

EFFECT OF CHEMICAL REACTION AND THERMO-DIFFUSION
ON NON-DARCY CONVECTIVE HEAT AND MASS TRANSFER FLOW
IN A VERTICAL CHANNEL WITH HEAT SOURCES

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ABSTRACT

We made attempt in this paper to study thermo-diffusion and dissipation effect on Non-Darcy convective heat and Mass transfer flow of a viscous fluid through a porous medium in a vertical channel with Radiation and heat sources. The governing equations flow, heat and mass transfer are solved by using regular perturbation method with δ , the porosity parameter as a perturbation parameter. The velocity, temperature, concentration, shear stress and rate of Heat and Mass transfer are evaluated numerically for different variations of parameter.

Keywords: Chemical Reaction, Thermo-diffusion, Non-Darcy, Heat and Mass Transfer, Heat Sources.

1. INTRODUCTION

The phenomenon of heat and mass transfer has been the object of extensive research due to its applications in Science and Technology. Such phenomena are observed in buoyancy induced motions in the atmosphere, in bodies of water, quasisolid bodies such as earth and so on.

Non – Darcy effects on natural convection in porous media have received a great deal of attention in recent years because of the experiments conducted with several combinations of solids and fluids covering wide ranges of governing parameters which indicate that the experimental data for systems other than glass water at low Rayleigh numbers, do not agree with theoretical predictions based on the Darcy flow model. This divergence in the heat transfer results has been reviewed in detail in Cheng [5] and Prasad et al. [16] among others. Extensive effects are thus being made to include the inertia and viscous diffusion terms in the flow equations and to examine their effects in order to develop a reasonable accurate mathematical model for convective transport in porous media. The work of Vafai and Tien [21] was one of the early attempts to account for the boundary and inertia effects in the momentum equation for a porous medium. They found that the momentum boundary layer thickness is of order of $\sqrt{\frac{k}{\epsilon}}$. Vafai and Thiyagaraja [22] presented analytical solutions for the velocity and temperature fields for the interface region using the Brinkman Forchheimer –extended Darcy equation. Detailed accounts of the recent efforts on non-Darcy convection have been recently reported in Tien and Hong [19], Cheng [5], Prasad et al [16], and Kladias and Prasad [9]. Here, we will restrict our discussion to the vertical cavity only. Poulikakos and Bejan [13] investigated the inertia effects through the inclusion of Forchheimer's velocity squared term, and presented the boundary layer analysis for tall cavities. They also obtained numerical results for a few cases in order to verify the accuracy of their boundary layer analysis for tall cavities. They also obtained numerical results for a few cases in order to verify the accuracy of their boundary layer solutions. Later, Prasad and Tuntomo [14] reported an extensive numerical work for a wide range of parameters, and demonstrated that effects of Prandtl number remain almost unaltered while the dependence on the modified Grashof number, Gr, changes significantly with an increase in the Forchheimer number. This result in reversal of flow regimes from boundary layer to asymptotic to conduction as the contribution of the inertia term increases in comparison with that of the boundary term. They also reported a criterion for the Darcy flow limit.

The Brinkman – Extended – Darcy modal was considered in Tong and Subramanian [20], and Lauriat and Prasad [23] to examine the boundary effects on free convection in a vertical cavity. While Tong and Subramanian performed a Weber – type boundary layer analysis, Lauriat and Prasad solved the problem numerically for A=1 and 5. It was shown that for a fixed modified Rayleigh number, Ra, the Nusselt number; decrease with an increase in the Darcy number; the

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reduction being larger at higher values of Ra. A scale analysis as well as the computational data also showed that the transport term $(v \cdot \nabla)v$, is of low order of magnitude compared to the diffusion plus buoyancy terms. A numerical study based on the Forchheimer-Brinkman-Extended Darcy equation of motion has also been reported recently by Beckerman et al [4]. They demonstrated that the inclusion of both the inertia and boundary effects is important for convection in a rectangular packed – sphere cavity.

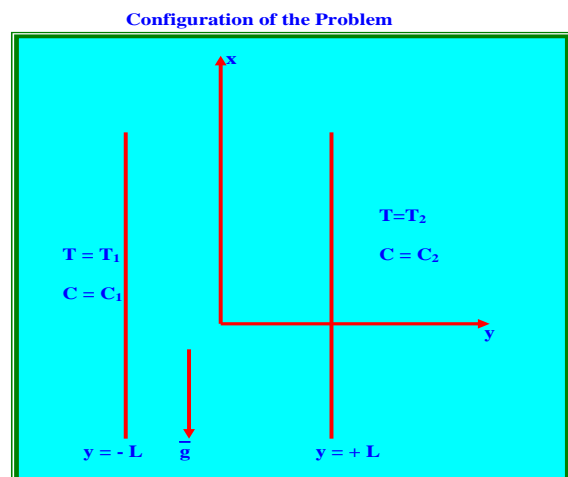
Also in all the above studies the thermal diffusion effect (known as Soret effect) has been neglected. This assumption is true when the concentration level is very low. Therefore, so ever, exceptions. The thermal diffusion effects for instance, has been utilized for isotropic separation and in mixtures between gases with very light molecular weight (H_2, He) and the medium molecular weight (N_2, air) the diffusion – thermo effects was found to be of a magnitude just it can not be neglected. In view of the importance of this diffusion – thermo effect, recently Jha and singh [7] studied the free convection and mass transfer flow in an infinite vertical plate moving impulsively in its own plane taking into account the Soret effect. Kafousias [8] studied the MHD free convection and mass transfer flow taking into account Soret effect. The analytical studies of Jha and singh and Kafousias [7, 8] were based on Laplace transform technique. Abdul Sattar and Alam [1] have considered an unsteady convection and mass transfer flow of viscous incompressible and electrically conducting fluid past a moving infinite vertical porous plate taking into the thermal diffusion effects. Similarity equations of the momentum energy and concentration equations are derived by introducing a time dependent length scale. Malsetty et al [12] have studied the effect of both the soret coefficient and Dufour coefficient on the double diffusive convective with compensating horizontal thermal and solutal gradients.

