

COMMON FIXED POINT THEOREMS OF COMPATIBLE MAPPINGS  
OF TYPE (A-1) AND TYPE (A-2)

L. Dwijendra Singh\*

Department of Mathematics, M.B. College, Imphal, Pin-795001, Manipur, India

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Leenthoi Ningombam

CMJ University, Shillong, Meghalaya, India

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ABSTRACT

In this paper we prove some common fixed point theorems for compatible mappings of type (A-1) and type (A-2) in fuzzy metric spaces. Our results modify and extend some results in the literature.

**Mathematics subject classification:** 54H25, 54E50.

**Key words:** Compatible mappings, Compatible mappings of type (A), Compatible mappings of type (A-1), Compatible mappings of type (A-2), Common fixed point, Fuzzy metric space.

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1. INTRODUCTION

The first important result in the theory of fixed point of compatible mappings was obtained by Gerald Jungck in 1986 [8] as a generalization of commuting mappings. In 1993 Jungck, Murthy and Cho [9] introduced the concept of compatible mappings of type (A) by generalizing the definition of weakly uniformly contraction maps. Pathak and Khan [14] introduced the concept of A-compatible and S-compatible by splitting the definition of compatible mappings of type (A). Pathak *et. al.* [10] renamed A-compatible and S-compatible as compatible mappings of type (A-1) and compatible mappings of type (A-2) respectively and introduced it in fuzzy metric space.

Zadeh [20] introduced the concept of fuzzy sets. The idea of fuzzy metric space was introduced by Kramosil and Michalek [13] which was modified by George and Veeramani [3, 4]. Bijendra Singh and M. S. Chauhan [18] introduced the concept of compatibility in fuzzy metric space and proved some common fixed point theorems in fuzzy metric spaces in the sense of George and Veeramani with continuous  $t$ -norm  $*$  defined by  $a*b = \min\{a, b\}$  for all  $a, b \in [0, 1]$ .

The aim of the paper is to prove some common fixed point theorems of compatible mappings of type (A-1) and type (A-2). These results modify and extend the results in [10, 14, 15, 16, 19].

2. PRELIMINARIES

**Definition 2.1.** [17] A binary operation  $*$ :  $[0, 1] \times [0, 1] \rightarrow [0, 1]$  is a continuous  $t$ -norm if it satisfies the following conditions

- (i)  $*$  is associative and commutative.
- (ii)  $*$  is continuous.
- (iii)  $a*1 = a$  for all  $a \in [0, 1]$ .
- (iv)  $a*b \leq c*d$  whenever  $a \leq c$  and  $b \leq d$ , for each  $a, b, c, d \in [0, 1]$ .

**Definition 2.2.** [3] The 3-tuple  $(X, M, *)$  is called a fuzzy metric space if  $X$  is an arbitrary (non-empty) set,  $*$  is continuous  $t$ -norm, and  $M$  is a fuzzy set on  $X^2 \times (0, \infty)$  satisfying the following conditions:

- (1)  $M(x, y, t) > 0$ ,
- (2)  $M(x, y, t) = 1$  if and only if  $x = y$ ,
- (3)  $M(x, y, t) = M(y, x, t)$ ,

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Corresponding author: L. Dwijendra Singh\*

Department of Mathematics, M.B. College, Imphal, Pin-795001, Manipur, India

$$(4) M(x, y, t) * M(y, z, s) \leq M(x, z, t + s),$$

$$(5) M(x, y, \cdot) : (0, \infty) \rightarrow [0,1] \text{ is continuous}$$

for all  $x, y, z \in X$  and  $t, s > 0$ .

Let  $(X, d)$  be a metric space, and let  $a * b = ab$  or  $a * b = \min \{a, b\}$ . Let  $M(x, y, t) = \frac{t}{t+d(x,y)}$  for all  $x, y \in X$  and  $t > 0$ . Then  $(X, M, *)$  is a fuzzy metric  $M$  induced by  $d$  is called the standard fuzzy metric space [3].

