

**EFFECT OF HALL CURRENT AND RADIATION ABSORPTION  
ON CONVECTIVE HEAT AND MASS TRANSFER FLOW OF A MICROPOLAR FLUID  
IN A ROTATING FLUID PAST A VERTICAL POROUS PLATE**

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**ABSTRACT**

*An attempt has been to investigate effect of Hall currents, thermal radiation and radiation absorption on mixed convective heat and mass transfer flow of Micropolar fluid in as rotating fluid past a porous vertical plate. The equations governing the flow, heat and mass transfer have been solved by assuming that the solution consists of harmonic and non-harmonic terms. the effect of Hall currents, solet effect and chemical reaction on all the flow characteristics have been analysed.*

**Keywords:** Hall currents, Radiation absorption, Chemical reaction, Heat sources and Porous medium.

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**1. INTRODUCTION**

In recent years, there has been a considerable interest in rotating hydro magnetic fluid flows due to possible applications to geophysical and astrophysical problems. An order of magnitude analysis shows that in the basic field equations, the Coriolis force is very significant as compared to the inertial force. Furthermore, it reveals that the Coriolis and magneto hydro- dynamic forces are of comparable magnitude. It is generally admitted that a number of astronomical bodies (e.g. the Sun, Earth, Jupiter, Magnetic stars, Pulsars) possess fluid interiors and (at least surface) magnetic fields, changes in the rotation rate of such objects suggest the possible importance of hydro magnetic spin-up. This problem of spin-up in magneto hydro dynamic rotating fluids has been examined under varied conditions by many researchers notably Gilman and Benton [1], Benton and Loper [2], Chawala [3], Debnath [4-5] and Singh [6].

The theory of micropolar fluids was first introduced and formulated by Eringen[7]. This theory displays the effect of local rotary inertia and couple stress. This theory is expected to provide a mathematical model for the non-Newtonian fluid behavior observed in certain fluid such as exotic lubricants, polymeric fluid. Colloidal fluids, liquid crystals, dirty oils, animal blood, etc., which is more realistic and important from a technological point of view. The theory of thermomicropolar fluids was developed by Eringen [8], by extending his theory of micropolar fluid. Physically, they represent fluids consisting of randomly oriented particles suspended in a viscous medium (Lukaszewicz [9]).

The micropolar fluids which contain micro-constituents and can undergo rotation has been proposed by Eringen[10]. These kind of fluids are utilized in analyzing exotic lubricants, the flow of colloidal suspensions, paints, liquid crystals, animal blood, fluid flowing in brain, turbulent shear flows and body fluids both mathematically and industrially. In addition due to its practical application to boundary layer control and thermal protection in high energy flow by means of wall velocity and mass transfer, considerable attention has been paid to the thermal boundary layer flows over moving boundaries [11]. The oscillatory boundary layer flow with constant heat source in the case of MHD free convection currents and mass transfer has been considered by Rahman and Sattar [12]. Khonsari and Brewe [13] have examined the effect of viscous dissipation on the lubrication characteristics of micropolar fluids. The effect of non zero values of micro gyration vector on semi-infinite moving porous plate with constant velocity when the magnetic field is imposed transversely to the plate and the temperature of the plate is oscillating with time have been analyzed by Kim and Lee[14].

Deka *et. al.* [15] investigated the effect of first order homogeneous chemical reaction on the process of an unsteady flow past an infinite vertical plate with a constant heat and mass transfer. Muthucumaraswamy and Ganesan [16] discussed the effect of the chemical reaction and injection on flow characteristics in an unsteady up-ward motion of an isothermal plate.

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In modern technology, considerable interest has been developed in the study of interaction between magnetic fields and convection flow of incompressible electrically conducting micropolar fluids past a porous plate embedded in a porous medium, owing to its wide range of applications in geophysics, plasma studies, oil exploration, nuclear reactors and the boundary layer control in the field of aerodynamics [16-18]. Seddeek studied the flow of a micropolar fluid by the presence of magnetic field over a continuously moving plate. Gibben [19] considered the MHD boundary layer flow over a semi-infinite plate with an aligned magnetic field in the presence of pressure gradient. He has obtained solutions for large and small magnetic Prandtl numbers using the method of matched asymptotic expansion. Kim and Lee [20] analytically studied an MHD oscillatory flow of a micropolar fluid over a vertical porous plate. Raptis [21] presented the flow of a micropolar fluid past a continuous moving plate by the presence of radiation. El-Arabawy [22] analyzed the effect of suction/injection on the flow of a micropolar fluid past continuously moving plate in the presence of radiation.

MHD flow of uniformly stretched vertical permeable surface in the presence of heat generation/absorption and a chemical reaction has been considered by Chamkha[17]. Rahman and Satter[18] examined MHD convective flow of micropolar fluid past a continuously moving vertical porous plate in the presence of heat generation/absorption. Ibrahim *et al* [23] obtained the analytical solution for unsteady MHD free convection flow past a semi-infinite vertical permeable moving plate with heat source and chemical reaction. Rahman *et al.* [24] studied heat transfer in micropolar fluid with temperature dependent fluid properties along a non-stretching sheet. Rahman *et al.* [25-26] considered heat transfer in micropolar fluid along an inclined plate with variable fluid properties under different boundary conditions. Damesh *et al.*[27] have investigated heat and mass transfer free convective flow adjacent to a continuous moving vertical porous plate for incompressible micropolar fluid in the presence of heat generation/absorption and a first order chemical reaction. Rahman and AL-Lawatia [28] developed the problem by considering higher order of chemical reaction.

In all the previous investigation, the effect of thermal radiation on the flow and heat transfer have not been provided. The effect of radiation on MHD flow and heat transfer problem have become more important industrially. At high operating temperature, radiation effect can be quite significant. Many process in engineering areas occur at high temperature and a knowledge of radiation heat transfer becomes very important for design of reliable equipment, nuclear plants, gas turbines and various propulsion devices or aircraft, missiles, satellites and space vehicles. Based on these applications, Cogley *et al.* [29] showed that in the optically thin limit, the fluid does not absorb its own emitted radiation but the fluid does absorb radiation emitted by the boundaries. Ibrahim *et al.* [35] discussed the case of mixed convection flow of a micropolar fluid past a semi infinite steady moving porous plate with varying suction velocity normal to the plate in presence of thermal radiation and viscous dissipation. Rahman and Sattar [36] studied transient convective flow of micropolar fluid past a continuous moving porous plate in the presence of radiation. The effect of the chemical reaction and radiation absorption on the unsteady MHD free convection flow past a semi-infinite vertical permeable moving plate with heat source and suction has been studied by Ibrahim *et al.* [37]. Rahman and Sultana [38] examined radiative heat flux with variable heat flux in a porous medium. Recently Bakr [39] presented an analysis on MHD free convection and mass transfer adjacent to moving vertical plate for micropolar fluid in a rotating frame of reference in presence of heat generation/absorption and a chemical reaction. Radhakrishnamachary [40] analyzed the flow of micropolar fluid through a constricted channel. Rees and Pop [41] discussed the free convection boundary layer flow of a micropolar fluid from a vertical flat plate. Sharma and Gupta [42] studied the effects of medium permeability on thermal convection in micropolar fluids. Prathap Kumar *et al.* [43] have investigated the problem of fully developed free convective flow of micropolar and viscous fluids in a vertical channel. Muthu *et.al.* [44] studied peristaltic motion of micropolar fluid in circular cylindrical tubes. Srinivasacharya *et.al.* [45] analyzed the unsteady stokes flow of micropolar fluid between two parallel porous plates. Muthuraj and Srinivas [46] investigated fully developed MHD flow of a micropolar and viscous fluids in a vertical porous space using Ham. Kim [47] investigated the effects of heat and mass transfer in the MHD micropolar fluid flow past a vertical moving plate. The simultaneous effects of heat and mass transfer with chemical reaction are of great importance to engineers and scientists because of its occurrence in many branches of science and engineering. Recently Das [55] has studied the effect of first order chemical reaction in thermal radiation hydro magnetic free convective heat and mass transfer flow of a micropolar fluid bounded by the semi infinite porous plate with constant heat & source in a rotating frame of reference. In most of the cases, the Hall term is ignored by applying Ohm's law as it has no marked effect for small magnetic fields. However, to study the effects of strong magnetic fields on the electrically conducting fluid flow, we see that the influence of the electromagnetic force is noticeable and causes anisotropic electrical conductivity in the plasma. This anisotropy in the electrical conductivity of the plasma produces a current known as the Hall current. The Hall Effect is important when the magnetic field is strong or when the collision frequency is low, causing the Hall parameter to be significant (Sutton and Sherman [56]). The effects of Hall current on the fluid flow in rotating channels have many engineering applications in flows of laboratory plasmas, in MHD power generation, in MHD accelerators, and in several astrophysical and geophysical situations. Thus, in a rotating system the effects of Hall current on MHD flow in parallel plate channels have been investigated by many researchers. Hall effects on unsteady MHD free and forced convection flow in a porous channel have been studied by Sivaprasad *et al.* [59]. Hayat *et al* [60] discussed the boundary value problem for oscillating rotating flows of MHD Oldroyd – B fluid in a porous space.