Recently Bharathi[3] has studied thermo-diffusion effect on unsteady convective Heat and Mass transfer flow of a viscous fluid through a porous medium in vertical channel. Taneja et al [18] studied the effects of magnetic field on free convective flow through porous medium with radiation and variable permeability in the slip flow regime. Kumar et al [10] studied the effect of MHD free convection flow of viscous fluid past a porous vertical plate through non homogeneous porous medium with radiations and temperature gradient dependent heat source in slip flow regime. The effect of free convection flow with thermal radiation and mass transfer past a moving vertical porous plate was studied by Makinde [11]. Ayani et al [1] studied the effect of radiation on the laminar natural convection induced by a line source. Raphil[17] have discussed the effect of radiation and free convection flow through porous medium. MHD oscillating flow on free convection radiation through porous medium with constant suction velocity was investigated by El.Hakim[6]

Keeping the above application in view we made attempt in this chapter to study thermo-diffusion and dissipation effect on non-Darcy convective heat and Mass transfer flow of a viscous fluid through a porous medium in a vertical channel with Radiation and heat sources. The governing equations flow, heat and mass transfer are solved by using regular perturbation method with δ , the porosity parameter as a perturbation parameter. The velocity, temperature, concentration, shear stress and rate of Heat and Mass transfer are evaluated numerically for different variations of parameter

2. FORMULATION OF THE PROBLEM

We consider a fully developed laminar convective heat and mass transfer flow of a viscous fluid through a porous medium confined in a vertical channel bounded by flat walls. We choose a Cartesian co-ordinate system $O(x,y,z)$ with x- axis in the vertical direction and y-axis normal to the walls. The walls are taken at $y = \pm L$. The walls are maintained at constant temperature and concentration. The temperature gradient in the flow field is sufficient to cause natural convection in the flow field. A constant axial pressure gradient is also imposed so that this resultant flow is a mixed convection flow. The porous medium is assumed to be isotropic and homogeneous with constant porosity and effective thermal diffusivity. The thermo physical properties of porous matrix are also assumed to be constant and Boussinesq approximation is invoked by confining the density variation to the buoyancy term. In the absence of any extraneous force flow is unidirectional along the x-axis which is assumed to be infinite.



The Brinkman-Forchheimer-extended Darcy equation which account for boundary inertia effects in the momentum equation is used to obtain the velocity field. Based on the above assumptions the governing equations in the vector form are

$$\nabla \cdot \bar{q} = 0 \quad (\text{Equation of continuity}) \quad (1)$$

$$\frac{\rho}{\delta} \frac{\partial \bar{q}}{\partial t} + \frac{\rho}{\delta^2} (\bar{q} \cdot \nabla) \bar{q} = -\nabla p + \rho g - \left(\frac{\mu}{k}\right) \bar{q} - \frac{\rho F}{\sqrt{k}} \bar{q} \cdot \bar{q} + \mu \nabla^2 \bar{q} \quad (\text{Equation of linear momentum}) \quad (2)$$

$$\rho C_p \left(\frac{\partial T}{\partial t} + (\bar{q} \cdot \nabla) T \right) = \lambda \nabla^2 T + Q(T_o - T) \quad (\text{Equation of energy}) \quad (3)$$

$$\frac{\partial C}{\partial t} + (\bar{q} \cdot \nabla) C = D_1 \nabla^2 C - KC + k_{11} \nabla^2 T \quad (\text{Equation of diffusion}) \quad (4)$$

$$\rho - \rho_0 = -\beta \rho_0 (T - T_o) - \beta^* \rho_0 (C - C_o) \quad (\text{Equation of State}) \quad (5)$$

where $\bar{q} = (u, 0, 0)$ is the velocity, T, C are the temperature and Concentration, p is the pressure, ρ is the density of the fluid, C_p is the specific heat at constant pressure, μ is the coefficient of viscosity, k is the permeability of the porous medium, δ is the porosity of the medium, β is the coefficient of thermal expansion, λ is the coefficient of thermal conductivity, F is a function that depends on the Reynolds number and the microstructure of porous medium, β^* is the volumetric coefficient of expansion with mass fraction concentration, k is the chemical reaction coefficient and D_1 is the chemical molecular diffusivity, k_{11} is the cross diffusivity and Q is the strength of the heat generating source. Here, the thermophysical properties of the solid and fluid have been assumed to be constant except for the density variation in the body force term (Boussinesq approximation) and the solid particles and the fluid are considered to be in the thermal equilibrium.

Since the flow is unidirectional, the continuity of equation (1) reduces to

$$\frac{\partial u}{\partial x} = 0 \quad \text{where } u \text{ is the axial velocity implies } u = u(y)$$

The momentum, energy and diffusion equations in the scalar form reduces to

$$-\frac{\partial p}{\partial x} + \left(\frac{\mu}{\delta}\right) \frac{\partial^2 u}{\partial y^2} - \left(\frac{\mu}{k}\right) u - \frac{\rho \delta F}{\sqrt{k}} u^2 - \rho g = 0 \quad (6)$$

$$\rho_0 C_p u \frac{\partial T}{\partial x} = \lambda \frac{\partial^2 T}{\partial y^2} + Q(T_o - T) \quad (7)$$

$$u \frac{\partial C}{\partial x} = D_1 \frac{\partial^2 C}{\partial y^2} - k_1 C + k_{11} \frac{\partial^2 T}{\partial y^2} \quad (8)$$

The boundary conditions are

$$\begin{aligned} u = 0, \quad T = T_1, \quad C = C_1 \quad \text{on } y = -L \\ u = 0, \quad T = T_2, \quad C = C_2 \quad \text{on } y = +L \end{aligned} \quad (9)$$

The axial temperature and concentration gradients $\frac{\partial T}{\partial x}$ & $\frac{\partial C}{\partial x}$ are assumed to be constant, say, A & B respectively.

We define the following non-dimensional variables as

$$u' = \frac{u}{(v/L)}, \quad (x', y') = (x, y)/L, \quad p' = \frac{p\delta}{(\rho v^2/L^2)}, \quad \theta = \frac{T - T_2}{T_1 - T_2}, \quad C' = \frac{C - C_2}{C_1 - C_2} \quad (10)$$

Introducing these non-dimensional variables the governing equations in the dimensionless form reduce to (on dropping the dashes)

$$\frac{d^2 u}{dy^2} = \pi + \delta(D^{-1})u - \delta G(\theta + NC) - \delta^2 \Delta u^2 \quad (11)$$

$$\frac{d^2 \theta}{dy^2} - \alpha \theta = (PN_T)u \quad (12)$$

$$\frac{d^2 C}{dy^2} - \gamma C = (Sc N_c)u + \frac{ScSo}{N} \frac{d^2 \theta}{dy^2} \quad (13)$$

where

$$\Delta = FD^{-1/2} \text{ (Inertia or Fochhemeir parameter)} \quad G = \frac{\beta g(T_1 - T_2)L^3}{\nu^2} \text{ (Grashof Number)}$$

$$D^{-1} = \frac{L^2}{k} \text{ (Darcy parameter)}, \quad Sc = \frac{\nu}{D_1} \text{ (Schmidt number)}, \quad S_o = \frac{k_{11}\beta^*}{\nu\beta} \text{ (Soret parameter)}$$

$$N = \frac{\beta^*(C_1 - C_2)}{\beta(T_1 - T_2)} \text{ (Buoyancy ratio)}, \quad P = \frac{\mu C_p}{\lambda} \text{ (Prandtl Number)}$$

$$\alpha = \frac{QL^2}{\lambda} \text{ (Heat source parameter)}, \quad \gamma = \frac{k_1 L^2}{D_1} \text{ (Chemical reaction parameter)}$$

$$N_T = \frac{AL}{(T_1 - T_2)} \text{ (Non-dimensional temperature gradient)}$$

$$N_c = \frac{BL}{(C_1 - C_2)} \text{ (Non-dimensional concentration gradient)}$$