**Definition 2.3.** [5] A sequence  $\{x_n\}$  in a fuzzy metric space  $(X, M, *)$  is said to be convergent to a point  $x \in X$  (denoted by  $\lim_{n \rightarrow \infty} x_n = x$ ), if for each  $\varepsilon > 0$  and each  $t > 0$ , there exists  $n_0 \in \mathbf{N}$  such that

$$M(x_n, x, t) > 1 - \varepsilon \text{ for all } n \geq n_0.$$

The completeness and non completeness of fuzzy metric space was discussed in George and Veeramani [3] and M. Grabiec[5].

**Definition 2.4.** [3] A sequence  $\{x_n\}$  in a fuzzy metric space  $(X, M, *)$  is called Cauchy sequence if for each  $\varepsilon > 0$  and each  $t > 0$ , there exists  $n_0 \in \mathbf{N}$  such that  $M(x_n, x_m, t) > 1 - \varepsilon$  for all  $n, m \geq n_0$ .

**Definition 2.5.** [10] Self mappings  $A$  and  $S$  of a fuzzy metric space  $(X, M, *)$  is said to be compatible if

$$\lim_{n \rightarrow \infty} M(ASx_n, SAx_n, t) = 1 \text{ for all } t > 0, \text{ whenever } \{x_n\} \text{ is a sequence in } X \text{ such that } \lim_{n \rightarrow \infty} Ax_n = \lim_{n \rightarrow \infty} Sx_n = z \text{ for some } z \in X.$$

**Definition 2.6** [10] Self mappings  $A$  and  $S$  of a fuzzy metric space  $(X, M, *)$  is said to be compatible of type (A) if  $\lim_{n \rightarrow \infty} M(ASx_n, SSx_n, t) = \lim_{n \rightarrow \infty} M(SAx_n, AAx_n, t) = 1$  for all  $t > 0$ , whenever  $\{x_n\}$  is a sequence in  $X$  such that

$$\lim_{n \rightarrow \infty} Ax_n = \lim_{n \rightarrow \infty} Sx_n = z \text{ for some } z \in X.$$

**Definition 2.7.** [10] Self mappings  $A$  and  $S$  of a fuzzy metric space  $(X, M, *)$  is said to be compatible of type (A-1) if

$$\lim_{n \rightarrow \infty} M(SAx_n, AAx_n, t) = 1 \text{ for all } t > 0, \text{ whenever } \{x_n\} \text{ is a sequence in } X \text{ such that } \lim_{n \rightarrow \infty} Ax_n = \lim_{n \rightarrow \infty} Sx_n = z \text{ for some } z \in X.$$

**Definition 2.8.** [10] Self mappings  $A$  and  $S$  of a fuzzy metric space  $(X, M, *)$  is said to be compatible of type (A-2) if  $\lim_{n \rightarrow \infty} M(ASx_n, SSx_n, t) = 1$  for all  $t > 0$ , whenever  $\{x_n\}$  is a sequence in  $X$  such that  $\lim_{n \rightarrow \infty} Ax_n = \lim_{n \rightarrow \infty} Sx_n = z$  for some  $z \in X$ .

**Lemma 2.9.** [5] Let  $(X, M, *)$  be a fuzzy metric space. Then for all  $x, y$  in  $X$ ,  $M(x, y, \cdot)$  is non-decreasing.

**Lemma 2.10.** [19] Let  $(X, M, *)$  be a fuzzy metric space. If there exists  $q \in (0, 1)$  such that  $M(x, y, qt) \geq M(x, y, t/q^n)$  for positive integer  $n$ . Taking limit as  $n \rightarrow \infty$ ,  $M(x, y, t) \geq 1$  and hence  $x = y$ .

**Lemma 2.11.** [12] The only  $t$ -norm  $*$  satisfying  $r * r \geq r$  for all  $r \in [0,1]$  is the minimum  $t$ -norm, that is,  $a * b = \min \{a, b\}$  for all  $a, b \in [0,1]$ .