In this paper we investigate the effect of combined influence of Hall effect, chemical reaction, and radiation absorption on rotating hydromagnetic convective heat and mass transfer flow of a micro polar fluid bounded by a semi infinite porous plate in the presence of heat generating sources. The dimensionless grouping equations for this investigation on solved using small perturbation approximation. The effect of various dimensionless parameters entering to the problem on the velocity & temperature concentration micro rotation profiles across the boundary layer are investigated to graphs. Also the result of the couple stress coefficient, the rate of heat and mass transfer at the wall are evaluated for different parameters.

## 2. FORMULATION AND SOLUTION OF THE PROBLEM

We consider the unsteady three dimensional flow of an incompressible, viscous, electrically conducting micropolar fluid past a semi-infinite vertical permeable moving plate embedded in a uniform porous medium and subjected to a constant transverse magnetic field  $B_0$  in the presence of thermal and concentration buoyancy effects with chemical reaction and thermal radiation. It is assumed that there is no applied voltage which implies the absence of an electric field. The flow is assumed to be in the x-direction which is taken along the plate in the upward direction and z-direction is normal to it. Also it is assumed that the whole system is rotate with a constant frame  $\Omega$  in a micropolar fluid about z-axis. The fluid is assumed to be gray, absorbing-emitting but not scattering medium. The radiation heat flux in x-direction is considered negligible in comparison that the z-direction. Due to the semi-infinite plate surface assumption, furthermore, the flow variables are functions z and time only.

When the strength of the magnetic field is very large we include the Hall current so that the generalized Ohm's law is modified to

$$\bar{J} + \omega_e \tau_e \bar{J} \times \bar{H} = \sigma (\bar{E} + \mu_e \bar{q} \times \bar{H}) \quad (1)$$

where  $\bar{q}$  is the velocity vector.  $\bar{H}$  is the magnetic field intensity vector.  $\bar{E}$  is the electric field,  $\bar{J}$  is the current density vector,  $\omega_e$  is the cyclotron frequency,  $\tau_e$  is the electron collision time,  $\sigma$  is the fluid conductivity and  $\mu_e$  is the magnetic permeability. Neglecting the electron pressure gradient, ion-slip and thermo-electric effects and assuming the electric field  $E=0$ , equation (1) reduces

$$j_x - m H_0 J_y = -\sigma \mu_e H_0 w \quad (2)$$

$$J_y + m H_0 J_x = \sigma \mu_e H_0 u \quad (3)$$

where  $m = \omega_e \tau_e$  is the Hall parameter.

Substituting  $J_x$  and  $J_y$  from equations (2) & (3) the governing equations are

$$u_t - w_0(1 - \varepsilon A e^{mt})u_z - 2\Omega v = (\nu + \nu_r)u_{yy} + \frac{\sigma \mu_e^2 H_0^2}{1 + m^2 H_0^2} (u + m H_0 v) J_y + \beta g(T - T_\infty) + \beta^* g(C - C_\infty) - \nu_r \omega_{2,z} \quad (4)$$

$$v_t - w_0(1 - \varepsilon A e^{mt})v_z + 2\Omega u = (\nu + \nu_r)v_{yy} - \frac{\sigma \mu_e^2 H_0^2}{1 + m^2 H_0^2} (m H_0 u - v) J_x + \nu_r \omega_{1,z} \quad (5)$$

$$\frac{\partial \omega_1}{\partial t} - w_0(1 + \varepsilon e^{mt}) \frac{\partial \omega_1}{\partial z} = \frac{A}{\rho j} \frac{\partial^2 \omega_1}{\partial z^2} \quad (6)$$

$$\frac{\partial \omega_2}{\partial t} - w_0(1 + \varepsilon e^{mt}) \frac{\partial \omega_2}{\partial z} = \frac{A}{\rho j} \frac{\partial^2 \omega_2}{\partial z^2} \quad (7)$$

The energy equation is

$$\rho C_p \left( \frac{\partial T}{\partial t} - w_0(1 + \varepsilon e^{mt}) \frac{\partial T}{\partial z} \right) = k_f \frac{\partial^2 T}{\partial z^2} + Q(T_e - T) - \frac{\partial(q_r)}{\partial z} + Q_1(C - C_\infty) \quad (8)$$

The diffusion equation is

$$\left( \frac{\partial C}{\partial t} - w_o(1 + \varepsilon e^{nt}) \right) \frac{\partial C}{\partial z} = D_1 \frac{\partial^2 C}{\partial z^2} \quad (9)$$

The equation of state is

$$\rho - \rho_0 = -\beta(T - T_o) - \beta^*(C - C_o) \quad (10)$$

Where T,C are the temperature and concentration in the fluid.  $k_f$  is the thermal conductivity,  $C_p$  is the specific heat constant pressure,  $D_1$  is molecular diffusivity,  $\beta$  is the coefficient of thermal expansion,  $\beta^*$  is the coefficient of volume expansion,  $Q$  is the strength of the heat source,  $Q_1$  is the radiation absorption coefficient and  $q_r$  is the radiative heat flux.

By Rosseland approximation, the radiative heat flux is given by

$$q_r = -\frac{4\sigma^*}{3\beta_r} \frac{\partial(T'^4)}{\partial z} \quad (11)$$

Expanding  $T'^4$  about  $T_e$  by Taylor expansion and neglecting the higher order terms we get

$$T'^4 \cong 4TT_e^3 - 3T_e^4 \quad (12)$$

where  $\sigma^*$  is the Stefan-Boltzmann constant and  $\beta_r$  is the mean absorption coefficient. Substituting (11) & (12) in (8) we obtain

$$\rho C_p \left( \frac{\partial T}{\partial t} - w_o(1 + \varepsilon e^{nt}) \frac{\partial T}{\partial z} \right) = k_f \frac{\partial^2 T}{\partial z^2} + Q(T_\infty - T) + Q_1(C - C_\infty) + \frac{16\sigma^* T_\infty^2}{3\beta_R} \frac{\partial^2 T}{\partial z^2} \quad (13)$$

The boundary conditions are

$$\begin{aligned} u = v = 0, \omega_1 = \omega_2 = 0, T = T_\infty, C = C_\infty \text{ for } t \leq 0 \\ u = U_r(1 + \varepsilon \exp(nt)), v = 0, \omega_1 = -0.5 \frac{\partial v}{\partial z}, \omega_2 = 0.5 \frac{\partial u}{\partial z}, \\ T = T_w + \varepsilon(T_w - T_\infty)e^{nt}, C = C_w + \varepsilon(C_w - C_\infty)e^{nt} \text{ on } z = 0 \\ u = v = 0, \omega_1 = 0, \omega_2 = 0, T = T_\infty, C = C_\infty \text{ as } z \rightarrow \infty, t > 0 \end{aligned} \quad (14)$$