The corresponding boundary conditions are

$$\begin{aligned} u = 0, \quad \theta = 1, \quad C = 1 \quad \text{on } y = -1 \\ u = 0, \quad \theta = 0, \quad C = 0 \quad \text{on } y = +1 \end{aligned} \quad (14)$$

3. SOLUTION OF THE PROBLEM

The governing equations of flow, heat and mass transfer are coupled non-linear differential equations. Assuming the porosity δ to be small we write

$$u = u_0 + \delta u_1 + \delta^2 u_2 + \dots, \quad \theta = \theta_0 + \delta \theta_1 + \delta^2 \theta_2 + \dots, \quad C = C_0 + \delta C_1 + \delta^2 C_2 + \dots \quad (15)$$

Substituting the above expansions in the equations (11)-(13) and equating like powers of δ , we obtain equations to the zeroth order as

$$\frac{d^2 u_0}{dy^2} = \pi \quad (16)$$

$$\frac{d^2 \theta_0}{dy^2} - \alpha \theta_0 = (PN_T)u_0 \quad (17)$$

$$\frac{d^2 C_0}{dy^2} - \gamma C_0 = (ScN_c)u_0 \quad (18)$$

The equations to the first order are

$$\frac{d^2 u_1}{dy^2} - (D^{-1})u_1 = -G(\theta_0 + NC_0) \quad (19)$$

$$\frac{d^2\theta_1}{dy^2} - \alpha\theta_1 = (PN_T)u_1 \quad (20)$$

$$\frac{d^2C_1}{dy^2} - \gamma C_1 = (ScN_C)u_1 \quad (21)$$

The equations to the second order are

$$\frac{d^2u_2}{dy^2} - (D^{-1})u_2 = -G(\theta_1 + NC_1) - \Delta u_0^2 \quad (22)$$

$$\frac{d^2\theta_2}{dy^2} - \alpha\theta_2 = (PN_T)u_2 \quad (23)$$

$$\frac{d^2C_2}{dy^2} - \gamma C_2 = (ScN_C)u_2 \quad (24)$$

The corresponding conditions are

$$u_0(1) = u_0(-1) = 0, \theta_0(+1) = 0, \theta_0(-1) = 1, C_0(+1) = 0, C_0(-1) = 1 \quad (25)$$

$$u_1(1) = u_1(-1) = 0, \theta_1(+1) = 0, \theta_1(-1) = 0, C_1(+1) = 0, C_1(-1) = 0 \quad (26)$$

$$u_2(1) = u_2(-1) = 0, \theta_2(+1) = 0, \theta_2(-1) = 0, C_2(+1) = 0, C_2(-1) = 0 \quad (27)$$

Solving the equations (16)-(18) & (22)-(24) subject to the boundary conditions (25)-(27) we get

$$u_0(y) = \frac{\pi}{2}(y^2 - 1)$$

$$\theta_0 = a_2 \left(1 - \frac{Ch(\beta_1 y)}{Ch(\beta_1)} \right) - a_1(1 - y^2) + 0.5 \left(\frac{Ch(\beta_1 y)}{Ch(\beta_1)} - \frac{Sh(\beta_1 y)}{Sh(\beta_1)} \right)$$

$$C_0 = a_7 \left(1 - \frac{Ch(\beta_1 y)}{Ch(\beta_1)} \right) + a_5 (Ch(\beta_2 y) - Ch(\beta_2)) + 0.5 \left(\frac{Ch(\beta_1 y)}{Ch(\beta_1)} - \frac{Sh(\beta_1 y)}{Sh(\beta_1)} \right) + a_6 (Sh(\beta_2 y) - Sh(\beta_2)) \frac{Sh(\beta_1 y)}{Sh(\beta_1)}$$

$$u_1 = a_{17} \left(\frac{Ch(M_1 y)}{Ch(M_1)} Ch(\beta_2) - Ch(\beta_2 y) \right) - a_{19} \left(\frac{Ch(M_1 y)}{Ch(M_1)} Ch(\beta_1) - Ch(\beta_1 y) \right)$$

$$+ a_{21} \left(\frac{Ch(M_1 y)}{Ch(M_1)} - y^2 \right) - a_{18} \left(Sh(\beta_2 y) - \frac{Sh(M_1 y)}{Sh(M_1)} Sh(\beta_2) \right) - a_{20} \left(Sh(\beta_1 y) - \frac{Sh(M_1 y)}{Sh(M_1)} Sh(\beta_1) \right)$$

$$\theta_1 = a_{41} \left(Ch(M_1 y) - Ch(M_1) \frac{Ch(\beta_2 y)}{Ch(\beta_2)} \right) + a_{42} \left(\frac{Sh(M_1 y) - Sh(M_1) \frac{Sh(\beta_2 y)}{Sh(\beta_2)}}{+ a_{43} (y Ch(\beta_2 y) - Ch(\beta_2)) \frac{Sh(\beta_2 y)}{Sh(\beta_2)}} \right)$$

$$+ a_{44} \left(y Sh(\beta_2 y) - Sh(\beta_2) \frac{Ch(\beta_2 y)}{Ch(\beta_2)} \right) + a_{45} \left(Ch(\beta_1 y) - Ch(\beta_1) \frac{Ch(\beta_2 y)}{Ch(\beta_2)} \right)$$

$$+ a_{46} \left(Sh(\beta_1 y) - Sh(\beta_1) \frac{Sh(\beta_2 y)}{Sh(\beta_2)} \right) + a_{47} \left(y^2 - \frac{Ch(\beta_2 y)}{Ch(\beta_2)} \right) + a_{48} \left(1 - \frac{Ch(\beta_2 y)}{Ch(\beta_2)} \right)$$