**Proposition 2.12.** [10] Let  $(X, M, *)$  be a fuzzy metric space and let  $A$  and  $S$  be continuous mappings of  $X$  then  $A$  and  $S$  are compatible if and only if they are compatible of type (A).

**Proposition 2.13.** [10] Let  $(X, M, *)$  be a fuzzy metric space and let  $A$  and  $S$  be compatible mappings of type (A-1) and  $Az = Sz$  for some  $z \in X$ , then  $SAz = AAz$ .

**Proposition 2.14.** [10] Let  $(X, M, *)$  be a fuzzy metric space and let  $A$  and  $S$  be compatible mappings of type (A-1) and  $Az = Sz$  for some  $z \in X$ , then  $ASz = SSz$ .

**Proposition 2.15.** [10] Let  $(X, M, *)$  be a fuzzy metric space and let  $A$  and  $S$  be compatible mappings of type (A-1) and let  $Ax_n, Sx_n \rightarrow z$  as  $n \rightarrow \infty$  for some  $z \in X$  then  $AAx_n \rightarrow Sz$  if  $S$  is continuous at  $z$ .

**Proposition 2.16. [10]** Let  $(X, M, *)$  be a fuzzy metric space and let  $A$  and  $S$  be compatible mappings of type (A-2) and let  $Ax_n, Sx_n \rightarrow z$  as  $n \rightarrow \infty$  for some  $z \in X$  then  $SSx_n \rightarrow Az$  if  $A$  is continuous at  $z$ .

### 3. MAIN RESULTS

We prove the following theorem.

**Theorem 3.1.** Let  $(X, M, *)$  be a complete fuzzy metric space and let  $A, B, S$  and  $T$  be a self mappings of  $X$  satisfying the following conditions:

- (i)  $A(X) \subset T(X), B(X) \subset S(X)$ ,
- (ii)  $S$  and  $T$  are continuous
- (iii) the pairs  $\{A, S\}$  and  $\{B, T\}$  are compatible mapping of type (A-1) on  $X$ .
- (iv) there exists  $q \in (0, 1)$  such that for every  $x, y \in X$  and  $t > 0$ ,

$$M(Ax, By, qt) \geq M(Sx, Ty, t) * M(Ax, Sx, t) * M(By, Ty, t) * M(Ax, Ty, t)$$

Then  $A, B, S$  and  $T$  have a unique common point in  $X$ .

**Proof:** Since  $A(X) \subset T(X)$  and  $B(X) \subset S(X)$ , for any  $x_0 \in X$ , there exists  $x_1 \in X$  such that  $Ax_0 = Tx_1$  and for this  $x_1 \in X$ , there exists  $x_2 \in X$  such that  $Bx_1 = Sx_2$ . Inductively, we define a sequence  $\{y_n\}$  in  $X$  such that

$$y_{2n-1} = Tx_{2n-1} = Ax_{2n-2} \text{ and } y_{2n} = Sx_{2n} = Bx_{2n-1}, \text{ for all } n = 0, 1, 2, \dots$$

From (iv),

$$\begin{aligned} M(y_{2n+1}, y_{2n+2}, qt) &= M(Ax_{2n}, Bx_{2n+1}, qt) \\ &\geq M(Sx_{2n}, Tx_{2n+1}, t) * M(Ax_{2n}, Sx_{2n}, t) * M(Bx_{2n+1}, Tx_{2n+1}, t) * M(Ax_{2n}, Tx_{2n+1}, t) \\ &= M(y_{2n}, y_{2n+1}, t) * M(y_{2n+1}, y_{2n}, t) * M(y_{2n+2}, y_{2n+1}, t) * M(y_{2n+1}, y_{2n+1}, t) \\ &\geq M(y_{2n}, y_{2n+1}, t) * M(y_{2n+1}, y_{2n+2}, t) \end{aligned}$$