On introducing the non-dimensional variables

$$\begin{aligned} z' = \frac{zU_r}{\nu}, t' = \frac{tU_r^2}{\nu}, u' = \frac{u}{U_r}, v' = \frac{v}{U_r}, n' = \frac{nv}{U_r^2}, \omega_1' = \frac{\omega_1\nu}{U_r^2}, \omega_2' = \frac{\omega_2\nu}{U_r^2}, \\ \theta = \frac{T - T_\infty}{T_w - T_\infty}, C' = \frac{C - C_\infty}{C_w - C_\infty} \end{aligned} \quad (15)$$

the equations (4)-(7),(9)&(13) reduces to

$$u_t' - S(1 + \varepsilon e^{nt'})u_{z'} - Rv = (1 + \Delta)u_{yy} - \frac{M^2}{1 + m^2}(u + mw) + G(\theta + NC) - \omega_{2,z} \quad (16)$$

$$v_t' - S(1 + \varepsilon e^{nt'})v_{z'} + Ru = (1 + \Delta)v_{yy} + \frac{M^2}{1 + m^2}(mu - w) + \omega_{1,z} \quad (17)$$

$$\frac{\partial \omega_1}{\partial t} - S(1 + \varepsilon e^{nt}) \frac{\partial \omega_1}{\partial z} = \lambda \frac{\partial^2 \omega_1}{\partial z^2} \quad (18)$$

$$\frac{\partial \omega_2}{\partial t} - S(1 + \varepsilon e^{nt}) \frac{\partial \omega_2}{\partial z} = \lambda \frac{\partial^2 \omega_2}{\partial z^2} \quad (19)$$

$$(\theta_t - S(1 + \varepsilon e^{nt}) \theta_z = \frac{(3N_1 + 4)}{3N_1 P_r} (\theta_{zz}) - \alpha \theta + Q_1 C \quad (20)$$

$$(C_t - S(1 + \varepsilon e^{nt}) C_z = \frac{1}{Sc} \frac{\partial^2 C}{\partial z^2} \quad (21)$$

where

$$R = \frac{2\Omega \nu}{U_r^2} \text{ (Rotation parameter), } M = \frac{B_0}{U_r} \sqrt{\sigma \nu / \rho} \text{ (Magnetic parameter)}$$

$$P_r = \frac{\mu C_p}{k_f} \text{ (Prandtl number), } Sc = \frac{\nu}{D_1} \text{ (Schmidt Number)}$$

$$Q_1 = \frac{Q_1' (C_w - C_\infty) \nu^2}{k_f (T_w - T_\infty) U_r^2} \text{ (Radiation absorption parameter), } G = \frac{\beta g \nu (T_w - T_\infty)}{U_r^3} \text{ (Grashof number)}$$

$$N = \frac{\beta^* (C_w - C_\infty)}{\beta (T - T_\infty)} \text{ (Buoyancy ratio), } S = \frac{w_o}{U_r} \text{ (Suction parameter)}$$

$$N_1 = \frac{\beta_R k_f}{4\sigma^* T_\infty^3} \text{ (Radiation parameter), } m = \omega_e t \text{ (Hall parameter)}$$

$$\alpha = \frac{Q \nu^2}{U_r^2} \text{ (Heat source parameter), } \lambda = \frac{\Delta}{\mu j} \text{ (micro rotation parameter)}$$

$$\Delta = \frac{\nu_r}{\nu} \text{ (Viscosity ratio parameter), } N_2 = \frac{3N_1}{3N_1 + 4} \quad P_1 = PN_2 \quad \alpha_1 = \alpha N_2$$

The transformed boundary conditions are

$$u = v = 0, \omega_1 = \omega_2 = 0, \theta = 0, C = 0 \text{ for } t \leq 0$$

$$u = (1 + \varepsilon \exp(nt)), v = 0, \omega_1 = -0.5 \frac{\partial v}{\partial z}, \omega_2 = 0.5 \frac{\partial u}{\partial z}, \quad (22)$$

$$\theta = 1 + \varepsilon e^{nt}, C = 1 + \varepsilon e^{nt} \text{ on } z = 0$$

$$u = v = 0, \omega_1 = 0, \omega_2 = 0, \theta = 0, C = 0 \text{ as } z \rightarrow \infty, t > 0$$

We now simplify the equations (16)-(21) by putting the fluid velocity and angular velocity in the complex form as

$$q = u + iv, \quad \omega = \omega_1 + i\omega_2$$

and we obtain

$$q_t - S(1 + \varepsilon e^{nt}) q_z + iRq = (1 + \Delta) q_{yy} - D^{-1} q - \frac{M^2(1 - im)}{1 + m^2} q + i\omega_z + G(\theta + NC) \quad (23)$$

$$\frac{\partial \omega}{\partial t} - S(1 + \varepsilon e^{nt}) \frac{\partial \omega}{\partial z} = \lambda \frac{\partial^2 \omega}{\partial z^2} \quad (24)$$

$$(\theta_t - S(1 + \varepsilon e^{nt})\theta_z = \frac{(3N_1 + 4)}{3N_1 P_r}(\theta_{zz}) - \alpha\theta + Q_1 C \quad (25)$$

$$(C_t - S(1 + \varepsilon e^{nt})C_z = \frac{1}{Sc} \frac{\partial^2 C}{\partial z^2} \quad (26)$$

The corresponding boundary conditions are

$$\begin{aligned} q = 0, \omega = 0, \theta = 0, C = 0 \text{ for } t \leq 0 \\ q = 1 + \varepsilon e^{nt}, \omega = 0.5 \frac{\partial q}{\partial z}, \theta = 1 + \varepsilon e^{nt}, C = 1 + \varepsilon e^{nt} \text{ at } z = 0 \\ q = 0, \omega = 0, \theta = 0, C = 0 \text{ as } z \rightarrow \infty \text{ for } t > 0 \end{aligned} \quad (27)$$

### 3. METHOD OF SOLUTION

To find the analytical solutions of the above system of partial differential equations (23)-(26) in the neighbourhood of the plate under the above boundary conditions (27), we express  $q, \omega, \theta$  and  $C$  as

$$\begin{aligned} q &= q_0 + \varepsilon e^{nt} q_1 \\ \omega &= \omega_0 + \varepsilon e^{nt} \omega_1 \\ \theta &= \theta_0 + \varepsilon e^{nt} \theta_1 \\ C &= C_0 + \varepsilon e^{nt} C_1 \end{aligned} \quad (28)$$

Invoking the above expansions into the equations (23)-(26) and equating the steady And transient parts and neglecting the higher order terms of  $O(\varepsilon^2)$ , we obtain the following set of equations to the zeroth order are

$$-s \frac{\partial q_0}{\partial z} = (1 + \Delta) \frac{\partial^2 q_0}{\partial z^2} - \left( M_1^2 + iR \right) q_0 + i \frac{\partial \omega_0}{\partial z} + G(\theta_0 + NC) \quad (29)$$

$$\lambda \frac{\partial^2 \omega_0}{\partial z^2} + S \frac{\partial \omega_0}{\partial z} = 0 \quad (30)$$

$$-S \frac{\partial \theta_0}{\partial z} = \frac{(3N_1 + 4)}{3N_1 P_r} \frac{\partial^2 \theta_0}{\partial z^2} - \alpha \theta_0 + Q_1 C_0 \quad (31)$$

$$-S \frac{\partial C_0}{\partial z} = \frac{1}{Sc} \frac{\partial^2 C_0}{\partial z^2} - k C_0 \quad (32)$$

and to the first order are

$$(1 + \Delta) \frac{\partial^2 q_1}{\partial z^2} + S \frac{\partial q_1}{\partial z} - (D^{-1} + M_1^2 + n + iR) q_1 + i \frac{\partial \omega_1}{\partial z} = -S \frac{\partial q_0}{\partial z} - G(\theta_1 + NC_1) \quad (33)$$

$$\lambda \frac{\partial^2 \omega_1}{\partial z^2} + S \frac{\partial \omega_1}{\partial z} = 0 \quad (34)$$

$$\frac{\partial^2 \theta_1}{\partial z^2} + S P_1 \frac{\partial \theta_1}{\partial z} - (\alpha_1 + n) \theta_1 = -S \frac{\partial \theta_0}{\partial z} - Q_1 C_1 \quad (35)$$

$$\frac{\partial^2 C_1}{\partial z^2} + S S c \frac{\partial C_1}{\partial z} - (k S c + n) C_1 = 0 \quad (36)$$