$$\begin{aligned}
 C_1 = & a_{25} \left(Ch(M_1 y) - Ch(M_1) \frac{Ch(\beta_1 y)}{Ch(\beta_1)} \right) + a_{26} \left(Sh(M_1 y) - Sh(M_1) \frac{Sh(\beta_1 y)}{Sh(\beta_1)} \right) \\
 & - a_{27} \left(Ch(\beta_2 y) - Ch(\beta_2) \frac{Ch(\beta_1 y)}{Ch(\beta_1)} \right) - a_{28} \left(Sh(\beta_2 y) - Sh(\beta_2) \frac{Sh(\beta_1 y)}{Sh(\beta_1)} \right) + \left(y Sh(\beta_1 y) - Sh(\beta_1) \frac{Ch(\beta_1 y)}{Ch(\beta_1)} \right) \\
 & - a_{30} \left(y Ch(\beta_1 y) - Ch(\beta_1) \frac{Sh(\beta_1 y)}{Sh(\beta_1)} \right) + a_{31} \left(y^2 - \frac{Ch(\beta_1 y)}{Ch(\beta_1)} \right) + a_{32} \left(1 - \frac{Ch(\beta_1 y)}{Ch(\beta_1)} \right) \\
 u_2 = & -a_{62} \left(\frac{Ch(M_1 y)}{Ch(M_1)} Ch(\beta_1) - Ch(\beta_1 y) \right) - a_{63} \left(\frac{Sh(M_1 y)}{Sh(M_1)} Sh(\beta_1) - Sh(\beta_1 y) \right) \\
 & - a_{64} \left(\frac{Ch(M_1 y)}{Ch(M_1)} Sh(\beta_2) - Ch(\beta_2 y) \right) + a_{72} \left(\frac{Ch(M_1 y)}{Ch(M_1)} - y^4 \right) - a_{73} \left(\frac{Ch(M_1 y)}{Ch(M_1)} - y^2 \right) \\
 & - a_{70} \left(\frac{Ch(M_1 y)}{Ch(M_1)} - 1 \right) - a_{65} \left(\frac{Sh(M_1 y)}{Sh(M_1)} Sh(\beta_2) - Sh(\beta_2 y) \right) + a_{66} \left(\frac{Ch(M_1 y)}{Ch(M_1)} Sh(M_1) - y Sh(M_1 y) \right) \\
 & + a_{67} \left(\frac{Sh(M_1 y)}{Sh(M_1)} Ch(M_1) - y Ch(M_1 y) \right) + a_{68} \left(\frac{Sh(M_1 y)}{Sh(M_1)} Ch(\beta_2) - y Ch(\beta_2 y) \right) \\
 & + a_{69} \left(\frac{Ch(M_1 y)}{Ch(M_1)} Sh(\beta_2) - y Sh(\beta_2 y) \right) \\
 C_2 = & a_{77} \left(Ch(M_1 y) - Ch(M_1) \frac{Ch(\beta_1 y)}{Ch(\beta_1)} \right) + a_{78} \left(Sh(M_1 y) - Sh(M_{12}) \frac{Sh(\beta_1 y)}{Sh(\beta_1)} \right) \\
 & + a_{79} \left(y Ch(\beta_1 y) - Ch(\beta_1) \frac{Sh(\beta_2 y)}{Sh(\beta_2)} \right) + a_{80} (y^2 - 1) Ch(\beta_1 y) + a_{79} (y^4 - 1) + a_{81} (y^2 - 1) \\
 & + a_{80} \left(y Sh(\beta_1 y) - \frac{Ch(\beta_1 y)}{Ch(\beta_1)} Sh(\beta_1) \right) + a_{81} \left(Ch(\beta_2 y) - \frac{Ch(\beta_1 y)}{Ch(\beta_1)} Ch(\beta_2) \right) + a_{82} \left(Sh(\beta_2 y) - \frac{Sh(\beta_1 y)}{Sh(\beta_1)} Sh(\beta_2) \right) \\
 & - a_{83} \left(y Ch(M_1 y) - Ch(M_1) \frac{Sh(\beta_1 y)}{Sh(\beta_1)} \right) - a_{84} \left(y Sh(M_1 y) - Sh(M_1) \frac{Ch(\beta_1 y)}{Ch(\beta_1)} \right) \\
 & - a_{85} \left(y Ch(\beta_2 y) - Ch(\beta_2) \frac{Sh(\beta_1 y)}{Sh(\beta_1)} \right) - a_{86} \left(y Sh(\beta_2 y) - Sh(\beta_2) \frac{Ch(\beta_1 y)}{Ch(\beta_1)} \right) \\
 & - a_{87} (y^2 - 1) Ch(\beta_1 y) - a_{88} (y^2 - 1) S(\beta_1 y) - a_{89} \left(y^4 - \frac{Ch(\beta_1 y)}{Ch(\beta_1)} \right) + a_{90} \left(y^2 - \frac{Ch(\beta_1 y)}{Ch(\beta_1)} \right) + a_{91} \left(1 - \frac{Ch(\beta_1 y)}{Ch(\beta_1)} \right) \\
 \theta_2 = & b_{18} \left(Ch(\beta_1 y) - Ch(\beta_1) \frac{Ch(\beta_2 y)}{Ch(\beta_2)} \right) + b_{18} \left(Sh(\beta_1 y) - Sh(\beta_1) \frac{Sh(\beta_2 y)}{Sh(\beta_2)} \right) \\
 & + b_{20} \left(y Sh(\beta_2 y) - Sh(\beta_2) \frac{Ch(\beta_2 y)}{Ch(\beta_2)} \right) + b_{21} \left(y Ch(\beta_2 y) - Ch(\beta_2) \frac{Sh(\beta_2 y)}{Sh(\beta_2)} \right) \\
 & + b_{22} \left(Ch(M_1 y) - Ch(M_1) \frac{Ch(\beta_2 y)}{Ch(\beta_2)} \right) + b_{23} \left(Sh(M_1 y) - Sh(M_1) \frac{Sh(\beta_2 y)}{Sh(\beta_2)} \right) \\
 & + b_{24} \left(y Ch(M_1 y) - Ch(M_1) \frac{Sh(\beta_2 y)}{Sh(\beta_2)} \right) + b_{25} \left(y Sh(M_1 y) - Sh(M_1) \frac{Ch(\beta_2 y)}{Ch(\beta_2)} \right)
 \end{aligned}$$

$$\begin{aligned}
 &+b_{26} \left(yCh(\beta_1 y) - \frac{Sh(\beta_2 y)}{Sh(\beta_2)} Ch(\beta_1) \right) + b_{27} \left(ySh(\beta_1 y) - \frac{Ch(\beta_2 y)}{Ch(\beta_2)} Sh(\beta_1) \right) \\
 &+b_{28} \left(y^2 Ch(\beta_1 y) - \frac{Ch(\beta_2 y)}{Ch(\beta_2)} Ch(\beta_1) \right) + b_{29} \left(y^2 Sh(\beta_1 y) - \frac{Sh(\beta_2 y)}{Sh(\beta_2)} Ch(\beta_1) \right) \\
 &+b_{30} (y^2 - 1)Sh(\beta_2 y) + b_{31} (y^2 - 1)Ch(\beta_2 y) + b_{32} \left(y^4 - \frac{Ch(\beta_2 y)}{Ch(\beta_2)} \right) \\
 &+b_{33} \left(y^2 - \frac{Ch(\beta_2 y)}{Ch(\beta_2)} \right) + b_{34} \left(1 - \frac{Ch(\beta_2 y)}{Ch(\beta_2)} \right)
 \end{aligned}$$

where $a_1, a_2, a_3, \dots, a_{91}$ are constants.

