

EQUILIBRIUM STRUCTURE OF DIFFERENTIALLY ROTATING AND TIDALLY DISTORTED PRASAD MODEL INCLUDING MASS VARIATION INSIDE THE STAR

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(Received on: 14-04-12; Accepted on: 30-04-12)

ABSTRACT

In this paper we propose suitable modifications in the concept of Roche equipotentials to account for the effect of mass variation inside the star on its equipotential surfaces and use this in conjunction with Kippenhahn and Thomas⁴ approach, in a manner earlier used by Mohan et. al.[12], to incorporate the effects of differentially rotating and tidally distorted stellar models of stars using the law of the type $\omega = b_1 + b_2 s^2$ where b_1, b_2 are numerical constants and s is the distance of rotating fluid element from the axis of rotation. The proposed method has been used to compute the structure parameters of differentially rotating and tidally distorted Prasad model of the star.

Keywords: Roche equipotentials, equilibrium structure of stars, Prasad model, rotating stars, stars in binary systems

1. INTRODUCTION

Observations show that most of the binary stars are rotating as well as revolving around their common centers of mass. Rotational forces as well as tidal distortion of the companion star have their effect on the equilibrium structure, shape and other observable physical parameters of binary stars. Prasad[13] introduced a model (called Prasad model thereafter) in which density ρ inside the star varies according to the law $\rho = \rho_c (1 - x^2)$, ρ_c being the density of fluid at the centre and x a non-dimensional measure of the distance of a fluid element from its centre. Since then several authors such as Gurm[3], Prasad and Mohan[14], Agarwal[1], Sharma[15] etc. have addressed themselves to these types of problems.

The mathematical problem of determining the effects of rotation and tidal forces on the equilibrium structure of a star is quite complex. Approximate methods have therefore often been used in literature to study such problems. In some such approximations Kopal [5,6]; Mohan and Singh[7]; Mohan and Saxena[9]; Mohan et al[10,11], the actual equipotential surfaces of a rotationally and tidally distorted star are approximated by equivalent Roche equipotentials, assuming both stars in the binary system to be point masses. This approximation is valid for highly centrally condensed types of stars. However in the case of stars in which the central condensation is not too large, this approximation is not very justified. Therefore, it will be of interest to analyze the effect of incorporating suitable modifications in the Roche equipotentials to account for the mass distribution inside the star. Baur [2] recently modified the Roche potentials to account for mechanical effects of the mutual irradiation of the binary components. In a somewhat similar manner we have suitably modified the Roche equipotentials to account for the mass distribution inside the primary component (e.g. Mohan et al.[12].

The paper is organized as follows: expressions for the modified Roche equipotentials of a rotationally and tidally distorted star are obtained in Section 2. This modified concept of Roche equipotentials is next used in Section 3 to obtain the equilibrium structure of a differentially and tidally distorted Prasad model of a star. Computational results for the inner structure, shapes and certain other physical parameters of differentially and tidally distorted Prasad model including mass variation inside the star is next obtained in Section 4 and compared with corresponding results earlier obtained by some other authors.

2. MODIFIED ROCHE EQUIPOTENTIALS

In order to investigate the equilibrium structures of binary stars, the concept of Roche equipotentials has been frequently used in literature Kopal[5]. However, while computing the Roche equipotential surfaces, the whole mass of the stars (the primary as well as the secondary) is assumed to be concentrated at their centers. This approximation,

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though reasonably valid for highly centrally condensed stars, is not reasonably true for stars, such as main sequence and pre-main sequence stars which are not very highly centrally condensed. The concept of Roche equipotentials, therefore, needs to be suitably modified to incorporate the effects of mass distribution inside the star so that it can provide a better approximation for the structure of a differentially and tidally distorted star which is not very highly centrally condensed.

In this section we suitably modify the mathematical expression for Roche equipotentials to reasonably account for the mass distribution inside the primary star (in whose inner structure we are primarily interested) assuming as earlier that the secondary star is still a point mass.