The corresponding boundary conditions can be written as

$$\begin{aligned} q_o = 1, q_1 = 1, \omega_o = 0.5 \frac{\partial q_o}{\partial z}, \omega_1 = 0.5 \frac{\partial q_1}{\partial z}, \\ \theta_o = 1, \theta_1 = 1, C_o = 1, C_1 = 1 \text{ at } z = 0 \\ q_o = q_1 = 0, \omega_o = \omega_1 = 0, \theta_o = \theta_1 = 0, \\ C_o = C_1 = 0 \text{ as } z \rightarrow \infty \text{ for } t > 0 \end{aligned} \quad (37)$$

Solving equations (29)-(35) under the boundary conditions (37) we obtain the expressions for the translational velocity, microrotation, temperature and concentration as

$$C_o = \exp(-m_1 y)$$

$$\theta_o = (1 - a_2) \exp(-m_2 y) + a_1 \exp(-m_1 y)$$

$$\omega_o = a_3 \exp(-m_3 y)$$

$$q_o = a_7 \exp(-m_4 y) + a_4 \exp(-m_2 y) + a_5 \exp(-m_1 y) + a_6 a_3 \exp(-m_3 y)$$

$$C_1 = (1 - a_9) \exp(-m_5 y) + a_9 \exp(-m_1 y)$$

$$\theta_1 = a_{13} \exp(-m_6 y) + a_{11} \exp(-m_5 y) + a_{12} \exp(-m_1 y)$$

$$\omega_1 = a_{14} \exp(-m_7 y)$$

$$q_1 = a_{19} \exp(-m_8 y) + a_{16} \exp(-m_5 y) + a_{17} \exp(-m_1 y) + a_{18} a_{14} \exp(-m_7 y)$$

#### 4. RATE OF HEAT AND MASS TRANSFER

The rate of heat transfer (Nusselt Number) at  $z=0$  is given by

$$Nu_{z=0} = \left( \frac{\partial \theta_o}{\partial z} + \epsilon e^{nt} \frac{\partial \theta_1}{\partial z} \right)_{z=0} = a_{22} + \epsilon e^{nt} a_{23} \text{ The rate of mass transfer (Sherwood Number)}$$

$$\text{at } z=0 \text{ is given by } Sh_{y=0} = \left( \frac{\partial C_o}{\partial z} + \epsilon e^{nt} \frac{\partial C_1}{\partial z} \right)_{z=0} = -m_1 + \epsilon e^{nt} a_{24}$$

$$\text{The couple stress coefficient at } z=0 \text{ is given by } C_w = \left( \frac{\partial \omega_o}{\partial z} + \epsilon e^{nt} \frac{\partial \omega_1}{\partial z} \right)_{z=0} = -a_3 m_3 - \epsilon e^{nt} a_{14} m_7$$

$$\text{where } M_1^2 = \frac{M^2(1-im)}{1+m^2} \quad m_1 = (SSc + \sqrt{S^2 Sc^2 + 4(KSc)})/2, \quad m_2 = (SP_1 + \sqrt{S^2 P_1^2 + 4\alpha_1})/2,$$

$$m_3 = \frac{S}{\lambda}, m_4 = (S + \sqrt{S^2 + 4(M_1^2 + iR)})/2(1 + \Delta)$$

$$m_5 = (SSc + \sqrt{S^2 Sc^2 + 4(kSc + n)})/2,$$

$$m_6 = (SP_1 + \sqrt{S^2 P_1^2 + 4(\alpha_1 + n)})/2, m_7 = \frac{S + \sqrt{S^2 + 4n}}{2\lambda}$$

$$m_8 = (S + \sqrt{S^2 + 4(M_1^2 + iR + n)})/2(1 + \Delta)$$

$$a_1 = -\frac{Q_1}{(m_1^2 - SP_1 m_1 - \alpha_1)}, a_2 = 1 - a_1, \quad a_4 = -G(1 - a_1)/(1 + \Delta)m_2^2 - Sm_2 - (M_1^2 + iR)$$

$$a_5 = -G(a_1 + N)/((1 + \Delta)m_1^2 - Sm_1 - (M_1^2 + iR))$$

$$a_6 = -ia_3 m_3 / ((1 + \Delta)m_3^2 - Sm_3 - (M_1^2 + iR)), \quad a_7 = 1 - a_4 - a_5 - a_6 a_3$$

$$a_3 = \frac{0.5(a_4 m_2 + a_5 m_1 - (a_4 + a_5 + 1)m_4)}{(1 + 0.5a_7(m_4 + m_3))}, a_9 = \frac{SScm_1}{m_1^2 - SS_c m_1 - (kSc + n_1)}, a_{10} = 1 + a_9$$

$$a_{11} = -\frac{Q_1(1 - a_9)}{(m_5^2 - SP_1 m_5 - (\alpha_1 + n))}, a_{12} = -\frac{Q_1 a_9}{(m_5^2 - SP_1 m_5 - (\alpha_1 + n))}$$

$$a_{13} = 1 - a_{11} - a_{12}, a_{15} = -\frac{Ga_{13}}{(1 + \Delta)m_6^2 - Sm_6 - (M_1^2 + iR + n)}$$

$$a_{16} = -\frac{G(a_{11} + Na_{10})}{(1 + \Delta)m_5^2 - Sm_5 - (M_1^2 + iR + n)}, a_{17} = -\frac{G(Na_9 + a_{12})}{(1 + \Delta)m_1^2 - Sm_1 - (M_1^2 + iR + n)}$$

$$a_{18} = -\frac{im_7 a_{14}}{(1 + \Delta)m_7^2 - Sm_7 - (M_1^2 + iR + n)}, \quad a_{19} = 1 - a_{15} - a_{16} - a_{17} - a_{18} a_{14}$$

$$a_{20} = -a_7 m_4 - a_4 m_2 - a_5 m_1 - a_6 a_3 m_3, a_{21} = -a_{19} m_8 - a_{15} m_6 - a_{16} m_5 - a_{17} m_1 - a_{18} a_{14} m_7$$

$$a_{22} = +(a_9 - 1)m_2 - a_1 m_1, a_{23} = -a_{13} m_6 - a_{11} m_5 - a_{12} m_1, a_{24} = m_5(a_9 - 1) - a_9 m_1$$

## 5. RESULTS AND DISCUSSION

We analyze the combined effect of Hall currents, thermal Radiation and Radiation absorption on Convective heat and mass transfer flow of a micro polar fluid past a vertical porous plate. The velocity, temperature, concentration and the micro rotation are analyzed for different variations.