4. NUSSELT NUMBER and SHERWOOD NUMBER

The rate of heat transfer (Nusselt Number) is given by

$$\begin{aligned}
 Nu_{y=\pm 1} &= \left(\frac{d\theta}{dy} \right)_{y=\pm 1} \text{ and corresponding expressions are} \\
 Nu_{y=+1} &= b_{38} + \delta b_{40} + \delta^2 b_{42}, \quad Nu_{y=-1} = b_{39} + \delta b_{41} + \delta^2 b_{43}
 \end{aligned}$$

The rate of mass transfer (Sherwood Number) is given by

$$\begin{aligned}
 Sh_{y=\pm 1} &= \left(\frac{dC}{dy} \right)_{y=\pm 1} \text{ and corresponding expressions are} \\
 Sh_{y=+1} &= b_{44} + \delta b_{46} + \delta^2 b_{48}, \quad Sh_{y=-1} = b_{45} + \delta b_{47} + \delta^2 b_{49}
 \end{aligned}$$

Where b_1, b_2, \dots, b_{49} are constants.

5. DISCUSSION OF RESULTS

In this analysis we investigate the effect of chemical reaction and thermo In this analysis, we investigate the combined effect of radiation and sorret effect on non -Darcy convective heat and mass transfer of a viscous electrically conducting fluid through a porous medium in a vertical channel in the presence of temperature dependent heat source . The equations governing flow, heat and mass transfer are solved by using a perturbation technique with δ , the porous parameter as a perturbation parameter.

The axial velocity u is shown in figs. 1-5 for different values of $D^{-1}, \alpha, Sc, S_0, k, N$. The variation of u with D^{-1} and α shows that lesser the permeability of the porous medium smaller u in the flow region. Also it enhances with increase in the strength of the heat generating source (fig-1). Fig-2 represents the variation of u with chemical reaction parameter k . It is observed that for smaller values of $k \leq 1.5$; u is positive and higher $k \geq 2.5$ it is negative in the flow region except in a narrow regions adjacent to the boundaries $y = \pm 1$. The variation of u with buoyancy ratio N shows that when the molecular buoyancy force dominates over the thermal buoyancy force the axial flow enhances in the entire flow region irrespective of the directions of buoyancy forces (fig-3). The variation of u with Schmidt Number Sc shows that lesser the molecular diffusivity smaller in the flow region (fig.4). The effect of thermo- diffusion on u is shown in fig-5. It is found that u depreciates with increase in $S_0 > 0$ and enhances with $|S_0|$.

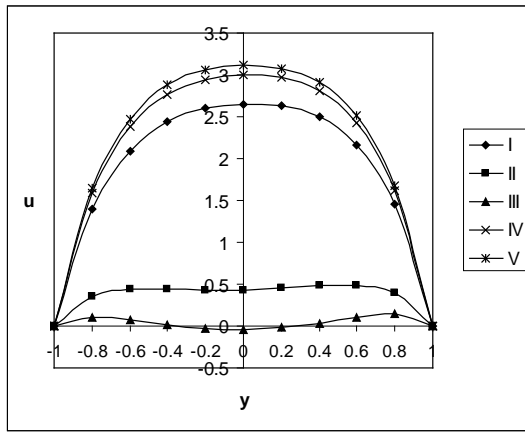


Fig. 1 : Variation of u with D^{-1}, α

	I	II	III	IV	V
D^{-1}	10^2	3×10^2	5×10^2	10^2	10^2
α	2	2	2	4	6

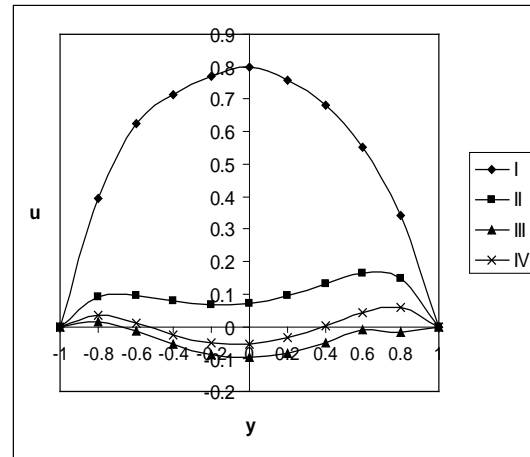


Fig. 2 : Variation of u with k

	I	II	III	IV
k	0.5	1.5	2.5	3.5

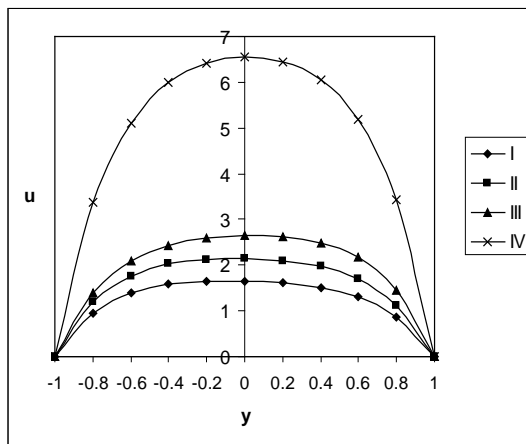


Fig. 3 : Variation of u with N

	I	II	III	IV
N	-0.5	-0.8	1	2

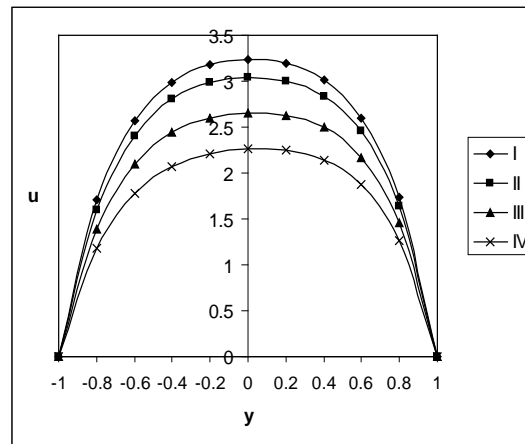


Fig. 4 : Variation of u with Sc

	I	II	III	IV
Sc	0.24	0.6	1.30	2.01

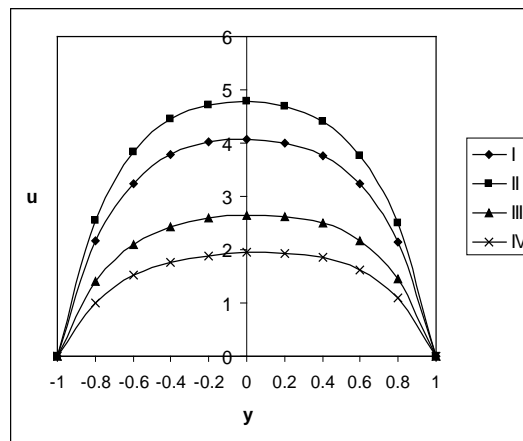


Fig. 5 : Variation of u with S_0

	I	II	III	IV
S_0	-0.5	-1	0.5	1

Figs. 6-10 represent the variation of the Non-dimensional temperature θ with different parametric values. The variation of θ with D^{-1} and α shows that lesser the permeability of the porous medium/higher the strength of the heat sources smaller the actual temperature in the entire flow region (fig.6). The variation of θ with chemical reaction parameter k is shown in fig-7. It is found that an increase in k results in a depreciation in actual temperature. The variation of θ with buoyancy ratio N shows that the actual temperature enhances with $|N|$ irrespective of the directions of the buoyancy forces (fig-8). From fig.9 we notice a marginal increment in the actual temperature with increase in Sc. The effect of thermo-diffusion on θ is shown in fig.10. It is found that the actual temperature reduces with increase in $S_0 > 0$ and enhances with $|S_0|$.