Let M_0 and M_1 be the masses of the primary and the secondary components of a binary system of stars in which the primary is assumed to be much massive than the secondary ($M_0 \gg M_1$). Let $M_0(r)$ represent the mass interior to a sphere of radius r inside the primary component. Let D be the mutual separation between the centers of the two stars. Further suppose that the position of the two components of this binary system is referred to a rectangular system of Cartesian coordinates having the origin at the center of gravity of the primary of mass M_0 , the x -axis along the line joining the centers of the two components of the binary, and z -axis perpendicular to the plane of the orbit of the two components (Fig 1).

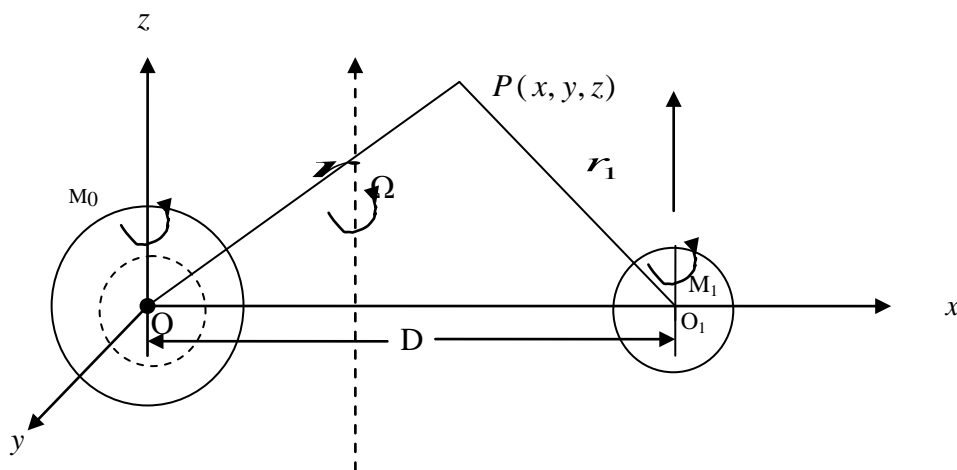


FIG. 1 AXES OF REFERENCE OF ROTATING BINARY SYSTEM

Then the total potential ψ due to the gravitational, rotational and other disturbing forces acting at an arbitrary point $P(x, y, z)$ distant r from the centre of the primary and r_1 from the centre of the secondary may be expressed as

$$\psi = G \frac{M^*}{r} + G \frac{M_1}{r_1} + \frac{1}{2} \Omega^2 \left(\left(x - \frac{M_1 D}{M_0 + M_1} \right)^2 + y^2 \right) \quad (1)$$

where $M^* = \begin{cases} M_0 & \text{if } r > R \\ M_0(r) & \text{if } r < R \end{cases}$. Here Ω is the angular velocity of rotation and G the gravitational constant.

The three terms on the right hand side of (1) are, respectively, the potential arising from the mass of the primary, the disturbing potential of its companion of mass M_1 and the potential arising from the centrifugal force. In the first term on the right hand side of (1) M_0 normally used in the definition of Roche potential has been replaced by M^* to account for the mass distribution inside the primary. This has been done keeping in view the fact that where as in the case of a sphere the gravitational potential at a point outside the sphere is $\frac{GM}{r}$, the gravitational potential at a point

inside the sphere is $\frac{GM(r)}{r}$, $M(r)$ being the mass contained inside a sphere of radius r concentric with the centre of stars of mass M .