Fig 1-7 represents the primary velocity  $u$  with variations in  $m$ ,  $R$ ,  $K$ ,  $Q$ ,  $N_1$ ,  $\lambda$  and  $\Delta$ . It is found that the primary velocity enhances with increase in  $|G|$  and Rotation parameter  $R$  (fig1&7). An increase in Hall parameters  $m \leq 1.5$  reduces  $|u|$  and enhances with higher  $m \geq 2.5$  (fig 1). The effect of the suction velocity on  $u$  is shown in fig-2. Fig-3 represents  $u$  with chemical reaction parameter  $\gamma$ . It can be seen from the profiles that the primary velocity enhances with increase in  $\gamma \leq 1.5$  and enhances with higher  $\gamma \geq 2.5$ . From fig.4 we find that an increase in the Radiation absorption parameter  $Q_1$  results in an enhancement of  $|u|$ . Fig-5 represents  $u$  with Radiation parameter  $N_1$ . It is found that higher the Radiative heat flux, larger  $|u|$  in the entire flow region. Fig-6 represents  $u$  with microrotation parameter  $\lambda$ . It can be seen from the profiles that  $|u|$  enhances with increase in  $\lambda$ . Fig-7 represents  $u$  with viscosity ratio parameter  $\Delta$ . We notice a depreciation in  $u$  with increase in  $\Delta$ .

The secondary velocity ( $v$ ) is shown in fig.8-14 for different parametric values. Fig-8 represents  $v$  with Hall parameter  $m$ . It is found that an increase in  $m \leq 1.5$  enhances  $|v|$  and for further higher  $m \geq 2.5$ ,  $|v|$  reduces in the boundary. The variation of  $v$  with chemical reaction parameter  $k$  shows that  $|v|$  enhances with  $k \leq 1.5$  and depreciates with  $k \geq 2.5$  (fig.9). An increase in the Radiation absorption parameter  $Q_1 \leq 1$  reduces  $|v|$  and enhances with higher  $Q_1 \geq 1.5$ . Higher the Radiative heat flux larger the magnitude of secondary velocity  $v$  (fig-10). An increase in radiation parameter  $N_1$  enhances  $|v|$  (fig 11). Fig-13 represents  $v$  with Rotation parameter  $R$ . It is observed that  $|v|$  exhibits decreasing tendency with increase in  $R$ . Fig-12 represents  $v$  with microrotation parameter  $\lambda$ . It is found that  $|v|$  enhances with increase in  $\lambda \leq 0.5$  and for higher  $\lambda \geq 0.7$  it reduces in the boundary layer. An increase in viscosity ratio parameter  $\Delta$  results in an enhancement in  $|v|$  in the entire flow region (fig.14).



The non-dimensional temperature ( $\Theta$ ) is shown in fig.15-17 for different values of  $k$ ,  $Q_1$ , and  $N_1$ . It is found that the non-dimensional temperature is positive for all variations. This shows that the actual temperature is greater than the ambient temperature  $T_\infty$ . The actual temperature enhances with increase in  $Q_1$  or radiation parameter  $N_1$  (fig 16). Also the non dimensional temperature depreciates in the degenerating chemical reaction case (17).

The non-dimensional concentration distribution ( $C$ ) is shown in fig. 18-19 for different values of  $Sc$ ,  $k$ . It is found that the non-dimensional concentration is positive for all variations. It is found that the actual concentration depreciates with increase in  $Sc$  (figs. 18). Also it reduces in the degenerating chemical reaction case (fig.19).

The micro rotation distribution ( $\omega$ ) is shown in fig. 20-25 for different values of different parametric values. An increase in the Hall parameter  $m \leq 2.5$  results in an enhancement in  $|\omega|$  and enhances with higher  $m \geq 3.5$  (fig.20). An increase in  $Q_1 \leq 1.5$  leads to a depreciation in  $|\omega|$  and for higher  $Q_1 \geq 2.5$  we notice an enhancement in  $|\omega|$  in the entire boundary layer. (fig.22). The effect of radiation parameter  $N_1$  on  $\omega$  is shown in fig.23. It is found that higher the radiative heat flux, larger  $|\omega|$  in the region. Fig.21 represents  $\omega$  with micro rotation parameter  $k$ . It can be seen from the profiles that an increase in  $k$  enhances  $|\omega|$  in the flow region. Fig-24 represents  $v$  with microrotation parameter  $\lambda$ . It is found that  $|\omega|$  enhances with increase in  $\lambda \leq 0.5$  and for higher  $\lambda \geq 0.7$  it reduces in the boundary layer. The variation of  $\omega$  with viscosity ratio parameter  $\Delta$  is shown in fig.25. We notice an increasing tendency in  $|\omega|$  with increase in  $\Delta$ .