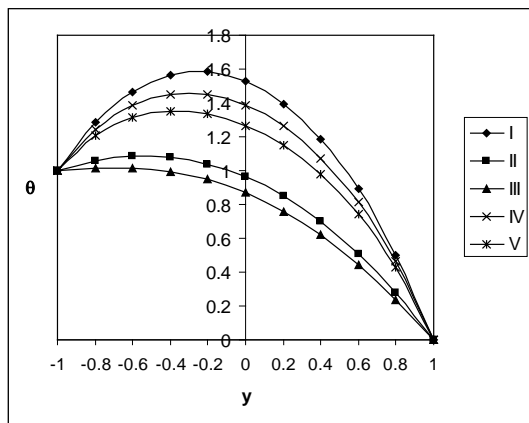


Fig 6 : Variation of θ with D^{-1} , α

I	II	III	IV	V
D^{-1}	10^2	3×10^2	5×10^2	10^2
α	2	2	2	4
				6

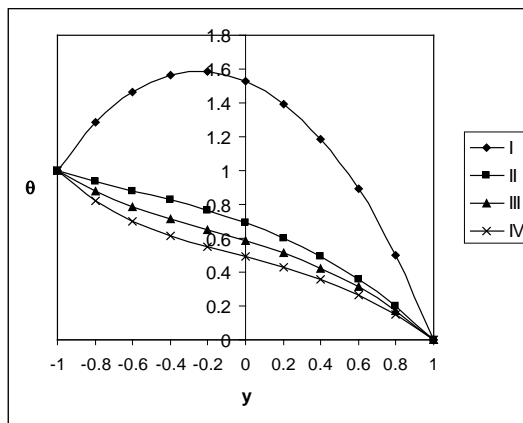


Fig. 7 : Variation of θ with k

I	II	III	IV
k	0.5	1.5	2.5
			3.5

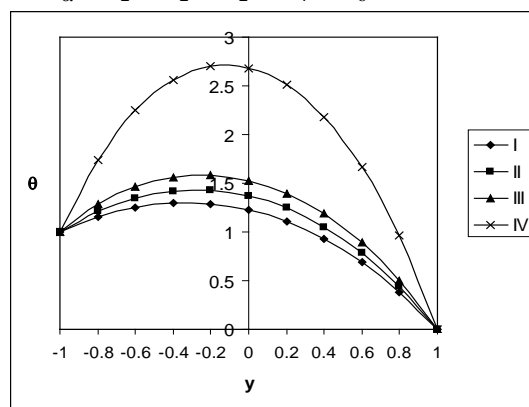


Fig 8 : Variation of θ with N

I	II	III	IV
N	-0.5	-0.8	1
			2

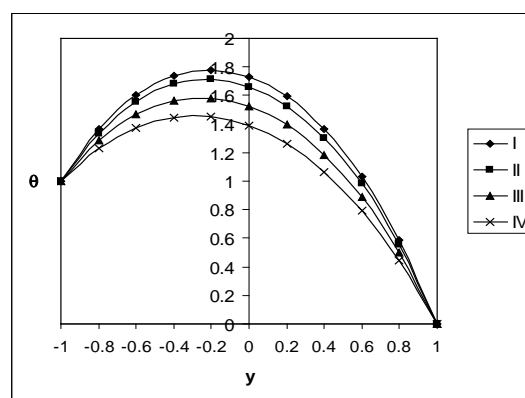


Fig. 9 : Variation of θ with Sc

I	II	III	IV
Sc	0.24	0.6	1.30
			2.01

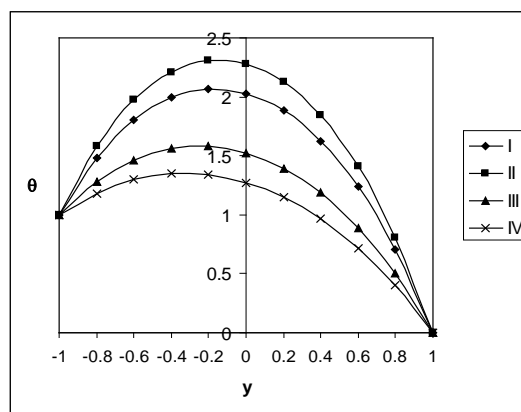


Fig. 10 : Variation of θ with S_0

I	II	III	IV
S_0	-0.5	-1	0.5
			1

The Non-dimensional concentration C is shown in figs. 11-15 for different parametric values. The variation of C with D^{-1} and α shows that lesser the molecular diffusivity larger the actual temperature in the left half and smaller in the right half and for further lowering of the permeability it depreciates in the left half and enhances in the right half, while an increase in the heat source α reduces the actual concentration in the left half and enhances in the right half (fig.11). The variation of C with chemical reaction parameter k shows that an increase in $k \leq 1.5$ the actual concentration enhances in the left half and reduces in the right half and for higher $k \geq 2.5$ it enhances in the entire flow region and for still higher $k = 3.5$ it depreciates in the flow region (fig-12). The variation of C with buoyancy ratio N shows that when the molecular buoyancy force dominates over the thermal buoyancy force, the actual concentration reduces in the left half and enhances in the right half irrespective of the directions of the buoyancy forces (fig.13). From fig.14 we notice that lesser the molecular diffusivity smaller the actual concentration in the left half and larger in the right half. An increase in $S_0 > 0$ reduces the actual concentration in the left half and enhances in the right half, while it enhances in the left half and reduces in the right half with increase in $|S_0|$. (fig.15).