Equation (1) in nondimensional form can be expressed as

$$\psi = \frac{z}{r} + \frac{q}{r_1} + \frac{1}{2} b_1^2 \left\{ r^2 (1 - \nu^2) - \frac{2qr\lambda}{1+q} + \frac{q^2}{(1+q)^2} \right\} + \frac{b_1 b_2}{2} \left\{ r^2 (1 - \nu^2) - \frac{2qr\lambda}{1+q} + \frac{q^2}{(1+q)^2} \right\}^2 + \frac{b_2^2}{6} \left\{ r^2 (1 - \nu^2) - \frac{2qr\lambda}{1+q} + \frac{q^2}{(1+q)^2} \right\}^3 \quad (2)$$

where $\psi^* = \frac{D\psi}{GM_0} - \frac{M_1^2}{2M_0(M_0 + M_1)}$, and

$$z = \begin{cases} \frac{M_0(r)}{M_0}, & \text{if } r < R \\ 1, & \text{if } r > R \end{cases} \quad \text{Also } r^* = \frac{r}{D} \text{ is a}$$

nondimensional measure of the distance and $\lambda = \sin \theta \cos \phi$, $\mu = \sin \theta \sin \phi$, $\nu = \cos \theta$, r, θ, ϕ being the spherical polar coordinates of the point P . Obviously, z is a nondimensional parameter, which becomes zero at the center of the primary M_0 and one at the points on and outside the surface of the primary. It will have a value between

0 and 1 at points inside the primary. Also $q = \frac{M_1}{M_0}$ is a nondimensional parameter representing the ratio of the mass

of the secondary over the mass of the primary ($q < 1$), and $2n$ represents the square of the normalized angular velocity Ω . In equation (2) if $q = 0$ it reduces to the potential of a rotating spherical model rotating with angular velocity Ω and if $n = 0$, then it reduces to the potential of a spherical model distorted only by the tidal effects of the

companion. For a binary system in synchronous rotation, $\Omega^2 = \frac{G(M_0 + M_1)}{D^3}$ this in terms of the nondimensional

variables as defined above, becomes $n = \frac{q+1}{2}$.

Equipotential surfaces represented by $\psi^* = \text{constant}$ as given in (2) are the modified Roche equipotential surfaces of the primary component of a rotationally and tidally distorted binary system which reasonably account for the mass distribution in the interior of the primary. This, however, modifies potential at the points inside the primary only. On substituting $z = 1$ in (2) or $M_0(r) = M_0$ in (1), it reduces to the expression for the Roche equipotential which has been earlier used by Kopal⁵ and other authors.

Following Kopal⁵ it can be shown that the values of r, θ, ϕ on the surfaces of the Roche equipotentials as given by (2) are connected through the relation

$$\begin{aligned} r = r_0 D \left[1 + \left(\frac{qP_2}{z^2} + \frac{b_1^2}{2z} x \right) r_0^3 + \frac{qP_3}{z^2} r_0^4 + \left(\frac{qP_4}{z^2} + \frac{b_1 b_2}{2z} x^2 + \frac{5}{2z} \lambda b_1^2 q x \right) r_0^5 + \right. \\ \left. + \left(\frac{qP_5}{z^2} + \frac{3q^2 P_2^2}{z^2} + \frac{3qP_2 b_1^2}{z^2} x \right) r_0^6 + \left(\frac{qP_6}{z^2} + \frac{b_2^2}{6z} x^3 + \frac{7}{4z^2} \lambda b_1^2 q x^2 + \frac{7q^2 P_2 P_3}{z^2} \right) r_0^7 + \right. \\ \left. + \left(\frac{qP_7}{z^2} + \frac{8q^2 P_2 P_4}{z^2} + \frac{4qP_4 b_1^2}{z^2} x + \frac{4q^2 P_3^2}{z^2} \right) r_0^8 + \right. \\ \left. + \left(\frac{qP_8}{z^2} + \frac{3\lambda b_2^2 q}{2z^2} x^3 + \frac{9q^2 P_3 P_4}{z^2} + \frac{9q}{4z^2} b_1^2 x^2 + \frac{9q^2 P_2 P_5}{z^2} \right) r_0^9 + \right. \\ \left. + \left(\frac{qP_9}{z^2} + \frac{10q^2 P_2 P_6}{z^2} + \frac{10q^2 P_3 P_5}{z^2} + \frac{5qb_2^2 P_2}{3z^2} x^3 + \frac{5q^2 P_4^2}{z^2} \right) r_0^{10} + \dots \right] \quad (3) \end{aligned}$$