From lemma 2.9 and 2.10, we have

$$M(y_{2n+1}, y_{2n+2}, qt) \geq M(y_{2n}, y_{2n+1}, t) \tag{3.1.1}$$

Similarly, we have

$$M(y_{2n+2}, y_{2n+3}, qt) \geq M(y_{2n+1}, y_{2n+2}, t) \tag{3.1.2}$$

From (3.1.1) and (3.1.2), we have

$$M(y_{n+1}, y_{n+2}, qt) \geq M(y_n, y_{n+1}, t) \tag{3.1.3}$$

From (3.1.3), we have

$$\begin{aligned} M(y_n, y_{n+1}, t) &\geq M(y_n, y_{n-1}, \frac{t}{q}) \\ &\geq M(y_{n-2}, y_{n-1}, \frac{t}{q^2}) \\ &\geq \dots \geq M(y_1, y_2, \frac{t}{q^n}) \rightarrow 1 \text{ as } n \rightarrow \infty. \end{aligned}$$

So,  $M(y_n, y_{n+1}, t) \rightarrow 1$  as  $n \rightarrow \infty$  for any  $t > 0$ . For each  $\varepsilon > 0$  and each  $t > 0$ , we can choose  $n_0 \in \mathbb{N}$  such that

$$M(y_n, y_{n+1}, t) > 1 - \varepsilon \text{ for all } n > n_0.$$

For  $m, n \in \mathbb{N}$ , we suppose  $m \geq n$ . Then we have that

$$M(y_n, y_m, t) \geq M(y_n, y_{n+1}, \frac{t}{m-n}) * M(y_{n+1}, y_{n+2}, \frac{t}{m-n}) * \dots * M(y_{m-1}, y_m, \frac{t}{m-n})$$

$$\geq (1-\varepsilon)^*(1-\varepsilon)^* \dots\dots\dots(m-n) \text{ times.}$$

$$\geq (1-\varepsilon)$$

and hence  $\{y_n\}$  is a Cauchy sequence in  $X$ .

Since  $(X, M, *)$  is complete,  $\{y_n\}$  converges to some point  $z \in X$ , and so

$\{Ax_{2n-2}\}$ ,  $\{Sx_{2n}\}$ ,  $\{Bx_{2n-1}\}$  and  $\{Tx_{2n-1}\}$  also converges to  $z$ .

From proposition 2.15 and (iii), we have

$$AAx_{2n-2} \rightarrow Sz \tag{3.1.4}$$

$$\text{and } BBx_{2n-1} \rightarrow Tz \tag{3.1.5}$$

From (iv), we get

$$M(AAx_{2n-2}, BBx_{2n-1}, qt) \geq M(SAx_{2n-2}, TBx_{2n-1}, t)^* M(AAx_{2n-2}, SAx_{2n-2}, t)^* M(BBx_{2n-1}, TBx_{2n-1}, t)^* M(AAx_{2n-2}, TBx_{2n-1}, t)$$

Taking limit as  $n \rightarrow \infty$  and using (3.1.4) and (3.1.5), we have

$$M(Sz, Tz, qt) \geq M(Sz, Tz, t)^* M(Sz, Sz, t)^* M(Tz, Tz, t)^* M(Sz, Tz, t)$$

$$\geq M(Sz, Tz, t)^* 1^* 1^* M(Sz, Tz, t)$$

$$\geq M(Sz, Tz, t).$$

$$\text{It follows that } Sz = Tz. \tag{3.1.6}$$

Now, from (iv),

$$M(Az, BBx_{2n-1}, qt) \geq M(Sz, TBx_{2n-1}, t)^* M(Az, Sz, t)^* M(BBx_{2n-1}, TBx_{2n-1}, t)^* M(Az, TBx_{2n-1}, t)$$