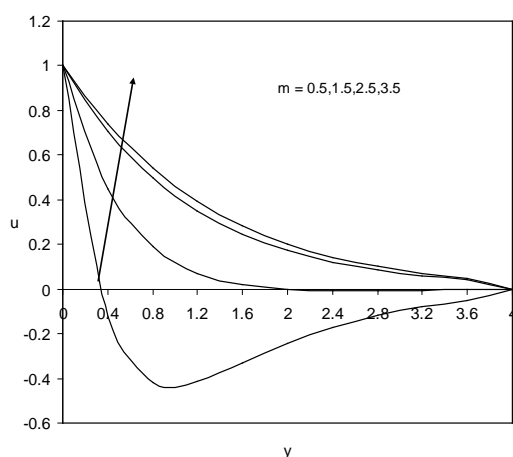


Fig. 1 : Variation of u with m

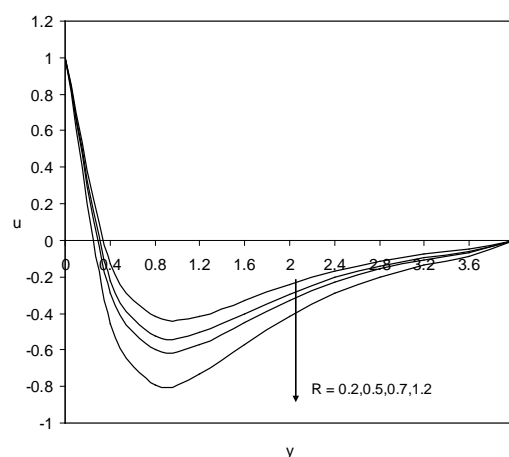


Fig. 2 : Variation of u with R

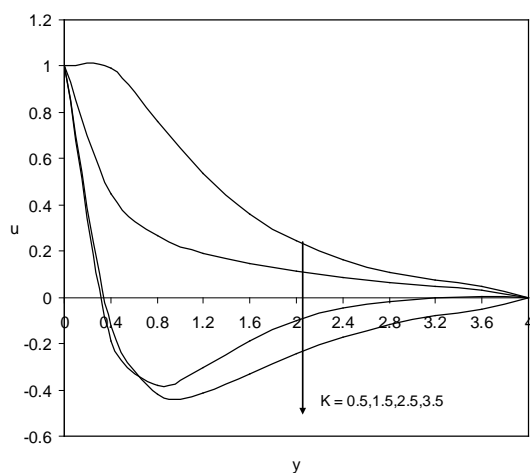


Fig. 3 : Variation of u with K

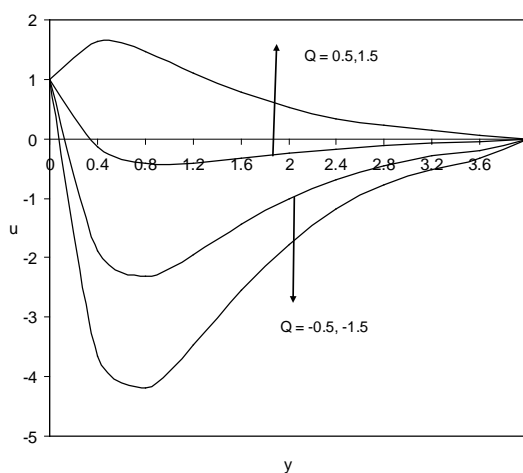


Fig. 4: Variation of u with Q

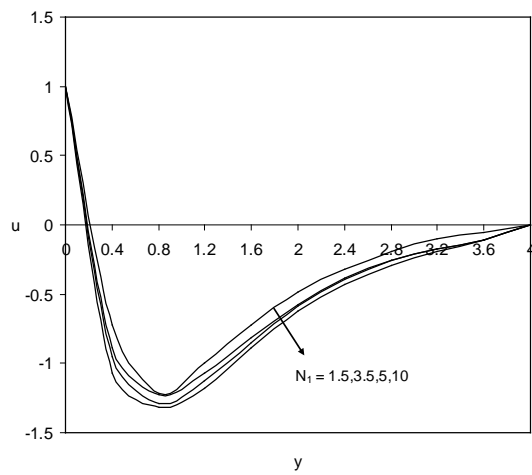


Fig. 5 : Variation of  $u$  with  $N_1$

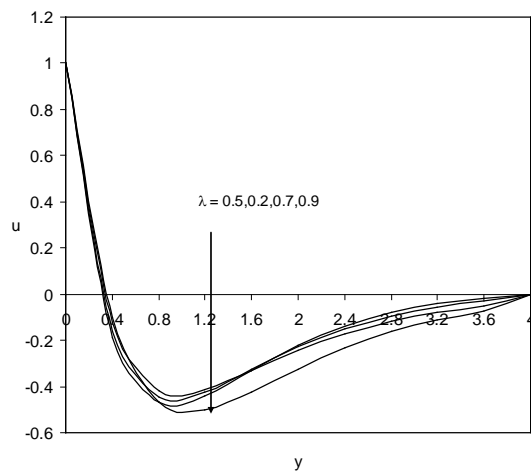


Fig. 6 : Variation of  $u$  with  $\lambda$

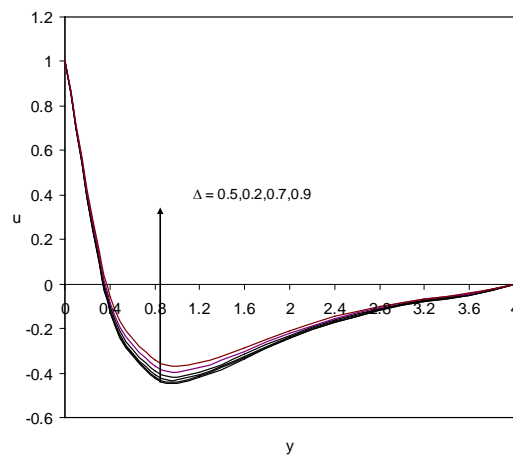


Fig. 7 : Variation of  $u$  with  $\Delta$

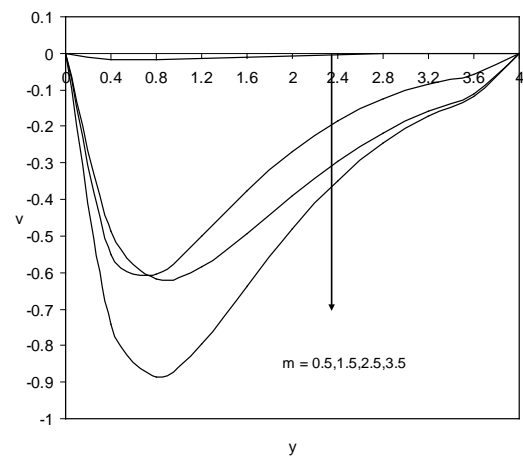


Fig. 8 : Variation of  $v$  with  $m$

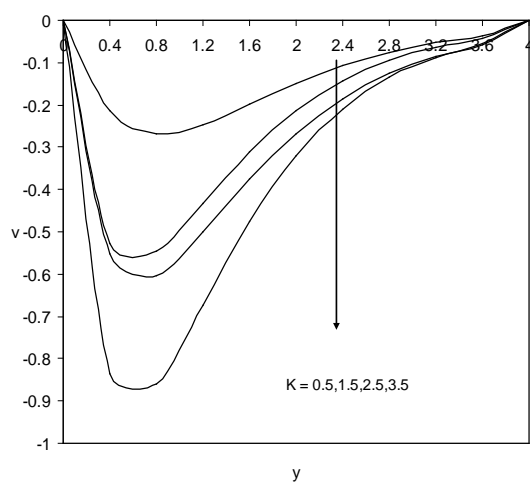


Fig. 9 : Variation of  $v$  with  $K$

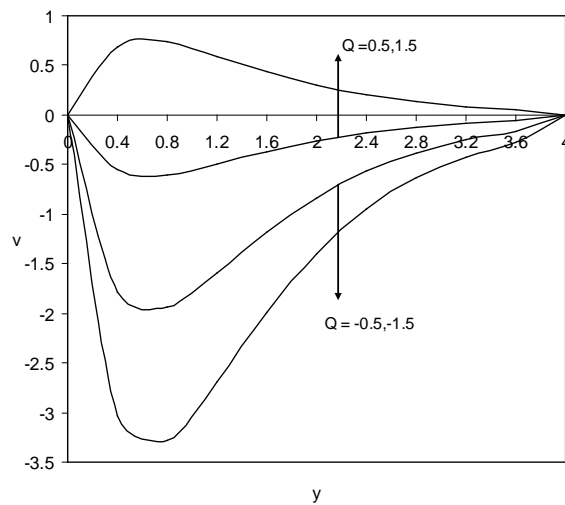


Fig. 10 : Variation of  $v$  with  $Q$

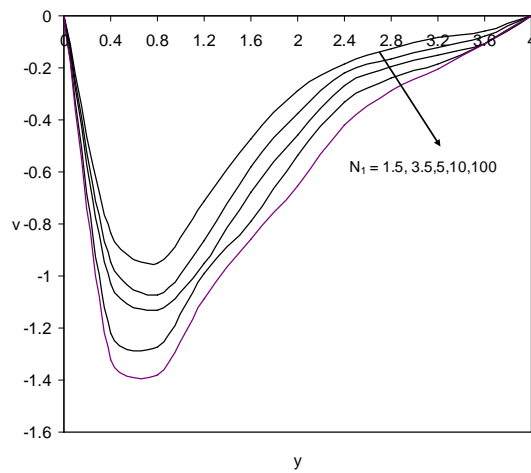


Fig. 11 : Variation of  $v$  with  $N_1$

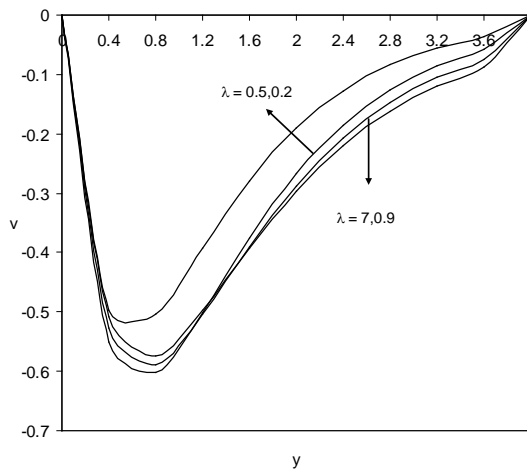


Fig. 12 : Variation of  $v$  with  $\lambda$

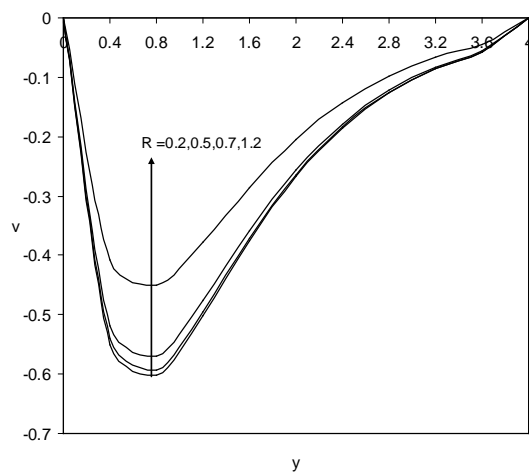


Fig. 13: Variation of  $v$  with  $R$

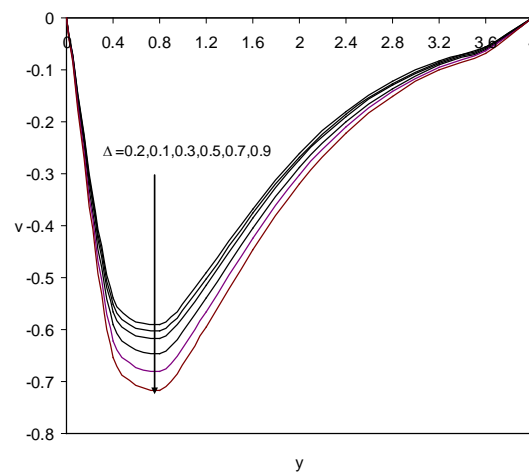


Fig. 14 : Variation of  $v$  with  $\Delta$

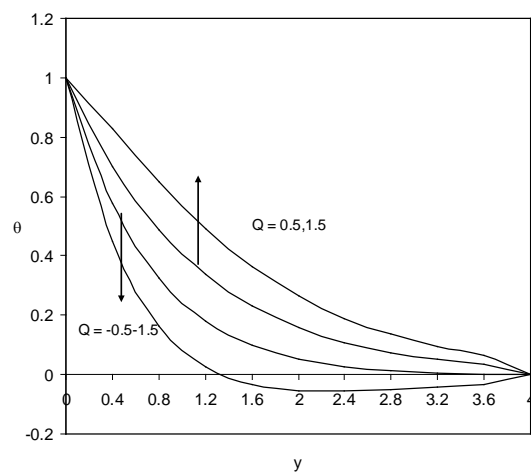


Fig. 15 : Variation of  $\theta$  with  $Q$

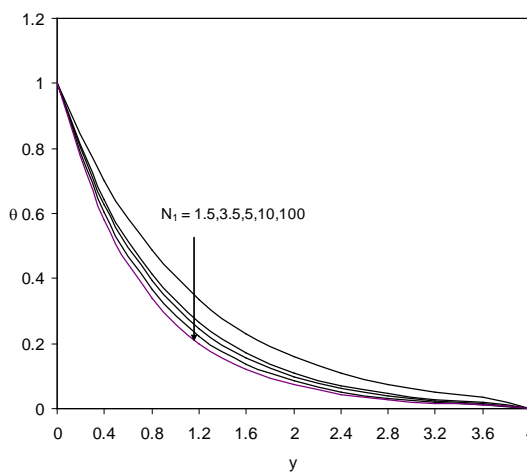


Fig. 16 : Variation of  $\theta$  with  $N_1$

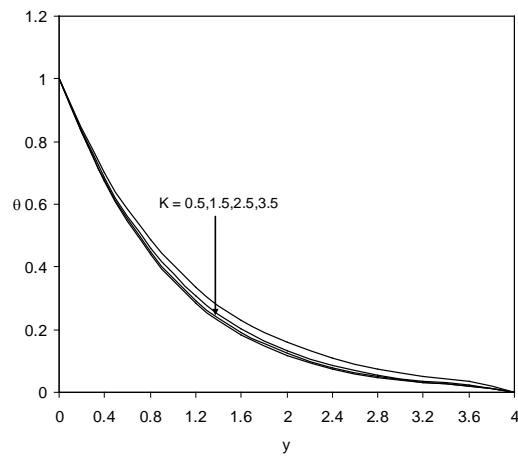


Fig. 17 : Variation of  $\theta$  with K

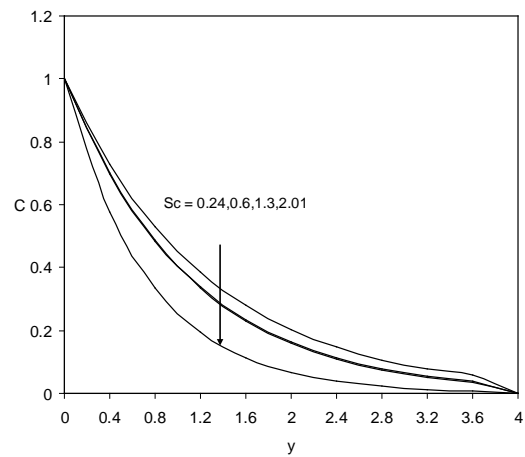


Fig. 18: Variation of C with Sc

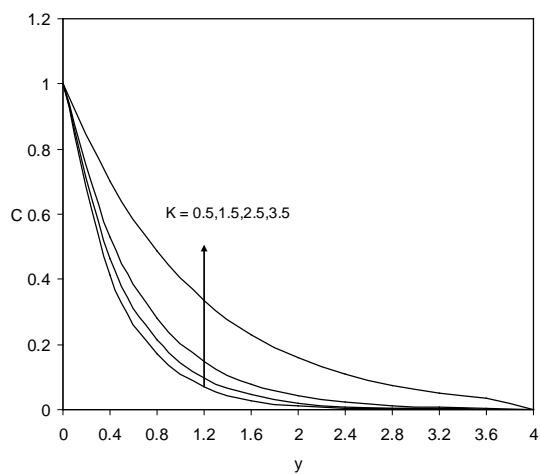


Fig. 19 : Variation of C with K

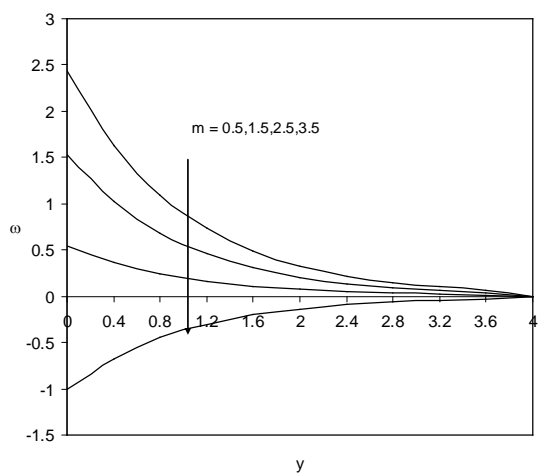


Fig. 20 : Variation of w with m

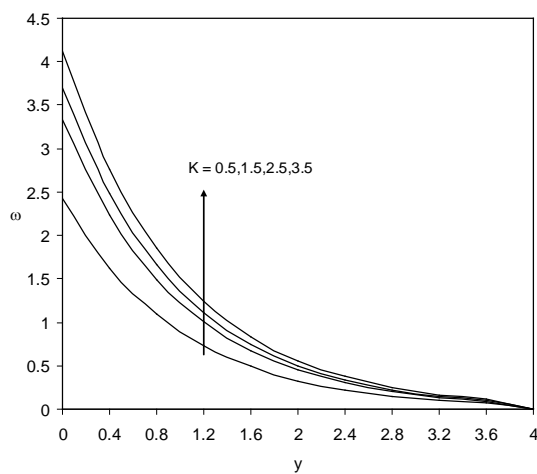


Fig. 21 : Variation of w with K

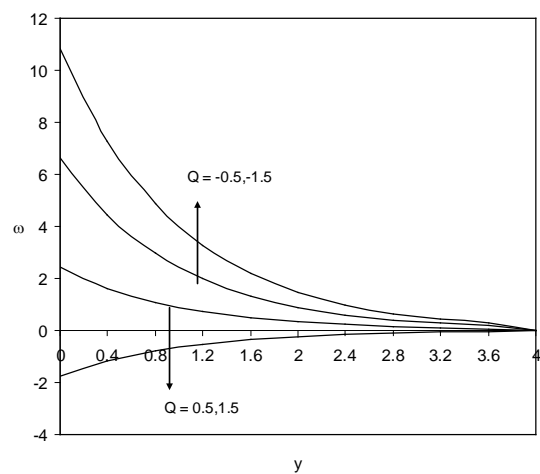


Fig. 22 : Variation of w with Q