where $r_0 = \frac{z}{\psi - q}$, $a_0 = \frac{q P_2}{z} + \frac{n(1 - \nu^2)}{z}$, $P_j = P_j(\lambda)$ Legendre polynomials and terms up to second order of smallness in n and q are retained. This relation can be used to obtain the shapes of Roche equipotential $\psi = \text{constant}$. Whereas on account of inclusion of mass distribution inside the primary, these will get modified at points inside the primary due to the presence of z , outside the primary (where $z = 1$), these will be same as earlier obtained by Kopal[5]. Following Kopal[5] and Mohan et. al.[12], modified expressions for the volume enclosed V_ψ , and the surface area S_ψ of an equipotential surface can be obtained if desired in series form.

3. EQUILIBRIUM STRUCTURES OF DIFFERENTIALLY AND TIDALLY DISTORTED PRASAD MODEL

If we assume that the primary component of binary system behaves as Prasad model and rotating about its axis then its equilibrium structure will be distorted by rotation as well as the tidal effects of the companion. In order to determine the equilibrium structure of this rotationally and tidally distorted stellar model we may follow the approach of Mohan and Saxena[9], it is assumed that the rotational velocity and the mass of the secondary as compared to the primary are suitably small.

Let r_ψ denote the radius of the topologically equivalent spherical model which corresponds to an equipotential surface $\psi = \text{constant}$ of this differentially and tidally distorted Prasad model. Also, let R_ψ be the value of r_ψ on the equipotentials surface $\psi = \text{constant}$ of this differentially and tidally distorted model. Following the approach as discussed in Seema[16] r_ψ and R_ψ are given as.

$$r_\psi = Dr_0 \left[1 + \frac{2b_1^2 r_0^3}{3z} + \frac{4b_1 b_2 r_0^5}{15z} + \frac{4q^2 r_0^6}{4z^2} + \frac{8b_2^2 r_0^7}{15z} + \frac{5q^2 r_0^8}{7z^2} + \frac{2q^2 r_0^{10}}{3z^2} \right] \quad (4)$$

$$R_\psi = Dr_{0s} \left[1 + \frac{4n r_{0s}^3}{3z} + \left(\frac{4q^2 r_0^6}{4z^2} + \frac{8nq}{15z^2} + \frac{76n^2}{45z^2} \right) r_{0s}^6 + \frac{5q^2 r_{0s}^8}{7z^2} + \frac{2q^2 r_{0s}^{10}}{3z^2} + \dots \right] \quad (5)$$

and

$$z = \frac{5}{2} \left(\frac{r_\psi}{R_\psi} \right)^3 - \frac{3}{2} \left(\frac{r_\psi}{R_\psi} \right)^5$$

where $r_0 = \frac{z}{\psi - q}$ (6)

Further let ρ_ψ denote the value of density on an equipotentials $\psi = \text{constant}$. The density distribution law of differentially and tidally distorted Prasad model is given as

$$\rho_\psi = \rho_c \left(1 - \frac{r_\psi^2}{R_\psi^2} \right) \quad (7)$$

On substituting the value of r_ψ and R_ψ from equation (4) and (5) in equation (7) we get

$$\rho_\psi = \rho_c \left[1 - \frac{D^2 r_0^2}{R_\psi^2} \left\{ 1 + \frac{2b_1^2 r_0^3}{3z} + \frac{8b_1 b_2 r_0^5}{15z} + \frac{8q^2 r_0^6}{5z^2} + \frac{6b_2^2 r_0^7}{105z} + \frac{10q^2 r_0^8}{7z^2} + \frac{4q^2 r_0^{10}}{3z^2} + \dots \right\} \right] \quad (8)$$