Again, taking limit as  $n \rightarrow \infty$  and using (3.1.5) and (3.1.6), we have

$$M(Az, Tz, qt) \geq M(Sz, Sz, t)^* M(Az, Tz, t)^* M(Az, Tz, t)^* M(Az, Tz, t)$$

$$\geq M(Az, Tz, t).$$

$$\text{and hence } Az = Tz. \tag{3.1.7}$$

From (iv), (3.1.6) and (3.1.7),

$$\begin{aligned} M(Az, Bz, qt) &\geq M(Sz, Tz, t)^* M(Az, Sz, t)^* M(Bz, Tz, t)^* M(Az, Tz, t) \\ &= M(Az, Az, t)^* M(Az, Az, t)^* M(Bz, Az, t)^* M(Az, Az, t) \\ &\geq M(Az, Bz, t). \end{aligned}$$

$$\text{and hence } Az = Bz. \tag{3.1.8}$$

From (3.1.6), (3.1.7) and (3.1.8), we have

$$Az = Bz = Tz = Sz. \tag{3.1.9}$$

Now, we show that  $Bz = z$ .

From (iv),

$$M(Ax_{2n}, Bz, qt) \geq M(Sx_{2n}, Tz, t)^* M(Ax_{2n}, Sx_{2n}, t)^* M(Bz, Tz, t)^* M(Ax_{2n}, Tz, t)$$

And, taking limit as  $n \rightarrow \infty$  and using (3.1.6) and (3.1.7), we have

$$\begin{aligned} M(z, Bz, qt) &\geq M(z, Tz, t) * M(z, z, t) * M(Bz, Tz, t) * M(z, Tz, t) \\ &= M(z, Bz, t) * 1 * M(Az, Az, t) * M(z, Bz, t) \\ &\geq M(z, Bz, t). \end{aligned}$$

And hence  $Bz = z$ . Thus from (3.1.9),  $z = Az = Bz = Tz = Sz$  and  $z$  is a common fixed point of  $A, B, S$  and  $T$ .

In order to prove the uniqueness of fixed point, let  $w$  be another common fixed point of  $A, B, S$  and  $T$ . Then

$$\begin{aligned} M(z, w, qt) &= M(Az, Bw, qt) \\ &\geq M(Sz, Tw, t) * M(Az, Sz, t) * M(Bw, Tw, t) * M(Az, Tw, t) \\ &\geq M(z, w, t). \end{aligned}$$

From lemma 2.10,  $z = w$ . This completes the proof of theorem.

**Corollary 3.2.** Let  $(X, M, *)$  be a complete fuzzy metric space and let  $A, B, S$  and  $T$  be a self mappings of  $X$  satisfying (i) - (iii) of theorem 3.1 and there exists  $q \in (0, 1)$  such that

$$M(Ax, By, qt) \geq M(Sx, Ty, t) * M(Ax, Sx, t) * M(By, Ty, t) * M(By, Sx, 2t) * M(Ax, Ty, t)$$

for every  $x, y \in X$  and  $t > 0$ . Then  $A, B, S$  and  $T$  have a unique common point in  $X$ .

**Corollary 3.3.** Let  $(X, M, *)$  be a complete fuzzy metric space and let  $A, B, S$  and  $T$  be a self mappings of  $X$  satisfying (i) - (iii) of theorem 3.1 and there exists  $q \in (0, 1)$  such that

$$M(Ax, By, qt) \geq M(Sx, Ty, t)$$

for every  $x, y \in X$  and  $t > 0$ . Then  $A, B, S$  and  $T$  have a unique common point in  $X$ .

**Corollary 3.4.** Let  $(X, M, *)$  be a complete fuzzy metric space and let  $A, B, S$  and  $T$  be a self mappings of  $X$  satisfying (i) - (iii) of theorem 3.1 and there exists  $q \in (0, 1)$  such that

$$M(Ax, By, qt) \geq M(Sx, Ty, t) * M(Sx, Ax, t) * M(Ax, Ty, t)$$

for every  $x, y \in X$  and  $t > 0$ . Then  $A, B, S$  and  $T$  have a unique common point in  $X$ .