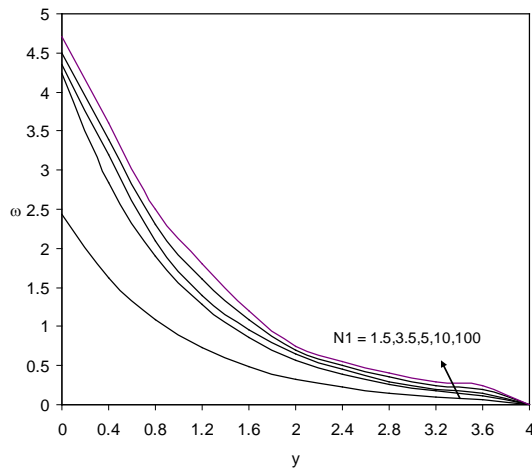


Fig. 23 : Variation of w with  $N_1$

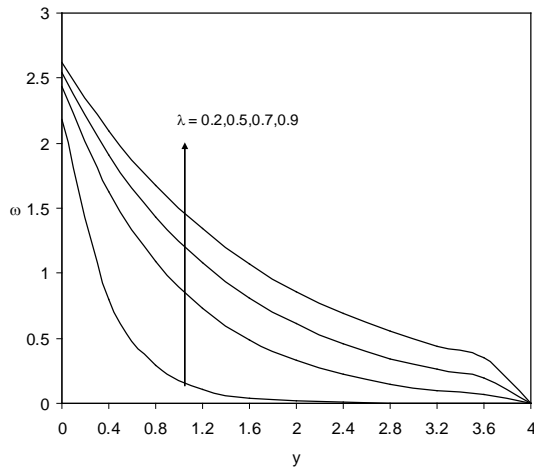


Fig. 24 : Variation of w with  $\lambda$

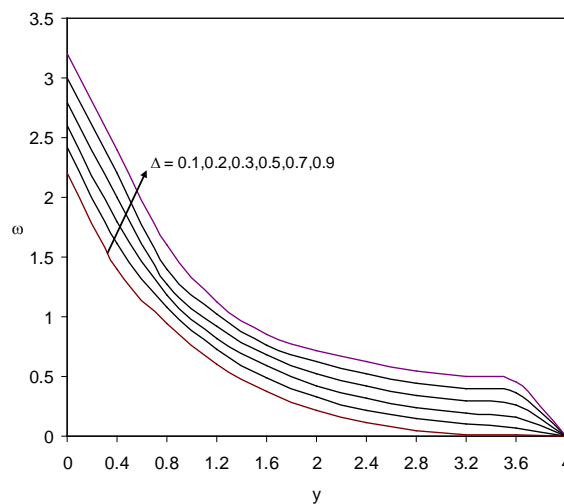


Fig. 25 : Variation of w with  $\Delta$

The Rate of heat transfer (Nusselt number) at  $\eta = 0$  is depicted in table.1. The variation of Nu with chemical reaction parameter  $K \leq 1.5$  leads to a reduction in  $|Nu|$  and for higher  $K \geq 2.5$ ; we notice an enhancement in  $|Nu|$ . An increase in the radiation absorption parameter  $Q_1$  results in an enhancement in  $|Nu|$  at the plate (table-1).

The rate of mass transfer (Sherwood number) at the Wall  $\eta = 0$  in  $|Nu|$  and for higher  $K \geq 2.5$ ; we notice an enhancement in  $|Nu|$ .

The Couple stress ( $C_w$ ) at  $\eta = 0$  is shown in tables 3-5 for different parametric values. An increase in  $Q_1 \leq 1.5$  reduces  $|C_w|$  and enhances with higher  $Q_1 \geq 2.5$ . An increase in the radiation parameter  $N_1 \leq 3.5$ , we notice a depreciation in  $|C_w|$  for  $G > 0$  and enhancement for  $G < 0$  and for further higher  $N_1 \geq 5$ ,  $|C_w|$  enhances for  $G > 0$  and reduces for  $G < 0$ . An increase in the rotation parameter  $R$  enhances  $|C_w|$ . With increase in microrotation parameter  $\lambda$   $|C_w|$  reduces and enhances for higher  $\lambda \geq 0.9$ . Also it reduces with increase in micro viscosity ratio parameter  $m$  leads to a depreciation. The Also  $|C_w|$  enhances in the degenerating chemical reaction parameter  $k$  (table.10). From table.3, we find that  $|C_w|$  enhances for  $G > 0$  and reduced for  $G < 0$  with increase in the Hall parameter  $m \leq 1.5$  and reduces with higher values of  $m \geq 2.5$ .

**Table - 1**  
Nusselt Number(Nu) at  $\eta=0$