On substituting value of ρ_ψ from (8) and using the approach used by Saxena[9] integrating w.r.t. r_0 and using the fact that $M_\psi = 0$ at center $r_0 = 0$ we get

$$M_{\psi} = \frac{4\pi\rho_c D^3 r_0^3}{3} \left[1 - \frac{3D^2}{5R_{\psi}^2} r_0^2 + \frac{b_1^2 r_0^3}{z} + \frac{4b_1 b_2 r_0^5}{5z^2} - \frac{b_1^2 R^2 r_0^5}{zR_{\psi}^2} + \frac{12q^2 r_0^6}{5z^2} \right. \\ \left. + \frac{16b_2^2 r_0^7}{70z} - \frac{4b_1 b_2 R^2 r_0^7}{5zR_{\psi}^2} + \left\{ \frac{15q^2}{7z^2} - \frac{12q^2 R^2}{5z^2 R_{\psi}^2} \right\} r_0^8 + \left(\frac{2q^2}{5z^2} - \frac{15q^2 R^2}{7R_{\psi}^2} \right) r_0^{10} + \dots \right] \quad (9)$$

Similarly on substituting ρ_{ψ} from (8) and M_{ψ} from (9) and using the approach used by Saxena[9] and integrating with respect to r_0 we get

$$P_{\psi} = \frac{2\pi z G \rho_c^2 D^2}{3} \left[K - r_0^2 + \frac{4D^2 r_0^4}{5R_{\psi}^2} - \frac{2b_1^2 r_0^5}{5z} - \frac{D^4 r_0^6}{5R_{\psi}^2} - \frac{8b_1 b_2 r_0^7}{35z} + \frac{16D^2 b_1^2 r_0^7}{21zR_{\psi}^2} + \right. \\ \left. + \frac{q^2 r_0^8}{2z^2} - \frac{16b_2^2 r_0^9}{315z} + \frac{64b_1 b_2 D^2 r_0^9}{135zR_{\psi}^2} - \frac{14D^4 b_1^2 r_0^9}{45zR_{\psi}^4} \right. \\ \left. - \frac{3q^2 r_0^{10}}{10z^2} + \frac{144D^2 q^2 r_0^{10}}{125z^2 R_{\psi}^2} + \dots \right] \quad (10)$$

where K is a constant of integration whose value may be calculated by using boundary condition say $P_{\psi} = 0$ at $r_0 = r_{0s}$. This yield

$$K = r_{0s}^2 - \frac{4D^2 r_{0s}^4}{5R_{\psi}^2} + \frac{2b_1^2 r_{0s}^5}{5z} + \frac{D^4 r_{0s}^6}{5R_{\psi}^2} + \frac{8b_1 b_2 r_{0s}^7}{35z} - \frac{16D^2 b_1^2 r_{0s}^7}{21zR_{\psi}^2} + \frac{q^2 r_{0s}^8}{2z^2} \\ + \frac{16b_2^2 r_{0s}^9}{315z} - \frac{64b_1 b_2 D^2 r_{0s}^9}{135zR_{\psi}^2} + \frac{14D^4 b_1^2 r_{0s}^9}{45zR_{\psi}^4} + \frac{3q^2 r_{0s}^{10}}{10z^2} - \frac{144D^2 q^2 r_{0s}^{10}}{125z^2 R_{\psi}^2} + \dots \quad (11)$$

Similarly the volume V_{ψ} , surface area S_{ψ} , g^{-} and g^{-1} of rotationally and tidally distorted Prasad model are obtained as

$$V_{\psi} = \frac{4\pi r_0^3}{3} \left[1 + \frac{b_1^2 r_0^3}{z} + \frac{4b_1 b_2 r_0^5}{5z} + \frac{12q^2}{5z^2} + \frac{8b_2^2 r_0^7}{35z} + \frac{15q^2 r_0^8}{7z^2} + \frac{2q^2 r_0^{10}}{z^2} + \dots \right] \quad (12)$$

$$S_{\psi} = 4\pi r_0^2 \left[1 + \frac{2b_1^2 r_0^3}{3z} + \frac{8b_1 b_2 r_0^5}{15z} + \frac{7q^2 r_0^6}{5z^2} + \frac{16b_2^2 r_0^7}{105z} + \frac{9q^2 r_0^8}{7z^2} + \frac{11q^2 r_0^{10}}{9z^2} + \dots \right] \quad (13)$$

