definition: 3.1

A space (X, τ) is called a T g'' -space if every g'' -closed set in it is closed.

Example: 3.2

Let $X = \{a, b, c\}$ with $\tau = \{\emptyset, \{b\}, X\}$. Then $G'' C(X) = \{\emptyset, \{a, c\}, X\}$. Thus (X, τ) is a T g'' -space.

Example: 3.3

Let $X = \{a, b, c\}$ with $\tau = \{\emptyset, \{a, c\}, X\}$. Then $G'' C(X) = \{\emptyset, \{b\}, \{a, b\}, \{b, c\}, X\}$. Thus (X, τ) is not a T g'' -space.

Proposition: 3.4

Every $T_{1/2}$ -space is T g'' -space but not conversely.

Proof: Follows from Result 2.5 (iii).

The converse of Proposition 3.4 need not be true as seen from the following example.

Example: 3.5

Let X and τ as in the Example 3.2, $G C(X) = \{\emptyset, \{a\}, \{c\}, \{a, b\}, \{a, c\}, \{b, c\}, X\}$. Thus (X, τ) is not a $T_{1/2}$ -space.

Proposition: 3.6

Every T ω -space is T g'' -space but not conversely.

Proof: Follows from Result 2.5 (ii).

The converse of Proposition 3.6 need not be true as seen from the following example.

Example: 3.7

Let $X = \{a, b, c\}$ with $\tau = \{\emptyset, \{a\}, \{b, c\}, X\}$. Then $\omega C(X) = P(X)$ and $\mathcal{G}^{\#} C(X) = \{\emptyset, \{a\}, \{b, c\}, X\}$. Thus (X, τ) is $T \mathcal{G}^{\#}$ -space but not a $T \omega$ -space.

Proposition: 3.8

Every αT_b -space is $T \mathcal{G}^{\#}$ -space but not conversely.

Proof: Follows from Result 2.5 (iv).

The converse of Proposition 3.8 need not be true as seen from the following example.

Example: 3.9

Let X and τ as in the Example 3.2, $\alpha \mathcal{G} C(X) = \{\emptyset, \{a\}, \{c\}, \{a, b\}, \{a, c\}, \{b, c\}, X\}$. Thus (X, τ) is not a αT_b -space.

Proposition: 3.10

Every *T_p -space and T_p^* -space is $T \mathcal{G}^{\#}$ -space but not conversely.

Proof: Follows from Result 2.5 (vi) and Definition 2.3 (vi) and (v).

The converse of Proposition 3.10 need not be true as seen from the following example.

Example: 3.11

Let X and τ as in the Example 3.2, $GSP C(X) = \{\emptyset, \{a\}, \{c\}, \{a, b\}, \{a, c\}, \{b, c\}, X\}$ and $G^*PC(X) = \{\emptyset, \{a\}, \{c\}, \{a, c\}, \{b, c\}, X\}$. Thus (X, τ) is neither a *T_p -space nor a T_p^* -space.

Proposition: 3.12

Every T_b -space is $T \mathcal{G}^{\#}$ -space but not conversely.

Proof: Follows from Result 2.5 (v).

The converse of Proposition 3.12 need not be true as seen from the following example.

Example: 3.13

Let X and τ as in the Example 3.2, $GS C(X) = \{\emptyset, \{a\}, \{c\}, \{a, b\}, \{a, c\}, \{b, c\}, X\}$. Thus (X, τ) is not a T_b -space.

Remark: 3.14

We conclude from the next two examples that $T \mathcal{G}^{\#}$ -spaces and α -spaces are independent.

Example: 3.15

Let X and τ as in the Example 3.2, $\alpha C(X) = \{\emptyset, \{a\}, \{c\}, \{a, c\}, X\}$. Thus (X, τ) is a $T \mathcal{G}^{\#}$ -space but not a α -space.

Example: 3.16

Let X and τ as in the Example 3.3, $\alpha C(X) = \{\emptyset, \{b\}, X\}$. Thus (X, τ) is a α -space but not a $T \mathcal{G}^{\#}$ -space.

Theorem: 3.17

For a space (X, τ) the following properties are equivalent:

- (i) (X, τ) is a $T \mathcal{G}^{\#}$ -space.
- (ii) Every singleton subset of (X, τ) is either gs -closed or open.

Proof: (i) \rightarrow (ii). Assume that for some $x \in X$, the set $\{x\}$ is not a gs -closed in (X, τ) . Then the only gs -open set containing $\{x\}^c$ is X and so $\{x\}^c$ is $\mathcal{G}^{\#}$ -closed in (X, τ) . By assumption $\{x\}^c$ is closed in (X, τ) or equivalently $\{x\}$ is open.

(ii) \rightarrow (i). Let A be a $\mathcal{G}^{\#}$ -closed subset of (X, τ) and let $x \in cl(A)$. By assumption $\{x\}$ is either gs -closed or open.