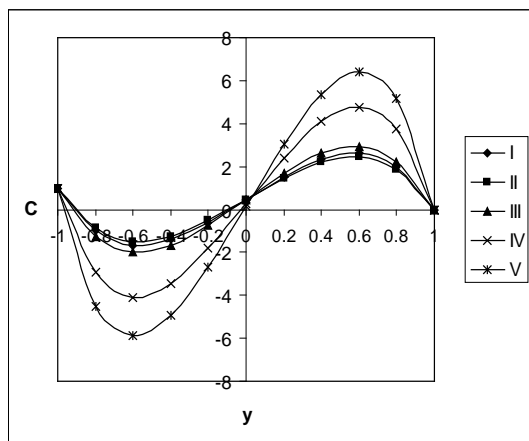


Fig 11 : Variation of C with D^{-1} , α

	I	II	III	IV	V
D^{-1}	10^2	3×10^2	5×10^2	10^2	10^2
α	2	2	2	4	6

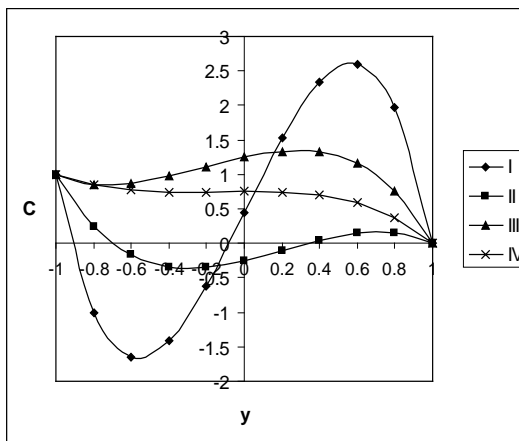


Fig 12 : Variation of C with k

	I	II	III	IV
k	0.5	1.5	2.5	3.5

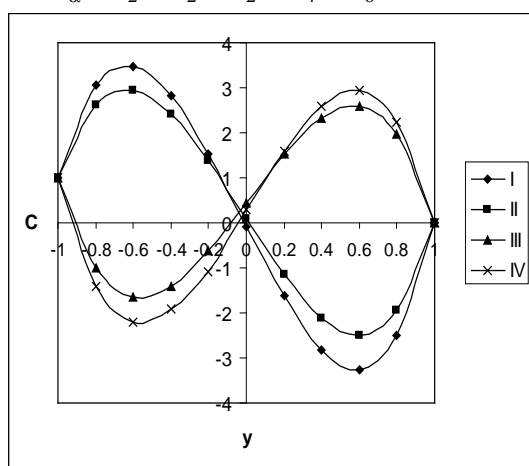


Fig 13 : Variation of C with N

	I	II	III	IV
N	-0.5	-0.8	1	2

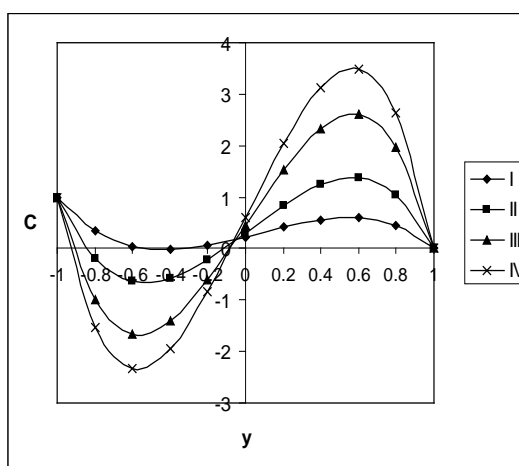


Fig 14 : Variation of C with Sc

	I	II	III	IV
Sc	0.24	0.6	1.3	2.01

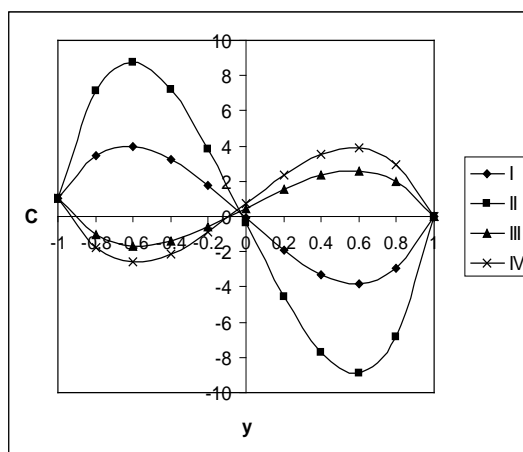


Fig. 15 : Variation of C with S_0

	I	II	III	IV
S_0	-0.5	-1	0.5	1

The Nusselt number which measures the rate of heat transfer at $y = \pm 1$ is shown in tables 1-6 for different parametric values. It is found that the rate of heat transfer enhances with increase in $|G|$ and reduces with D^{-1} and α at both the walls (tables 1 & 4). From tables 2 & 5 we notice that the rate of heat transfer depreciates with k at $y = +1$ and at $y = -1$ it depreciates with $k \leq 1.5$ and enhances with higher $k \geq 2.5$. The rate of heat transfer experiences with N irrespective of the directions of the buoyancy forces at both the walls. Also lesser the molecular diffusivity $|Nu|$ at $y = \pm 1$. Also $|Nu|$ depreciates with $S_0 > 0$ and enhances with $|S_0|$ and enhances with $|S_0|$ at $y = \pm 1$ (tables 3 & 6)

Table 1
Nusselt number (Nu) at y = +1

G	I	II	III	IV	V
1×10^2	-2.82953	-1.50236	-1.27664	-2.68265	-2.50902
2×10^2	-8.38162	-2.81850	-1.82841	-7.57544	-6.77935
-1×10^2	-3.36044	-1.77884	-1.46590	-2.99489	-2.71971
-2×10^2	-9.44343	-3.37147	-2.20692	-8.19990	-7.20073
D^{-1}	10^2	2×10^2	3×10^2	10^2	10^2
α	2	2	2	4	6

Table 2
Nusselt number (Nu) at y = +1

G	I	II	III	IV	V	VI	VII
1×10^2	-2.82953	-1.08345	-0.97586	-0.84914	-2.13027	-2.45913	-5.52003
2×10^2	-8.38162	-8.8368	-1.90093	-1.76810	-5.65782	-7.00467	-19.06371
-1×10^2	-3.36044	-1.20986	-0.90899	-0.80898	-2.73443	-3.09471	-5.97103
-2×10^2	-9.44343	-2.22548	-1.76720	-1.68777	-6.86614	-8.27585	-19.96570
k	0.5	1.5	2.5	3.5	0.5	0.5	0.5
N	1	1	1	1	-0.5	-0.8	2

Table 3
Nusselt number (Nu) at y = +1

G	I	II	III	IV	V	VI	VII
1×10^2	-3.32008	-3.15348	-2.82953	-2.50096	-4.03275	-4.63436	-2.22792
2×10^2	-10.19160	-9.57689	-8.38162	-7.16928	-12.82119	-15.04098	-6.16183
-1×10^2	-3.69879	-3.58388	-3.36044	-3.13381	-4.19035	-4.60531	-2.94548
-2×10^2	-10.94902	-10.43769	-9.44343	-8.43497	-13.13639	-14.98287	-7.59695
Sc	0.24	0.6	1.3	2.01	1.3	1.3	1.3
S_0	0.5	0.5	0.5	0.5	-0.5	-1	1