$$g^{-} = \frac{z G M_{\psi}}{r_0^2} \left[1 - \frac{4b_1^2 r_0^3}{3z} - \frac{8b_1 b_2 r_0^5}{5z} - \frac{3q^2 r_0^6}{z^2} - \frac{64b_2^2 r_0^7}{105z} - \frac{51q^2 r_0^8}{14z^2} - \frac{13q^2 r_0^{10}}{3z^2} + \dots \right] \quad (14)$$

$$g^{-1} = \frac{r_0^2}{z G M_{\psi}} \left[1 + \frac{4b_1^2 r_0^3}{3z} + \frac{8b_1 b_2 r_0^5}{5z} + \frac{31q^2 r_0^6}{5z^2} + \frac{64b_2^2 r_0^7}{105z} + \frac{101q^2 r_0^8}{14z^2} + \frac{75q^2 r_0^{10}}{9z^2} + \dots \right] \quad (15)$$

4. NUMERICAL EVALUATION OF STRUCTURE FOR PRASAD MODEL AND ANALYSIS OF RESULTS

For a better appreciation of the effects of differentially and tidally distorted stars the values of density, mass and pressure at various points inside the star we have used equations (8), (9) and (10) to numerically compute the values of ρ_{ψ} , M_{ψ} and P_{ψ} at various points inside Prasad model.

The results presented in Tables 1(A-D) give the values of certain structures parameters and related observable quantities of undistorted, rotationally distorted, tidally distorted and rotationally and tidally distorted Prasad model for

$\psi = 5.0$. Results show that with the modification of expression for potential to account for mass variation inside the star on its equipotential surfaces, our results show marginal changes but no significant trend is observed.

Table 1 A:

Structure Parameters of Uniformly Distorted Prasad Model For $\psi_s^* = 5, b_1 = 0, b_2 = 0, q = 0.1$

x	V_ψ	s_ψ	ρ_ψ	M_ψ	P_ψ	σ	ε	T_e/T_p	L_e/L_p
0.1	0.00001	0.00042	0.99000	0.00248	0.01313	0.00035	0.00035	0.14283	0.99825
0.2	0.00006	0.00166	0.96000	0.01952	0.01499	0.00036	0.00036	0.20199	0.99817
0.3	0.00023	0.00374	0.91000	0.06385	0.01317	0.00038	0.00038	0.24738	0.99806
0.4	0.00054	0.00666	0.84000	0.14464	0.01081	0.00041	0.00041	0.28565	0.99791
0.5	0.00106	0.01041	0.75000	0.26563	0.00819	0.00044	0.00044	0.31936	0.99772
0.6	0.00183	0.01499	0.64000	0.42336	0.00559	0.00049	0.00049	0.34983	0.99745
0.7	0.00291	0.20408	0.51000	0.60536	0.00327	0.00056	0.00056	0.37784	0.99709
0.8	0.00435	0.02665	0.36000	0.78848	0.00149	0.00066	0.00066	0.40391	0.99657
0.9	0.00622	0.03373	0.18999	0.93676	0.00036	0.00081	0.00081	0.42837	0.99576
1.0	0.00800	0.41692	0.00000	1.00000	0.00000	0.00100	0.00100	0.45148	0.99438

Table 1 B

Structure Parameters of Rotationally and Tidally Distorted Prasad Model $\psi_s^* = 5, b_1 = 0.3162, b_2 = 0, q = 0.1$