**Theorem 3.5.** Let  $(X, M, *)$  be a complete fuzzy metric space. Then continuous self mappings  $S$  and  $T$  of  $X$  have a common fixed point in  $X$  if and only if there exists a self mapping  $A$  of  $X$  such that the following condition are satisfied:

- (i)  $A(X) \subset T(X) \cap S(X)$ ,
- (ii) the pairs  $\{A, S\}$  and  $\{A, T\}$  are compatible mapping of type (A-1) on  $X$ ,
- (iii) there exists  $q \in (0, 1)$  such that for every  $x, y \in X$  and  $t > 0$ ,

$$M(Ax, Ay, qt) \geq M(Sx, Ty, t) * M(Ax, Sx, t) * M(Ay, Ty, t) * M(Ax, Ty, t)$$

In fact  $A, S$  and  $T$  have a unique common point in  $X$ .

**Proof:** We shown that the necessity of the conditions (i)-(iii). Suppose that  $S$  and  $T$  have a common fixed point in  $X$ , say  $z$ . Then  $Sz = z = Tz$ .

Let  $Ax = z$  for all  $x \in X$ . Then we have  $A(X) \subset T(X) \cap S(X)$  and we know that  $[A, S]$  and  $[A, T]$  are compatible mapping of type (A-1), in fact  $A \circ S = S \circ A$  and  $A \circ T = T \circ A$ , and hence the conditions (i) and (ii) are satisfied.

For some  $q \in (0, 1)$ , we get

$$M(Ax, Ay, qt) = 1 \geq M(Sx, Ty, t) * M(Ax, Sx, t) * M(Ay, Ty, t) * M(Ax, Ty, t)$$

for every  $x, y \in X$  and  $t > 0$  and hence The condition (iii) is satisfied.

Now, for the sufficiency of the conditions, let  $A = B$  in theorem 3.1. Then  $A, S$  and  $T$  have a unique common fixed point in  $X$ .

**Corollary 3.6.** Let  $(X, M, *)$  be a complete fuzzy metric space. Then continuous self mappings  $S$  and  $T$  of  $X$  have a common fixed point in  $X$  if and only if there exists a self mapping  $A$  of  $X$  satisfying (i) – (ii) of theorem 3.5 and there exists  $q \in (0, 1)$  such that for every  $x, y \in X$  and  $t > 0$

$$M(Ax, Ay, qt) \geq M(Sx, Ty, t) * M(Ax, Sx, t) * M(Ay, Ty, t) * M(Ax, Sx, 2t) * M(Ax, Ty, t)$$

In fact  $A, S$  and  $T$  have a unique common point in  $X$ .

**Corollary 3.7.** Let  $(X, M, *)$  be a complete fuzzy metric space. Then continuous self mappings  $S$  and  $T$  of  $X$  have a common fixed point in  $X$  if and only if there exists a self mapping  $A$  of  $X$  satisfying (i) – (ii) of theorem 3.5 and there exists  $q \in (0, 1)$  such that for every  $x, y \in X$  and  $t > 0$

$$M(Ax, Ay, qt) \geq M(Sx, Ty, t)$$

In fact  $A, S$  and  $T$  have a unique common point in  $X$ .

**Corollary 3.8.** Let  $(X, M, *)$  be a complete fuzzy metric space. Then continuous self mappings  $S$  and  $T$  of  $X$  have a common fixed point in  $X$  if and only if there exists a self mapping  $A$  of  $X$  satisfying (i) – (ii) of theorem 3.5 and there exists  $q \in (0, 1)$  such that for every  $x, y \in X$  and  $t > 0$

$$M(Ax, Ay, qt) \geq M(Sx, Ty, t) * M(Sx, Ax, t) * M(Ax, Ty, t)$$

In fact  $A, S$  and  $T$  have a unique common point in  $X$ .

**Remark:** Corresponding results for compatible mappings of type (A-2) can also be obtained.

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