Table 4
Nusselt number (Nu) at y = -1

G	I	II	III	IV	V
1×10^2	1.68912	0.35552	0.12650	1.53242	1.35543
2×10^2	7.26215	1.68619	0.68949	6.43633	5.63354
-1×10^2	2.17813	0.60295	0.29331	1.82240	1.55057
-2×10^2	8.24017	2.18105	1.02311	7.01628	6.02381
D^{-1}	10^2	2×10^2	3×10^2	10^2	10^2
α	2	2	2	4	6

Table 5
Nusselt number (Nu) at y = -1

G	I	II	III	IV	V	VI	VII
1×10^2	1.68912	-0.35204	-0.74386	-1.10321	0.94005	1.27573	4.38174
2×10^2	7.26215	0.55788	0.18241	-0.17489	4.43875	5.79924	17.94850
-1×10^2	2.17813	-0.26707	-0.81311	-1.16210	1.60192	1.95539	4.78659
-2×10^2	8.24017	0.72782	0.04390	-0.29267	5.76249	7.158556	18.75819
k	0.5	1.5	2.5	3.5	0.5	0.5	0.5
N	1	1	1	1	-0.5	-0.8	2

Table 6
Nusselt number (Nu) at y = -1

G	I	II	III	IV	V	VI	VII
1×10^2	2.16938	2.00627	1.68912	1.36743	2.86712	3.45612	1.10012
2×10^2	9.05157	8.44385	7.26215	6.06358	11.65129	13.84587	5.06750
-1×10^2	2.52676	2.40835	2.17813	1.94461	3.03326	3.46082	1.75056
-2×10^2	9.76632	9.24801	8.24017	7.21794	11.98356	13.85526	6.36848
Sc	0.24	0.6	1.3	2.01	1.3	1.3	1.3
S_0	0.5	0.5	0.5	0.5	-0.5	-1	1

The Sherwood number (Sh) which measures the rate of mass transfer with different parametric values is shown in tables.7-12. It is found that the rate of mass transfer enhances with increase in |G| or α at $y = \pm 1$. The variation of Sh with D^{-1} shows that lesser the permeability of porous medium smaller |Sh| and for further lowering of permeability larger |Sh| at $y = \pm 1$ (tables 7 & 10). An increase in the chemical reaction parameter k enhances Sh for all G at $y = +1$ while at $y = -1$ it depreciates with $k \leq 2.5$ and enhances with higher $k \geq 3.5$. The rate of mass transfer enhances with increase in the buoyancy ratio N and depreciates |Sh| at $y = \pm 1$ (tables 8 & 11). From Tables 9 & 12 we find that the rate of mass transfer enhances at $y = \pm 1$ with increase in Sc. Also |Sh| experiences an enhancement with increase in $|S_0|$ at both the walls.

Table 7
Sherwood number (Sh) at $y = +1$

G	I	II	III	IV	V
1×10^2	-13.66442	-12.75362	-15.45016	-27.62905	-39.48521
2×10^2	-54.21877	-50.44022	-61.23803	-65.1254	-79.0956
-1×10^2	-14.04267	-12.99654	-15.70471	-28.46951	-40.76753
-2×10^2	-54.97527	-50.92607	-61.74714	-66.1209	-80.1256
D^{-1}	10^2	2×10^2	3×10^2	10^2	10^2
α	2	2	2	4	6

Table 8
Sherwood number (Sh) at $y = +1$

G	I	II	III	IV	V	VI	VII
1×10^2	-13.66442	-4.35165	-2.33663	-1.13952	17.5951	13.58951	-15.95853
2×10^2	-54.21877	-8.01491	-7.80968	-5.14211	70.21468	55.59991	-63.84138
-1×10^2	-14.04267	-0.63777	-0.61882	-0.11269	18.59697	14.72046	-16.62602
-2×10^2	-54.97527	-6.58714	-5.37406	-5.24652	72.91384	57.86182	-65.17636
k	0.5	1.5	2.5	3.5	0.5	0.5	0.5
N	1	1	1	1	-0.5	-0.8	2

Table 9
Sherwood number (Sh) at $y = +1$

G	I	II	III	IV	V	VI	VII
1×10^2	-3.02025	-7.16231	-13.66442	-18.16560	20.81835	48.66371	-20.30183
2×10^2	-11.93973	-28.41439	-54.21877	-71.98674	83.10132	194.32800	-80.31210
-1×10^2	-3.44022	-7.57561	-14.04267	-18.47853	20.45685	48.46138	-20.53767
-2×10^2	-12.77967	-29.24098	-54.97527	-72.61261	82.37832	193.92340	-80.78378
Sc	0.24	0.6	1.3	2.01	1.3	1.3	1.3
S_0	0.5	0.5	0.5	0.5	-0.5	-1	1

Table 10
Sherwood number (Sh) at $y = -1$

G	I	II	III	IV	V
1×10^2	-14.29768	-13.33169	-16.02035	-29.12505	-41.75275
2×10^2	-54.91245	-51.02355	-61.80558	-65.1254	-79.0956
-1×10^2	-14.55506	-13.56410	-16.28017	-29.41346	-42.06879
-2×10^2	-55.42722	-51.48838	-62.32523	-66.1209	-80.1256
D^{-1}	10^2	2×10^2	3×10^2	10^2	10^2
α	2	2	2	4	6

Table 11
Sherwood number (Sh) at $y = -1$

G	I	II	III	IV	V	VI	VII
1×10^2	-14.29768	-3.90662	-1.41468	-0.25790	15.31475	12.13729	-17.09646
2×10^2	-54.91245	-10.91014	-7.59213	-5.47224	68.97286	54.80628	-65.20266
-1×10^2	-14.55506	-2.51222	-0.28805	-0.64468	15.28269	11.95107	-17.31727
-2×10^2	-55.42722	-8.12134	-5.33888	-6.24581	68.90874	54.43384	-65.64427
k	0.5	1.5	2.5	3.5	0.5	0.5	0.5
N	1	1	1	1	-0.5	-0.8	2

Table 12
Sherwood number (Sh) at $y = -1$

G	I	II	III	IV	V	VI	VII
1×10^2	-4.34972	-8.2555	-14.29768	-18.33151	18.48060	45.47777	-20.07877
2×10^2	-13.46850	-29.65995	-54.91245	-72.11906	80.36572	190.57960	-79.97672
-1×10^2	-4.37109	-8.36415	-14.55506	-18.71162	18.91478	46.40040	-20.53927
-2×10^2	-13.51124	-29.87718	-55.42722	-72.87928	81.23409	192.42490	-80.89772
Sc	0.24	0.6	1.3	2.01	1.3	1.3	1.3
S_0	0.5	0.5	0.5	0.5	-0.5	-1	1

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