x	V_ψ	s_ψ	ρ_ψ	M_ψ	P_ψ	σ	ε	T_e/T_p	L_e/L_p
0.1	0.00001	0.00041	0.99000	0.00284	0.01305	0.00052	0.00052	0.14282	0.99733
0.2	0.00006	0.00166	0.96001	0.01951	0.01499	0.00053	0.00053	0.20197	0.99729
0.3	0.00023	0.00374	0.91002	0.06382	0.01317	0.00056	0.00056	0.24736	0.99715
0.4	0.00054	0.00666	0.84005	0.14457	0.01081	0.00059	0.00059	0.28562	0.99697
0.5	0.00106	0.01041	0.75007	0.26551	0.00820	0.00064	0.00064	0.31933	0.99671
0.6	0.00183	0.01499	0.64010	0.42321	0.00559	0.00071	0.00071	0.34979	0.99637
0.7	0.00291	0.02041	0.51012	0.60523	0.00327	0.00080	0.00080	0.37780	0.99589
0.8	0.00435	0.02666	0.36012	0.78834	0.00146	0.00093	0.00093	0.40385	0.99519
0.9	0.00620	0.03375	0.19010	0.93670	0.00036	0.00114	0.00114	0.42830	0.99411
1.0	0.00850	0.41673	0.00000	1.00000	0.00000	0.001499	0.001497	0.451384	0.99226

Table C

Structures Parameters of Rotationally and Tidally Distorted Prasad Model $\psi_s^* = 5, b_1 = 0, b_2 = 0.3162, q = 0.1$

X	V_ψ	s_ψ	ρ_ψ	M_ψ	P_ψ	σ	ε	T_e/T_p	L_e/L_p
0.1	0.00001	0.00041	0.99000	0.00249	0.01313	0.00035	0.00035	0.14832	0.998245
0.2	0.00006	0.00166	0.96000	0.01952	0.01499	0.00036	0.00036	0.20199	0.998168
0.3	0.00022	0.00374	0.91000	0.06386	0.01317	0.00038	0.00038	0.24738	0.998060
0.4	0.00054	0.00666	0.84000	0.14464	0.01081	0.00041	0.00041	0.28565	0.99915
0.5	0.00106	0.01041	0.75000	0.26562	0.00819	0.00044	0.00044	0.31936	0.997721
0.6	0.00183	0.01499	0.64000	0.42333	0.00559	0.00049	0.00049	0.34983	0.997459
0.7	0.00291	0.02040	0.51000	0.60539	0.00327	0.00056	0.00056	0.37784	0.997096
0.8	0.00435	0.02665	0.36000	0.78848	0.00146	0.00066	0.00066	0.40391	0.996572
0.9	0.00619	0.03373	0.18999	0.93676	0.00035	0.00081	0.00081	0.42837	0.995764
1.0	0.00850	0.41649	0.00000	1.00000	0.00000	0.00107	0.00107	0.45148	0.994383

Table: D

Structure Parameters of Differentially Rotating and Tidally Distorted Prasad Model

$\psi_s^* = 5, b_1 = .3162, b_2 = .32, q = 0.1$

X	V_ψ	s_ψ	ρ_ψ	M_ψ	P_ψ	σ	ε	T_e/T_p	L_e/L_p
0.1	0.00001	0.00042	0.99004	0.00248	0.01304	0.00053	0.00053	0.14282	0.99731
0.2	0.00006	0.00166	0.96001	0.01951	0.01489	0.00054	0.00054	0.20198	0.99726
0.3	0.00023	0.00375	0.91003	0.06385	0.01314	0.00056	0.00056	0.24736	0.99713
0.4	0.00054	0.00666	0.84005	0.14457	0.01087	0.00060	0.00060	0.28562	0.99694
0.5	0.00106	0.01041	0.75008	0.26551	0.00819	0.00065	0.00065	0.31933	0.99668
0.6	0.00184	0.01499	0.64001	0.42320	0.00559	0.00072	0.00072	0.34983	0.99632

0.7	0.00292	0.02041	0.51013	0.60522	0.00327	0.00082	0.00081	0.37782	0.99582
0.8	0.00435	0.02665	0.36014	0.78833	0.00146	0.00095	0.00095	0.40386	0.99512
0.9	0.00619	0.03378	0.19010	0.93669	0.00035	0.00116	0.00116	0.42830	0.99399
1.0	0.00850	0.04165	0.00000	1.00000	0.00000	0.00153	0.00153	0.45147	0.99203

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Source of support: Nil, Conflict of interest: None Declared