Sc	I	II	III	IV	V
0.24	-1.7820	0.47593	-0.5822	-3.2613	-4.65399
0.6	-1.9512	-1.0873	-0.6983	-4.2496	-6.28833
1.3	-2.6542	-0.5886	-0.8787	-23.954	-39.0970
2.01	-1.248	-0.8843	-1.0382	2.3341	4.77006
K	0.5	1.5	2.5	0.5	0.5
Q	0.5	0.5	0.5	1.5	2.5

**Table - 2**Sherwood Number(Sh) at  $\eta=0$ 

Sc	I	II	III
0.24	-0.7872	-1.33761	-1.69151
0.6	-0.8424	-1.42976	-1.78360
1.3	-0.9594	-1.62460	-1.97478
2.01	-1.1077	-1.86994	-2.20647
K	0.5	1.5	2.5

**Table - 3**Couple stress(Cw) at  $\eta=0$ 

G	I	II	III	IV	V	VI	VII	VIII
10	0.03484	3.27509	-6.06123	-6.08860	-11.7112	-0.88666	-0.77910	-0.19351
20	-2.90286	4.01148	-14.0059	-13.6859	-25.5439	-3.47960	-2.92888	-0.24363
-10	4.13340	1.78445	9.88764	9.88764	15.50315	4.64543	4.56178	3.98238
-20	6.65133	0.97869	17.74663	17.66292	29.71136	7.08876	5.32633	3.46851
Q	0.5	1.5	1.5	2.5	3.5	0.5	0.5	0.5
m	0.5	0.5	0.5	0.5	0.5	1.5	2.5	3.5

**Table - 4**Couple stress(Cw) at  $\eta=0$ 

G	I	II	III	IV	V	VI	VII	VIII	IX
10	2.49488	1.93087	2.04346	2.15503	-1.1094	-0.2173	-0.63293	-0.7640	-0.8178
20	5.53553	3.43477	3.85550	4.69710	-2.3816	0.17291	-2.16496	-2.7064	-2.8534
-10	1.29809	1.86134	1.74913	1.63798	4.61685	2.38460	4.37766	4.45619	4.47865
-20	-1.00692	0.45597	0.28480	-0.1272	6.12719	2.36659	5.97493	6.50296	6.72277
$N_1$	1.5	3.5	5	10	1.5	1.5	1.5	1.5	1.5
$\lambda$	0.5	0.5	0.5	0.5	0.3	0.9	0.5	0.5	0.5
R	0.2	0.2	0.2	0.2	0.2	0.2	0.5	0.9	1.20

**Table - 5**Couple stress(Cw) at  $\eta=0$ 

G	I	II	III	IV	V	VI	VII
10	-0.8178	3.44497	4.12413	4.81686	-0.5251	-0.616	-0.672
20	-2.8534	3.87264	4.70311	5.289461	-3.1205	-3.238	-3.292
-10	4.47865	2.29668	3.13461	3.84684	4.30084	4.3620	4.4352
-20	6.72277	2.20431	2.63682	3.32315	6.53366	6.51378	6.9076
K	0.5	1.5	2.5	3.5	0.5	0.5	0.5
$\Delta$	0.2	0.2	0.2	0.2	0.5	0.7	0.9

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