Case (a) Suppose that $\{x\}$ is gs-closed. If $x \notin A$, then $\text{cl}(A) - A$ contains a nonempty gs-closed set $\{x\}$, which is a contradiction to Theorem 2.6. Therefore $x \in A$.

Case (b) Suppose that $\{x\}$ is open. Since $x \in \text{cl}(A)$, $\{x\} \cap A \neq \emptyset$ and so $x \in A$. Thus in both case, $x \in A$ and therefore $\text{cl}(A) \subseteq A$ or equivalently A is a closed set of (X, τ) .

Definition: 3.18

A topological space (X, τ) is called generalized semi- R_0 (briefly gs- R_0) if and only if for each gs-open set G and $x \in G$ implies $\text{gs-cl}(\{x\}) \subset G$.

Definition: 3.19

A topological space (X, τ) is called:

- (i) generalized semi- T_0 (briefly gs- T_0) if and only if to each pair of distinct points x, y of X , there exists a gs-open set containing one but not the other.
- (ii) generalized semi- T_1 (briefly gs- T_1) if and only if to each pair of distinct points x, y of X , there exists a pair of gs-open sets, one containing x but not y , and the other containing y but not x .

Theorem: 3.20

For a topological space X , each of the following statement is equivalent:

- (i) X is a gs- T_1 .
- (ii) Each one point set is gs-closed set in X .

Proof: (i) \Rightarrow (ii) Let a space X be gs- T_1 and $x \in X$. Suppose $\text{gscl}(\{x\}) \neq \{x\}$. Then we can find an element $y \in \text{gscl}(\{x\})$ with $y \neq x$. Since X is gs- T_1 , there exist gs-open sets U and V such that $x \in U, y \notin U$ and $y \in V, x \notin V$. Now $x \in V^c$ and V^c is gs-closed. Therefore $\text{gscl}(\{x\}) \subseteq V^c$ which implies $y \in V^c$, contradiction. Hence $\text{gscl}(\{x\}) = \{x\}$ or $\{x\}$ is gs-closed.

(ii) \Rightarrow (i) Let $x, y \in X$ with $x \neq y$. Then $\{x\}$ and $\{y\}$ are gs-closed. Therefore $U = (\{x\})^c$ and $V = (\{y\})^c$ are gs-open and $x \in U, y \notin U$ and $y \in V, x \notin V$. Hence X is gs- T_1

Theorem: 3.21

For a space (X, τ) the following properties hold:

- (i) If (X, τ) is gs- T_1 , then it is $T \mathcal{G}^{\#}$.
- (ii) If (X, τ) is $T \mathcal{G}^{\#}$, then it is gs- T_0 .

Proof:

(i) The proof is obvious from Theorem 3.20.

(ii) Let x and y be two distinct elements of X . Since the space (X, τ) is $T \mathcal{G}^{\#}$, we have that $\{x\}$ is gs-closed or open. Suppose that $\{x\}$ is open. Then the singleton $\{x\}$ is a gs-open set such that $x \in \{x\}$ and $y \notin \{x\}$. Also, if $\{x\}$ is gs-closed, then $X \setminus \{x\}$ is gs-open such that $y \in X \setminus \{x\}$ and $x \notin X \setminus \{x\}$. Thus, in the above two cases, there exists a gs-open set U of X such that $x \in U$ and $y \notin U$ or $x \notin U$ and $y \in U$. Thus, the space (X, τ) is gs- T_0 .

Theorem: 3.22

For a gs- R_0 topological space (X, τ) the following properties are equivalent:

- (i) (X, τ) is gs- T_0 .
- (ii) (X, τ) is $T \mathcal{G}^{\#}$.
- (iii) (X, τ) is gs- T_1 .

Proof: It suffices to prove only (i) \Rightarrow (iii). Let $x \neq y$ and since (X, τ) is $gs-T_0$, we may assume that $x \in U \subseteq X \setminus \{y\}$ for some gs -open set U . Then $x \in X \setminus gs-cl(\{y\})$ and $X \setminus gs-cl(\{y\})$ is gs -open. Since (X, τ) is $gs-R_0$, we have $gs-cl(\{x\}) \subseteq X \setminus gs-cl(\{y\}) \subseteq X \setminus \{y\}$ and hence $y \notin gs-cl(\{x\})$. There exists gs -open set V such that $y \in V \subseteq X \setminus \{x\}$ and (X, τ) is $gs-T_1$.

4. $gT \mathcal{G}^{\#}$ -SPACES:

Definition: 4.1

A space (X, τ) is called a $gT \mathcal{G}^{\#}$ -space if every g -closed set in it is $\mathcal{G}^{\#}$ -closed.

Example: 4.2

Let X and τ as in the Example 3.3, is a $gT \mathcal{G}^{\#}$ -space and the space (X, τ) in the Example 3.2, is not a $gT \mathcal{G}^{\#}$ -space.

Proposition: 4.3

Every $T_{1/2}$ -space is $gT \mathcal{G}^{\#}$ -space but not conversely.

Proof: Follows from Result 2.5 (i).

The converse of Proposition 4.3 need not be true as seen from the following example.

Example: 4.4

Let X and τ as in the Example 3.3, is a $gT \mathcal{G}^{\#}$ -space but not a $T_{1/2}$ -space.

Remark: 4.5

$T \mathcal{G}^{\#}$ -space and $gT \mathcal{G}^{\#}$ -space are independent.

Example: 4.6

The space (X, τ) in the Example 3.3, is a $gT \mathcal{G}^{\#}$ -space but not a $T \mathcal{G}^{\#}$ -space and the space (X, τ) in the Example 3.2, is a $T \mathcal{G}^{\#}$ -space but not a $gT \mathcal{G}^{\#}$ -space.

Theorem: 4.7

If (X, τ) is a $gT \mathcal{G}^{\#}$ -space, then every singleton subset of (X, τ) is either g -closed or $\mathcal{G}^{\#}$ -open.

Proof: Assume that for some $x \in X$, the set $\{x\}$ is not a g -closed in (X, τ) . Then $\{x\}$ is not a closed set, since every closed set is a g -closed set. So $\{x\}^c$ is not open and the only open set containing $\{x\}^c$ is X itself. Therefore $\{x\}^c$ is trivially a g -closed set and by assumption, $\{x\}^c$ is an $\mathcal{G}^{\#}$ -closed set or equivalently $\{x\}$ is $\mathcal{G}^{\#}$ -open.

The converse of Theorem 4.7 need not be true as seen from the following example.

Example: 4.8

Let X and τ as in the Example 3.2. The sets $\{a\}$ and $\{c\}$ are g -closed in (X, τ) and the set $\{b\}$ is $\mathcal{G}^{\#}$ -open. But the space (X, τ) is not a $gT \mathcal{G}^{\#}$ -space.

Theorem: 4.9

A space (X, τ) is $T_{1/2}$ if and only if it is both $T \mathcal{G}^{\#}$ and $gT \mathcal{G}^{\#}$.

Proof: Necessity. Follows from Propositions 3.4 and 4.3.

Sufficiency. Assume that (X, τ) is both $T \mathcal{G}^{\#}$ and $gT \mathcal{G}^{\#}$. Let A be a g -closed set of (X, τ) . Then A is $\mathcal{G}^{\#}$ -closed, since (X, τ) is a $gT \mathcal{G}^{\#}$. Again since (X, τ) is a $T \mathcal{G}^{\#}$, A is a closed set in (X, τ) and so (X, τ) is a $T_{1/2}$.

5. $\alpha T \mathcal{G}^{\#}$ -SPACES:

Definition: 5.1

A space (X, τ) is called a $\alpha T \mathcal{G}^{\#}$ -space if every α g -closed set in it is $\mathcal{G}^{\#}$ -closed.

Example: 5.2

Let X and τ as in the Example 3.3, is a $\alpha T \mathcal{G}^{\#}$ -space and the space (X, τ) in the Example 3.2, is not a $\alpha T \mathcal{G}^{\#}$ -space.

Proposition: 5.3

Every αT_b -space is $\alpha T \mathcal{G}^{\#}$ -space but not conversely.

Proof: Follows from Result 2.5 (i).

The converse of Proposition 5.3 need not be true as seen from the following example.

Example: 5.4

Let X and τ in the Example 3.3, is a $\alpha T \mathcal{G}^{\#}$ -space but not a αT_b -space.

Proposition: 5.5

Every $\alpha T \mathcal{G}^{\#}$ -space is a αT_d -space but not conversely.

Proof: Let (X, τ) be an $\alpha T \mathcal{G}^{\#}$ -space and let A be an α g-closed set of (X, τ) . Then A is a $\mathcal{G}^{\#}$ -closed subset of (X, τ) and by Result 2.5 (iii), A is g-closed. Therefore (X, τ) is an αT_d -space.

The converse of Proposition 5.5 need not be true as seen from the following example.

Example: 5.6

Let X and τ in the Example 3.3, is a αT_d -space but not a $\alpha T \mathcal{G}^{\#}$ -space.

Theorem: 5.7

If (X, τ) is a $\alpha T \mathcal{G}^{\#}$ -space, then every singleton subset of (X, τ) is either α g-closed or $\mathcal{G}^{\#}$ -open.

Proof: Similar to Theorem 4.7.

The converse of Theorem 5.7 need not be true as seen from the following example.

Example: 5.8

Let X and τ as in the Example 3.2. The sets $\{a\}$ and $\{c\}$ are α g-closed in (X, τ) and the set $\{b\}$ is $\mathcal{G}^{\#}$ -open. But the space (X, τ) is not a $\alpha T \mathcal{G}^{\#}$ -space.

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